

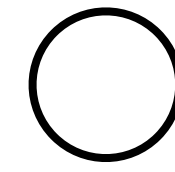
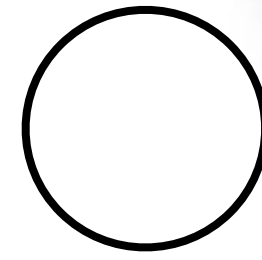
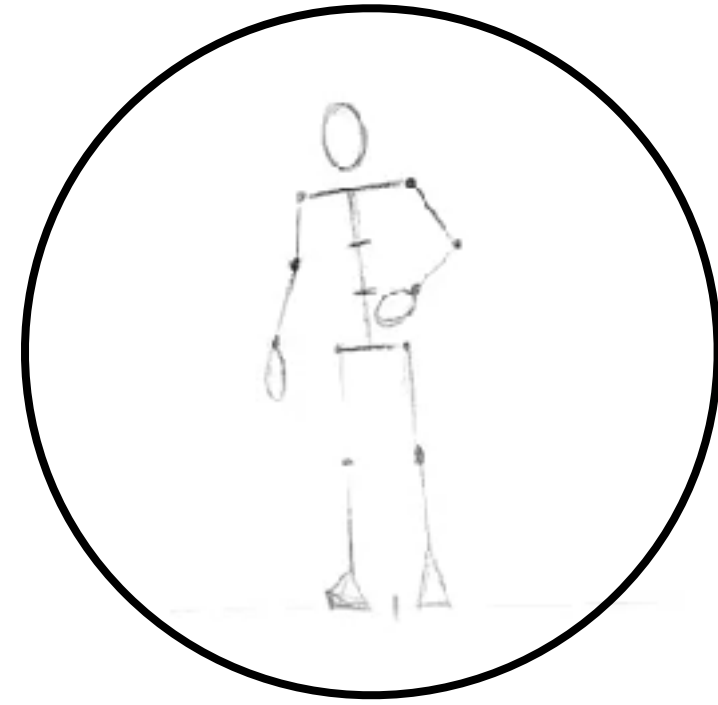
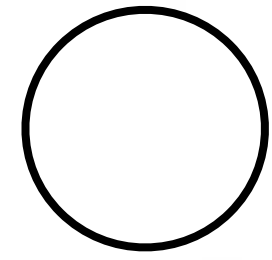
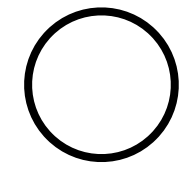
# Learning Symmetric and Low-energy Locomotion

Wenhao Yu, Greg Turk, C. Karen Liu  
Georgia Institute of Technology

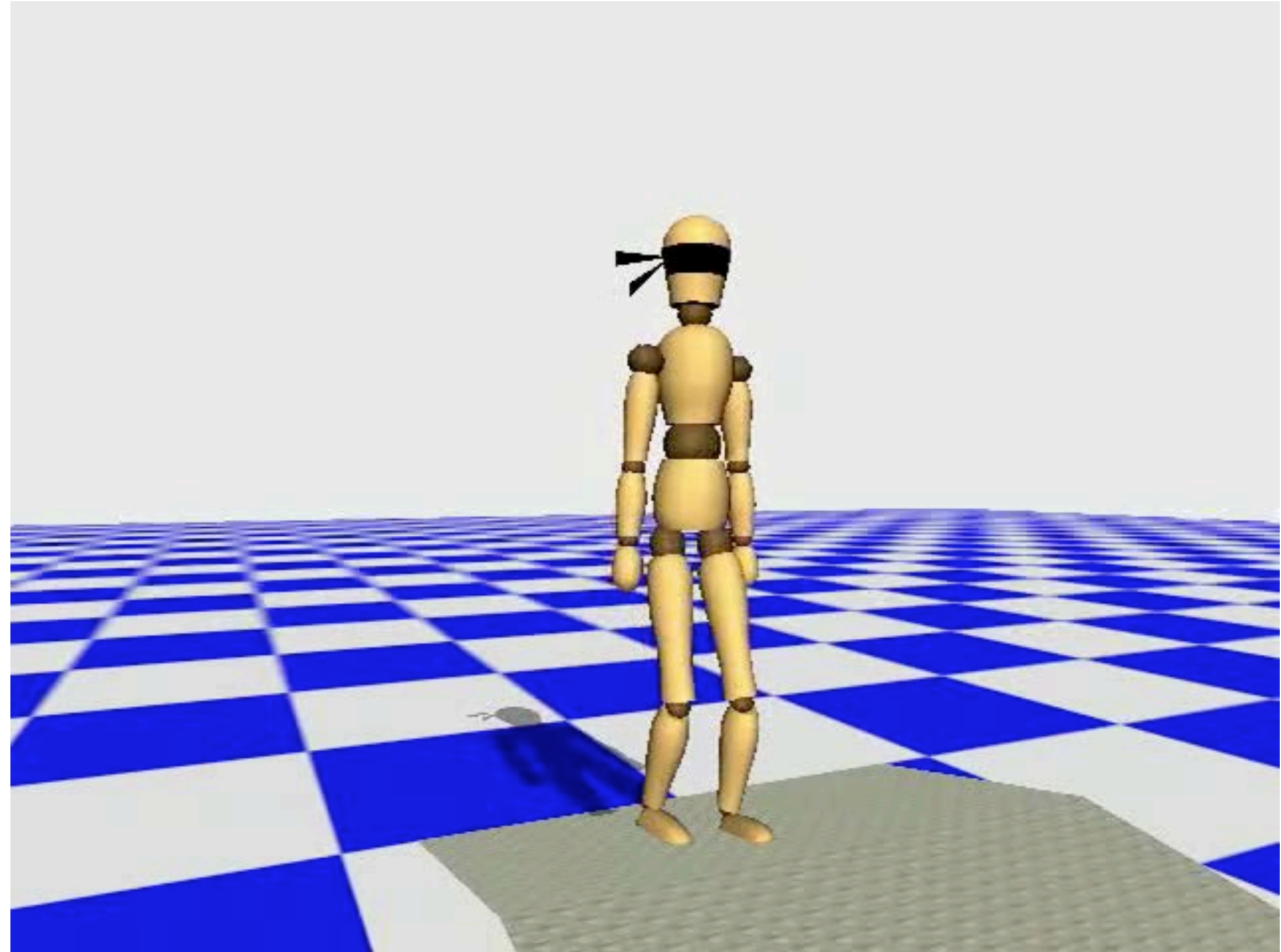
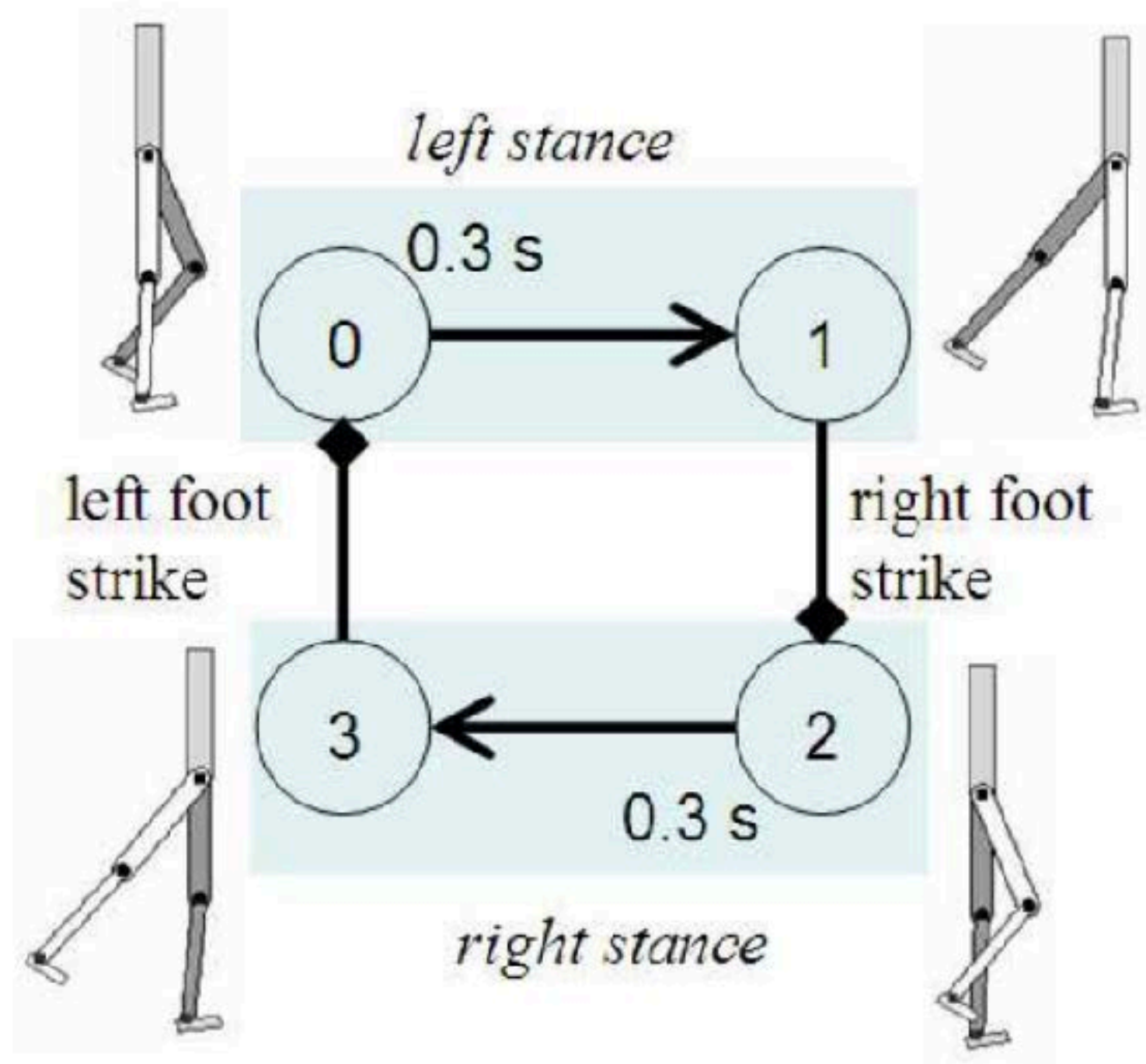




<https://www.ncbi.nlm.nih.gov/pmc/articles/PMC3591461/>  
<https://www.youtube.com/watch?v=Wz3beWec7D4>



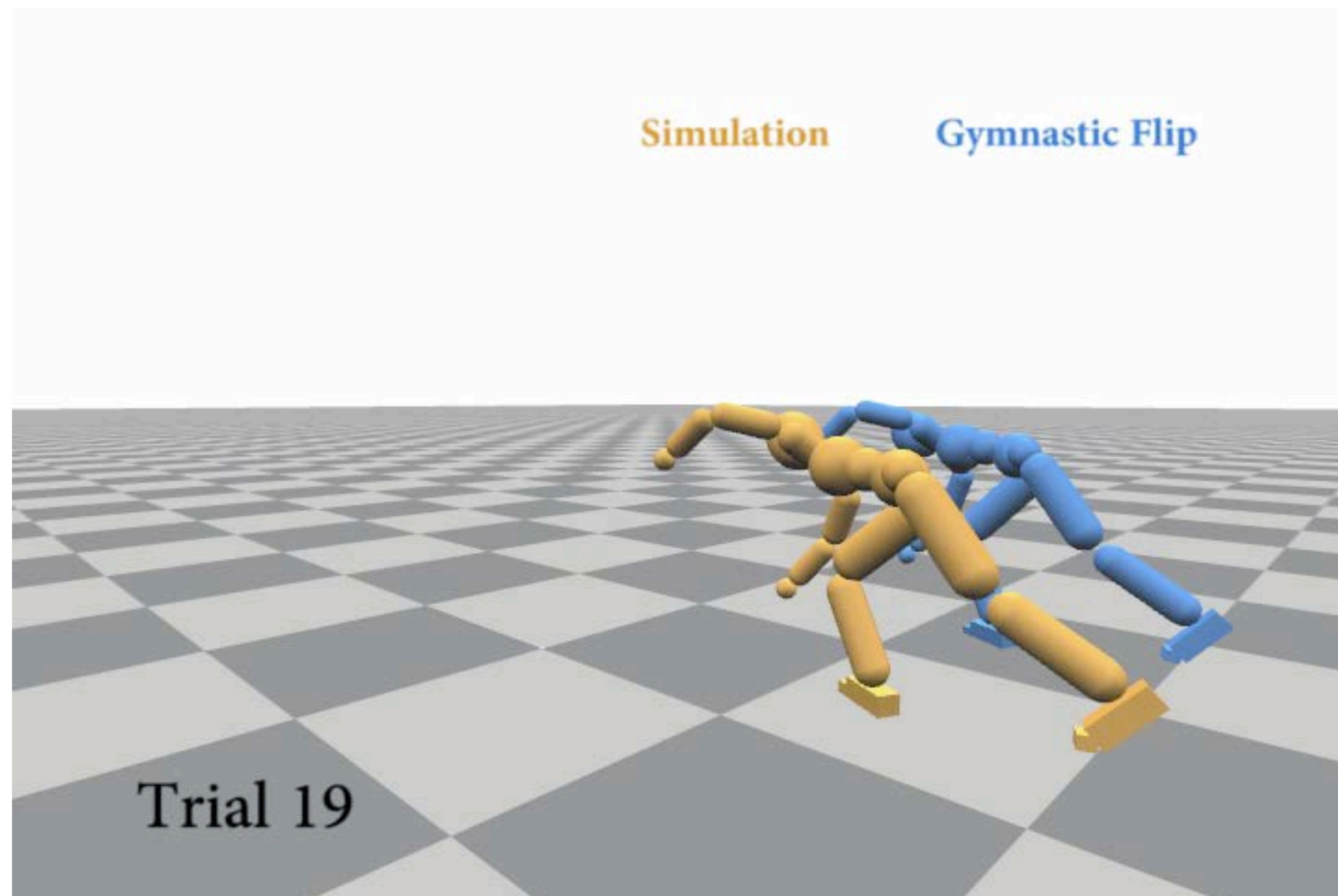
[Robotis OP2]



[Yin et al. 2009]

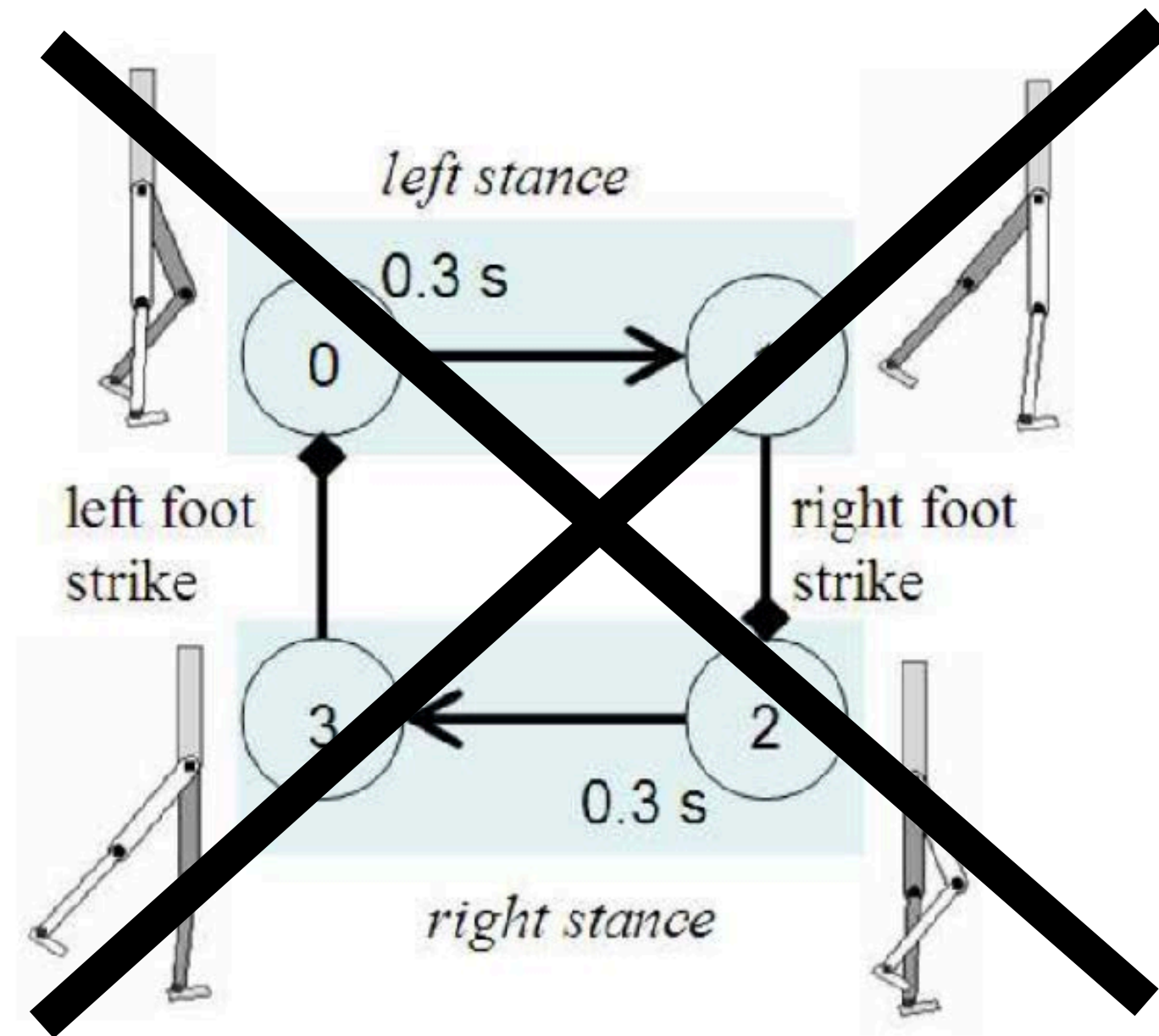


[OptiTrack]



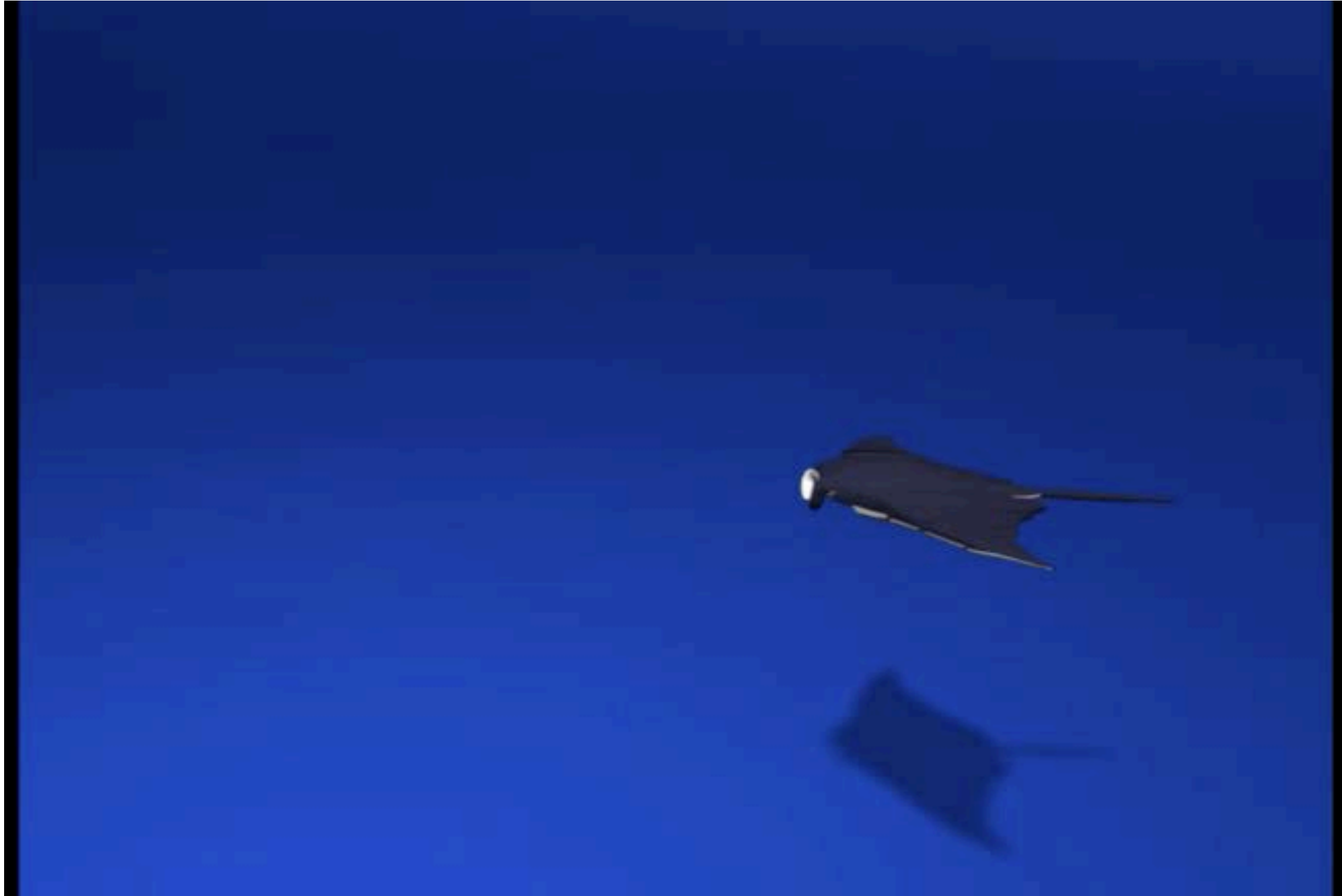
[Liu et al. 2015]

No FSM



No Mocap





[Tan et al. 2011]

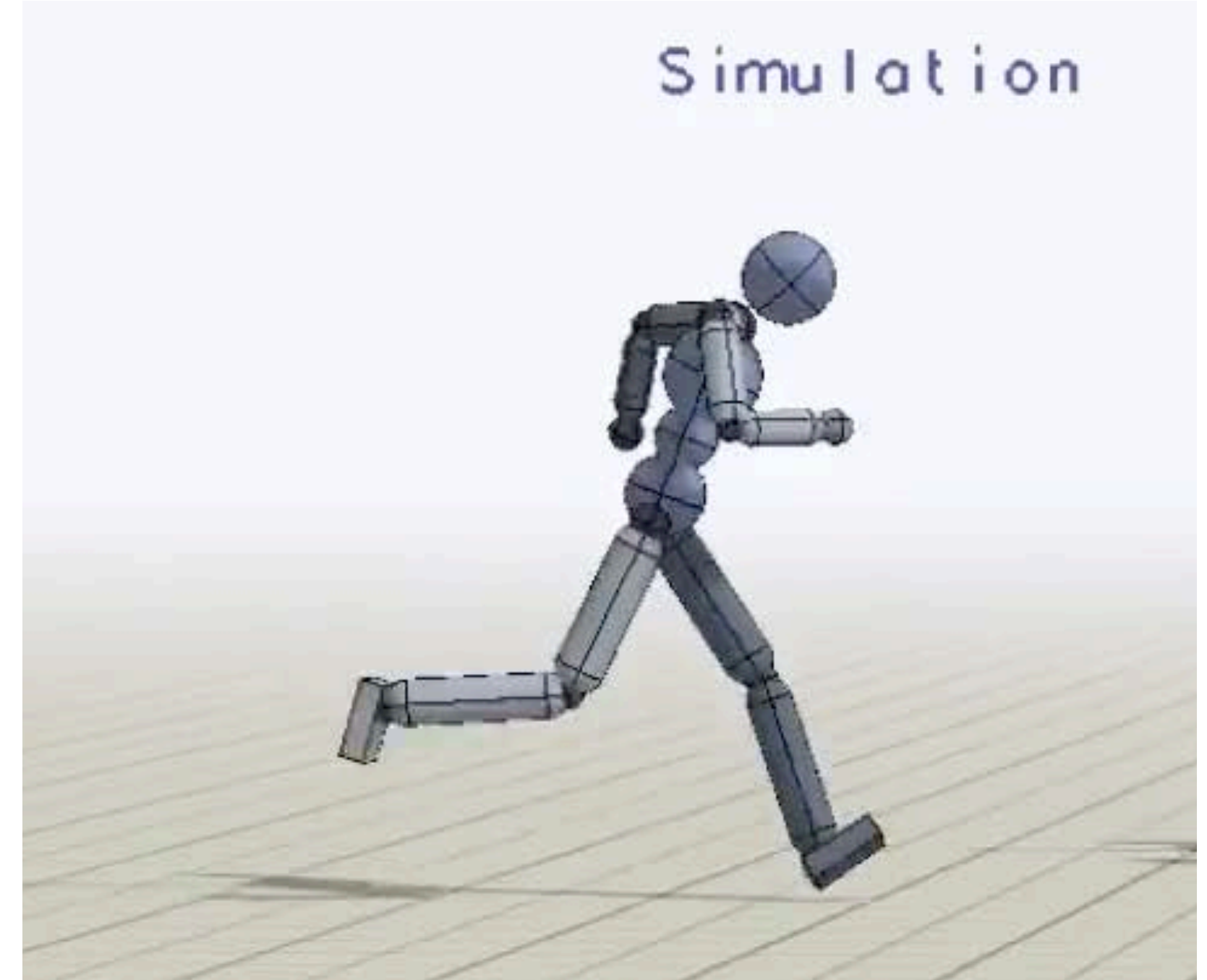


[Tan et al. 2014]



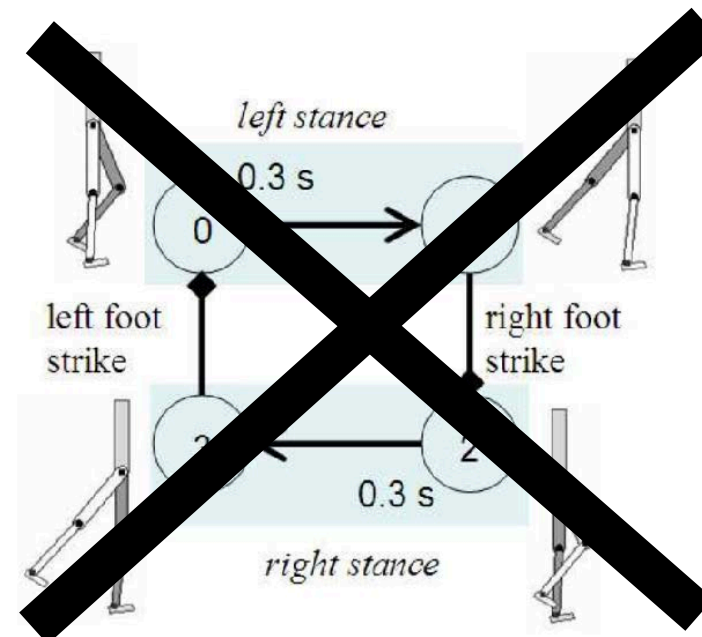


[Heess et al. 2017]



[Peng et al. 2018]

# Deep Reinforcement Learning



Deep Reinforcement  
Learning

**1.0 m/s**



**3.0 m/s**



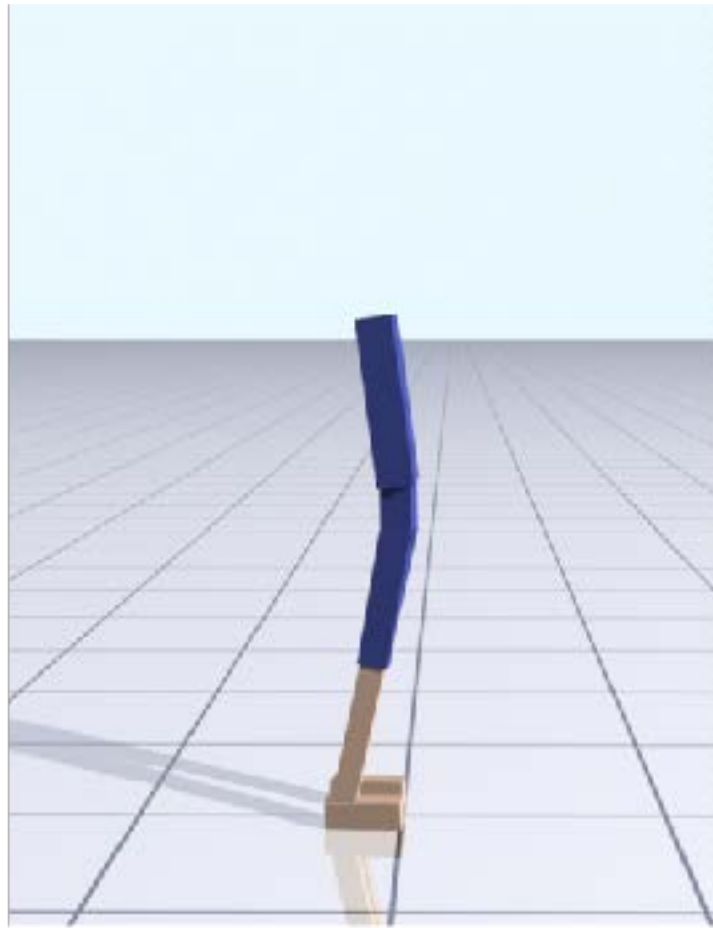
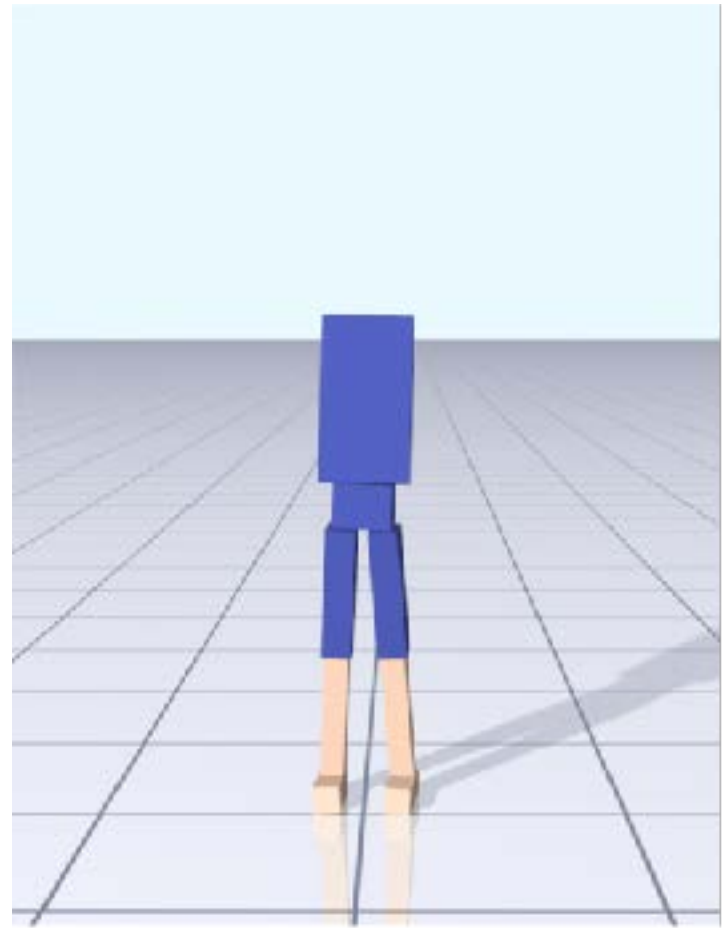
Deep Reinforcement  
Learning

+

Energy Minimization

+

Gait Symmetry

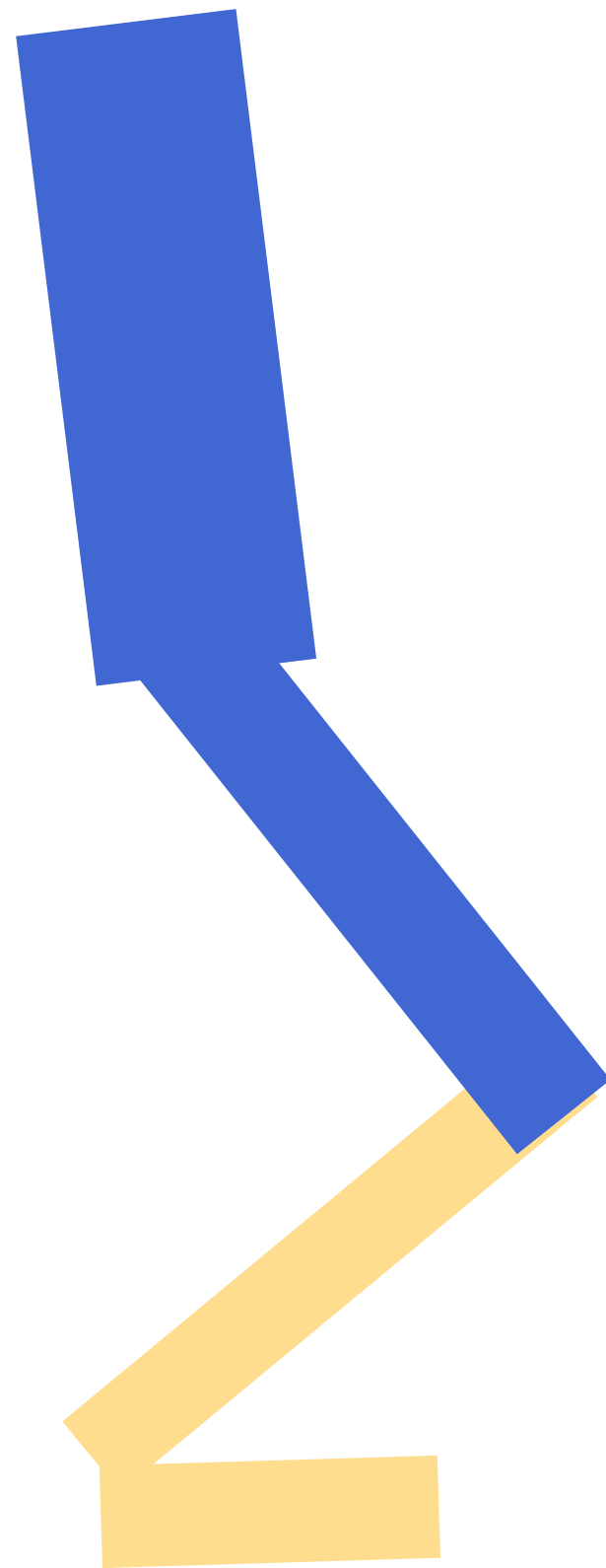


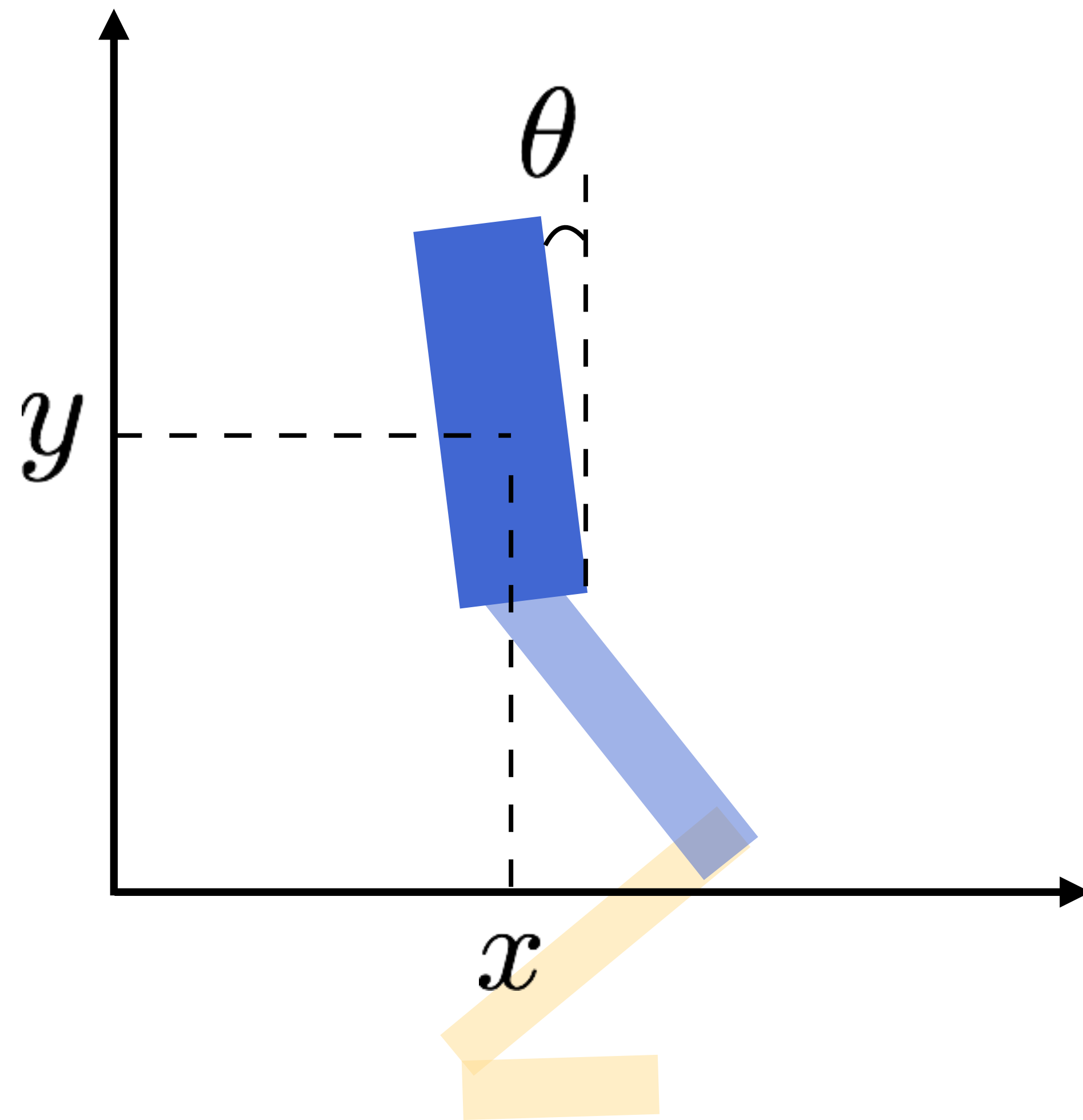
Deep Reinforcement Learning



?

State:



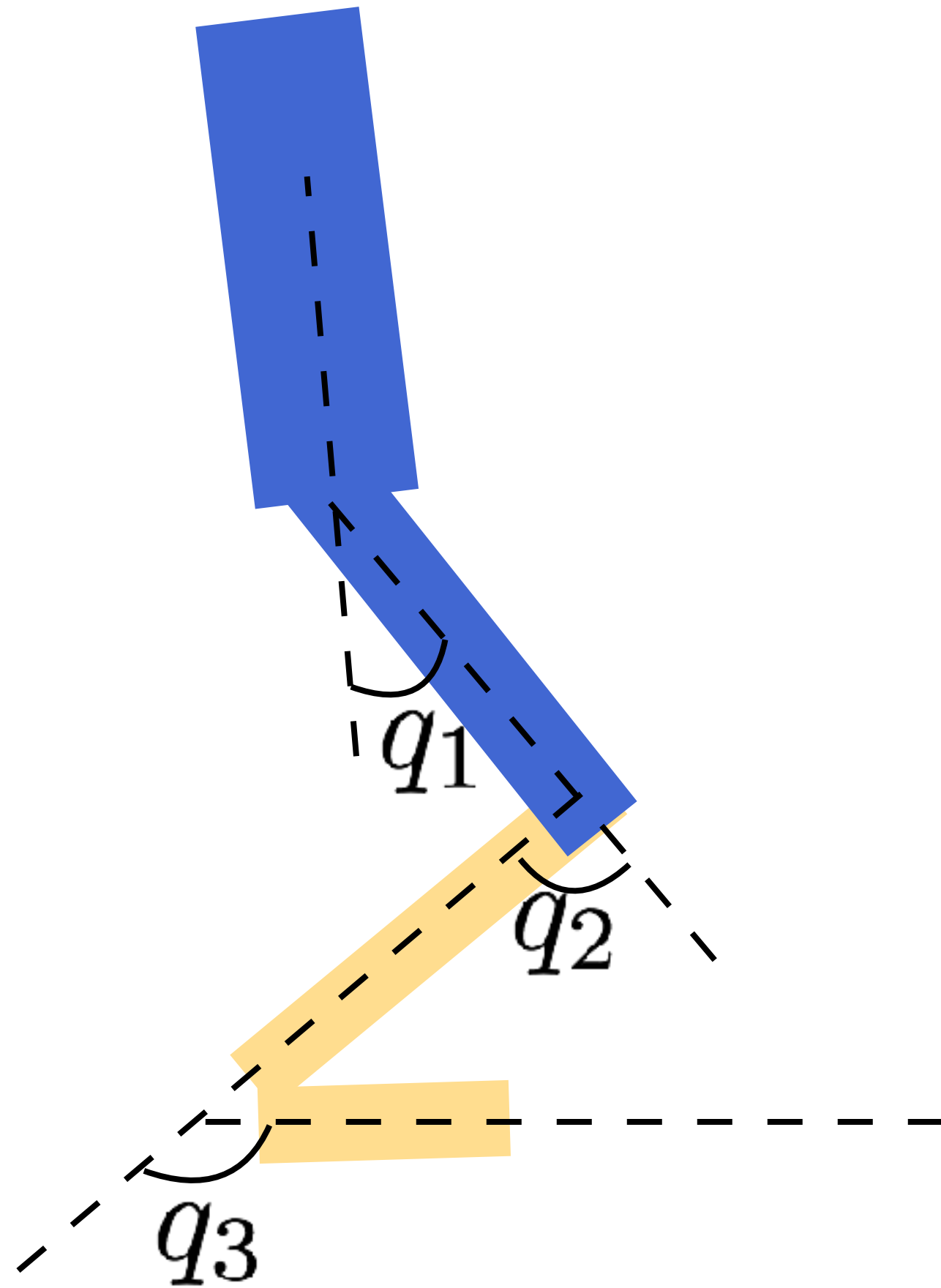


State:

$$\mathbf{s} = [x, y, \theta]$$

State:

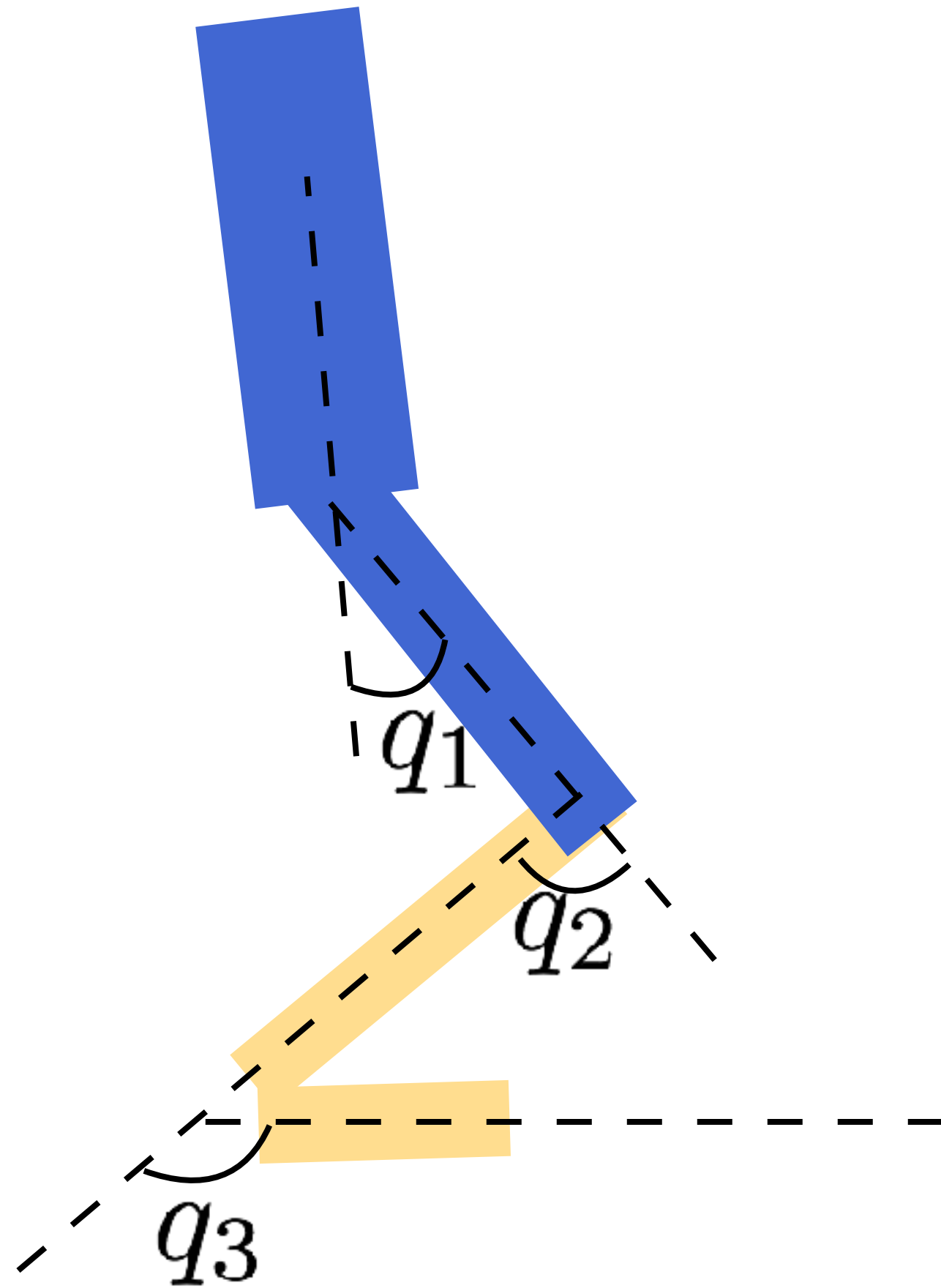
$$\mathbf{s} = [x, y, \theta, q_1, q_2, q_3]$$

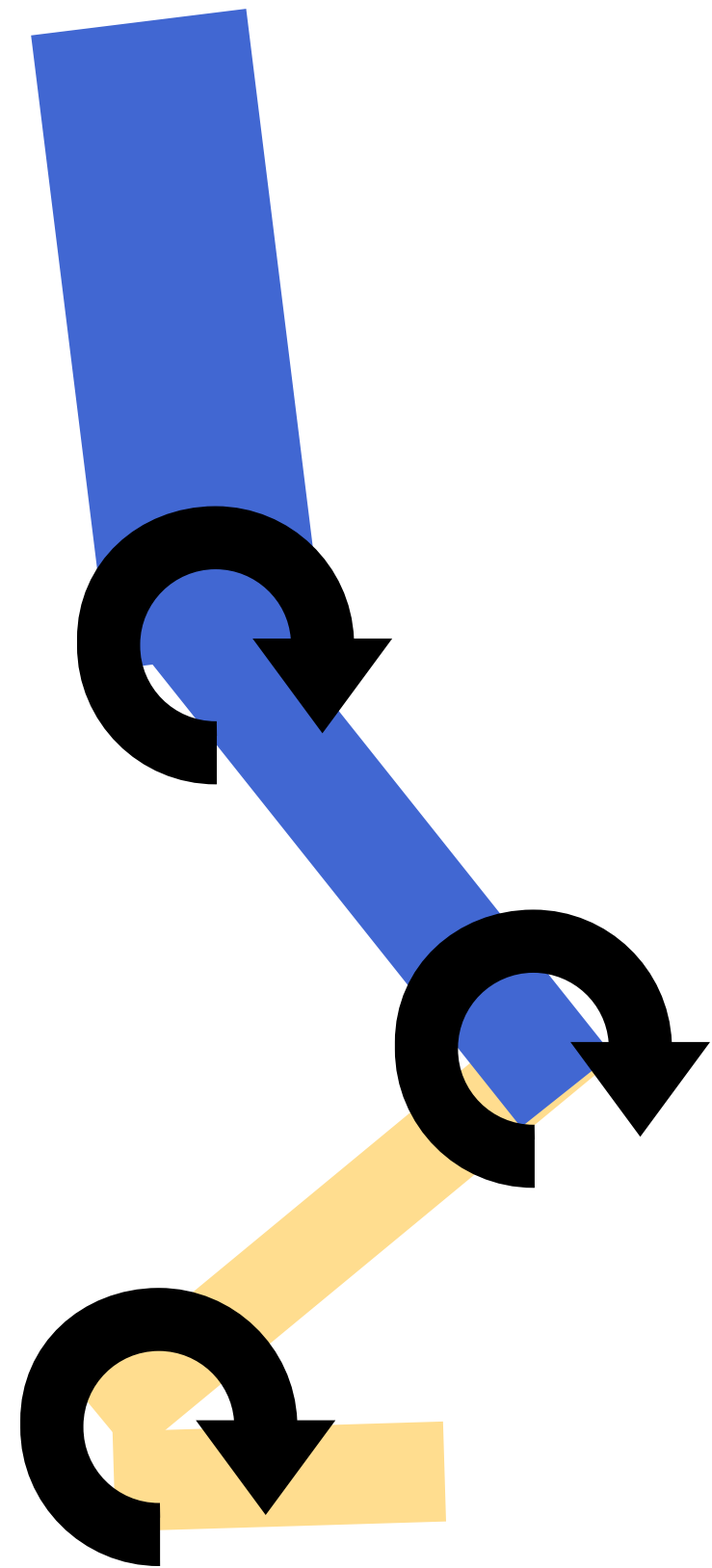




State:

$$\mathbf{s} = [x, y, \theta, q_1, q_2, q_3, \dot{x}, \dot{y}, \dot{\theta}, \dot{q}_1, \dot{q}_2, \dot{q}_3]$$



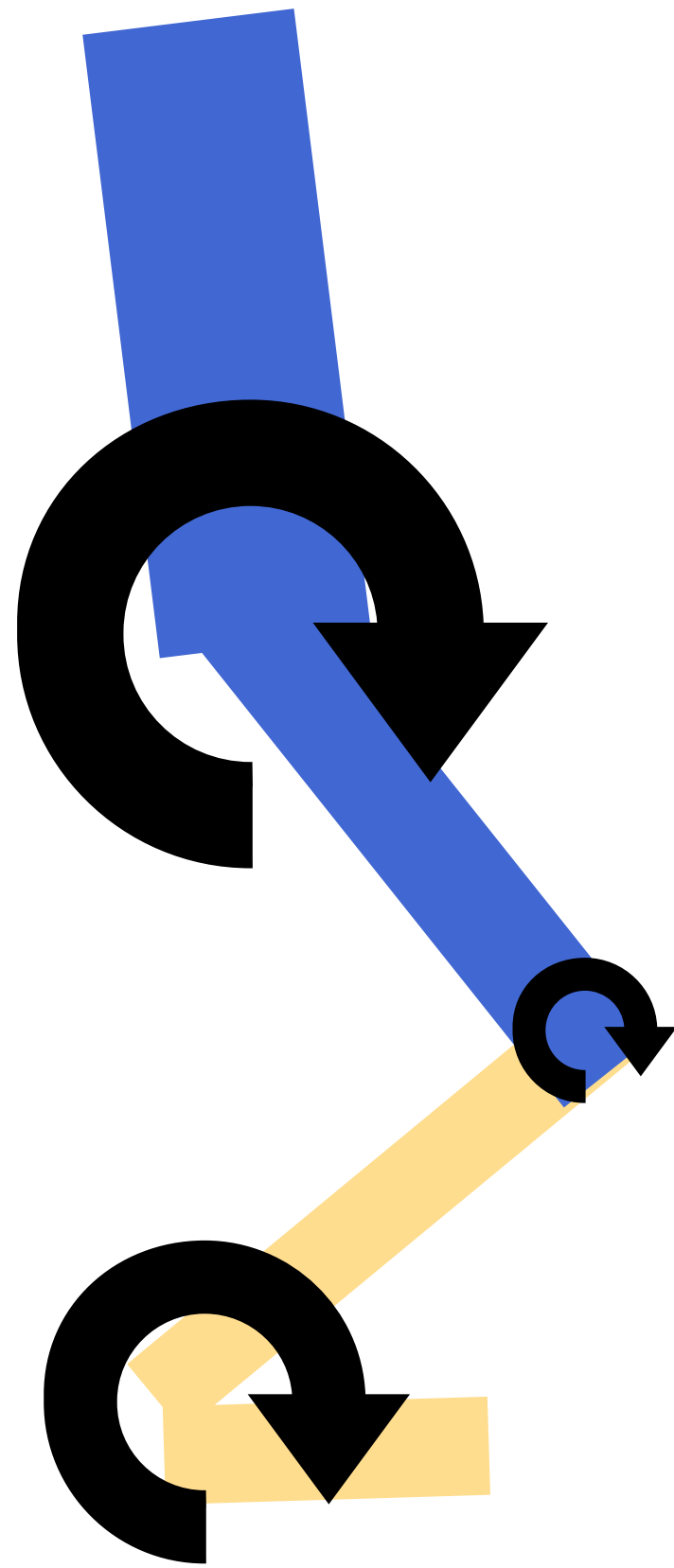


State:

$$\mathbf{s} = [x, y, \theta, q_1, q_2, q_3, \dot{x}, \dot{y}, \dot{\theta}, \dot{q}_1, \dot{q}_2, \dot{q}_3]$$

Action:

$$\mathbf{a} = [a_1, a_2, a_3]$$

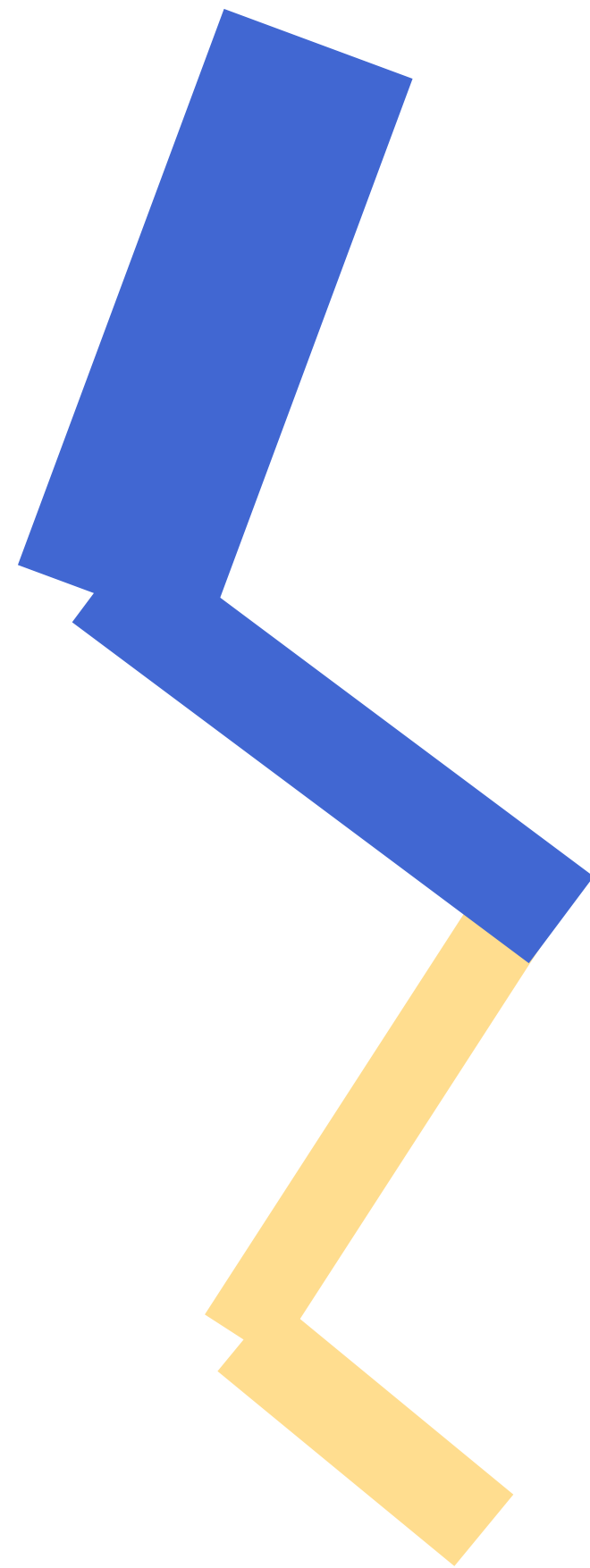


State:

$$\mathbf{s} = [x, y, \theta, q_1, q_2, q_3, \dot{x}, \dot{y}, \dot{\theta}, \dot{q}_1, \dot{q}_2, \dot{q}_3]$$

Action:

$$\mathbf{a} = [a_1, a_2, a_3]$$



State:

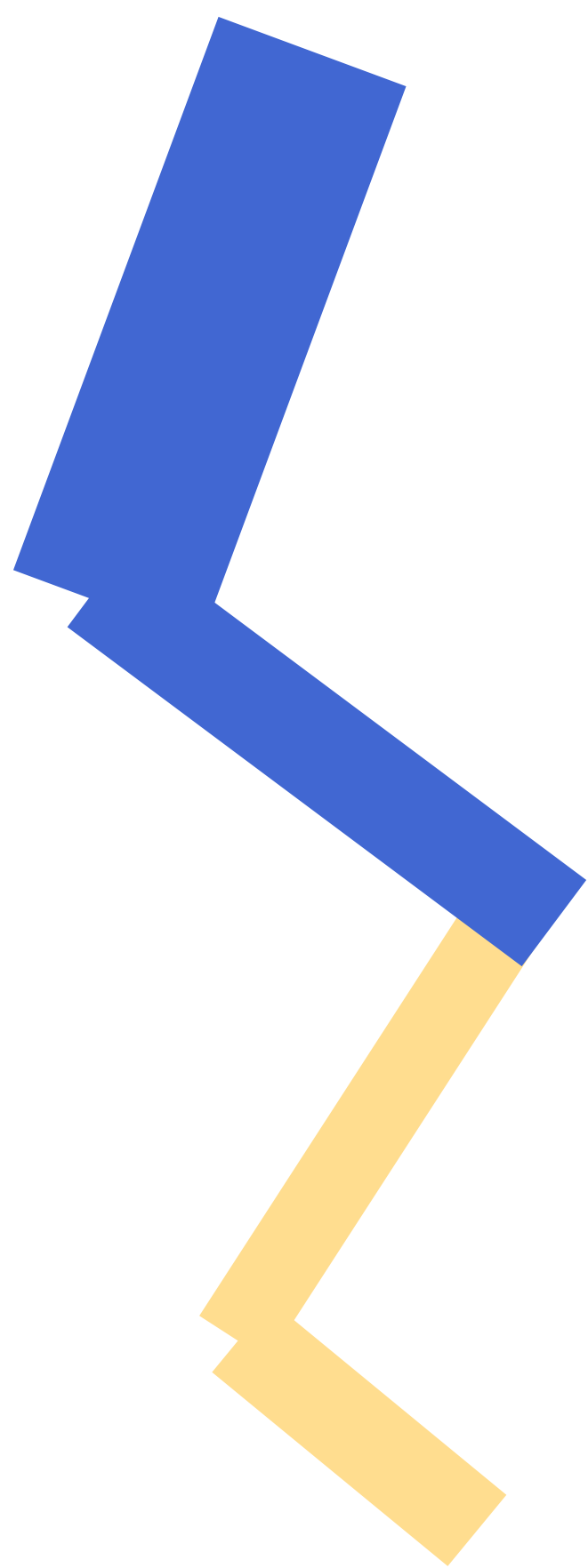
$$\mathbf{s} = [x, y, \theta, q_1, q_2, q_3, \dot{x}, \dot{y}, \dot{\theta}, \dot{q}_1, \dot{q}_2, \dot{q}_3]$$

Action:

$$\mathbf{a} = [a_1, a_2, a_3]$$

Transition:

$$\mathbf{s}^{t+1} = \mathbf{T}(\mathbf{s}^t, \mathbf{a})$$



State:

$$\mathbf{s} = [x, y, \theta, q_1, q_2, q_3, \dot{x}, \dot{y}, \dot{\theta}, \dot{q}_1, \dot{q}_2, \dot{q}_3]$$

Action:

$$\mathbf{a} = [a_1, a_2, a_3]$$

Transition:

$$\mathbf{s}^{\mathbf{t}+1} = \mathbf{T}(\mathbf{s}^{\mathbf{t}}, \mathbf{a})$$

Reward:

$$r = R(\mathbf{s}, \mathbf{a}) = x - \sum_{i=1}^3 |a_i|$$

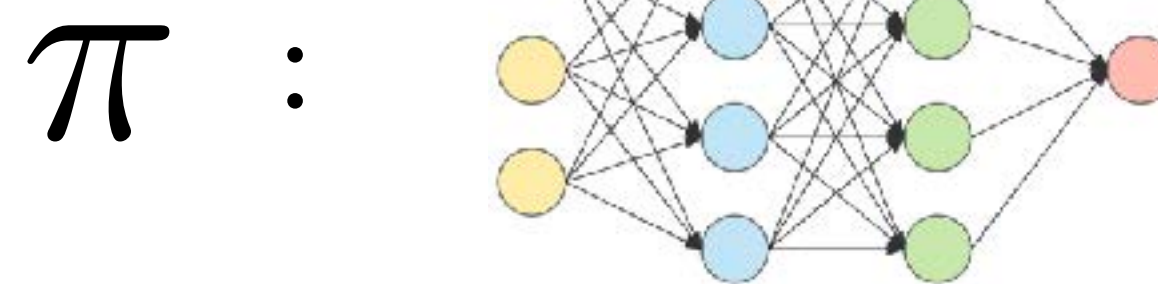
Markov Decision Process:  $\{ \mathbf{s} \quad \mathbf{a} \quad \mathbf{T} \quad R \}$

Control Policy:  $\mathbf{a}_t \sim \pi(\mathbf{a}|\mathbf{s}_t)$

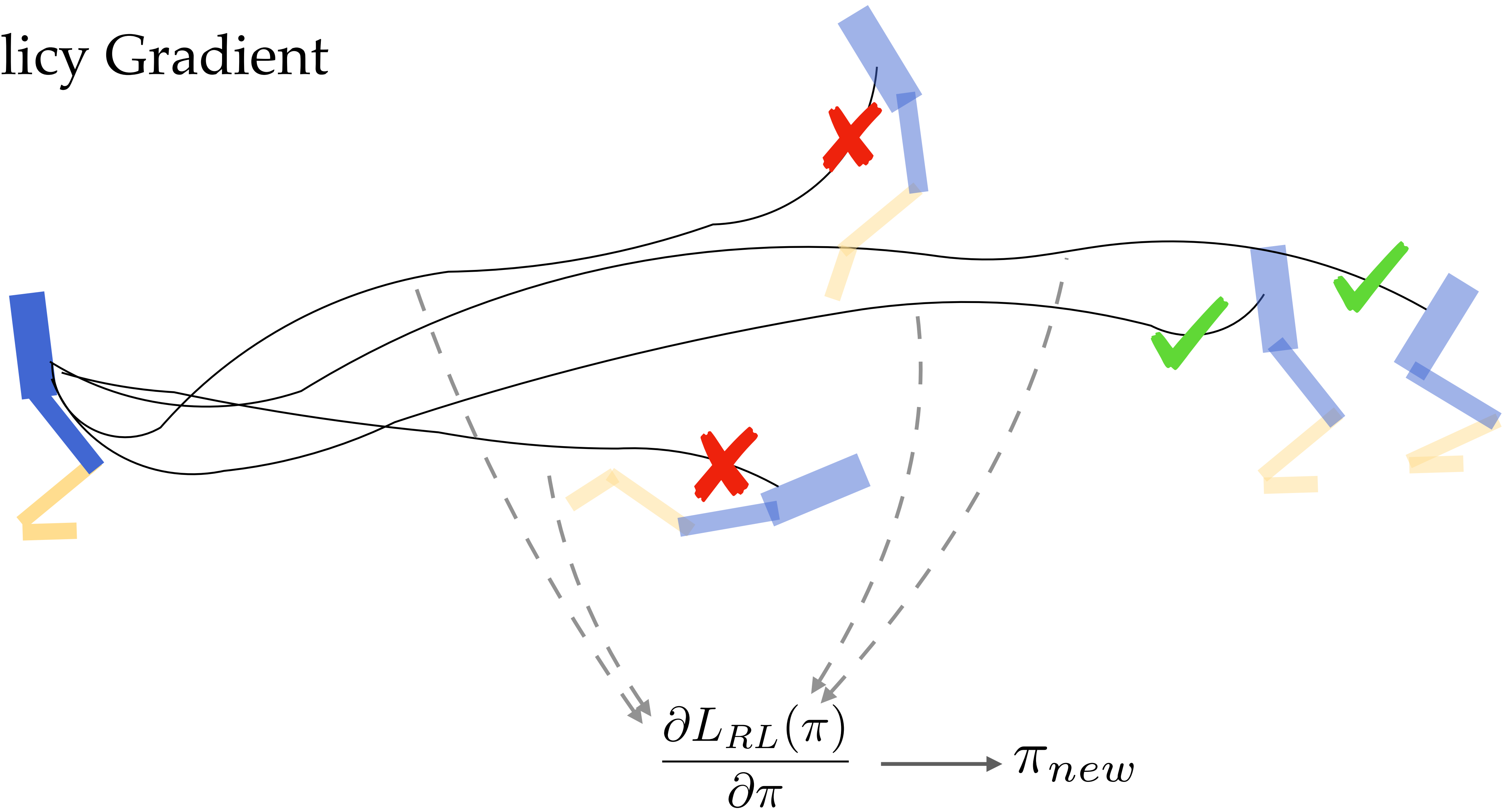
Rollout:  $[\mathbf{s}_0, \mathbf{a}_0, \mathbf{s}_1, \mathbf{a}_1, \dots, \mathbf{s}_T]$

Reinforcement Learning: maximize  $L_{RL}(\pi) = \mathbb{E}[\sum_{t=1}^T R(\mathbf{s}^{t+1}, \mathbf{a}^t)]$

DeepReinforcement Learning:



# Policy Gradient





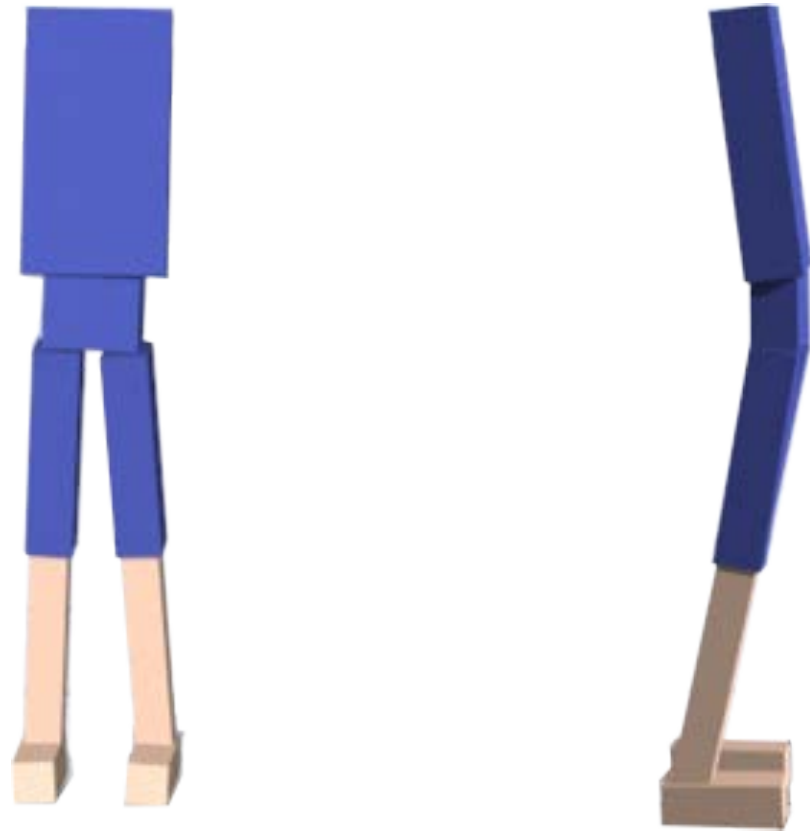
$$\mathbf{s} = [\mathbf{q}, \dot{\mathbf{q}}, \bar{v}, \text{contact}]$$

$$\mathbf{a} = [a_0 - 14]$$

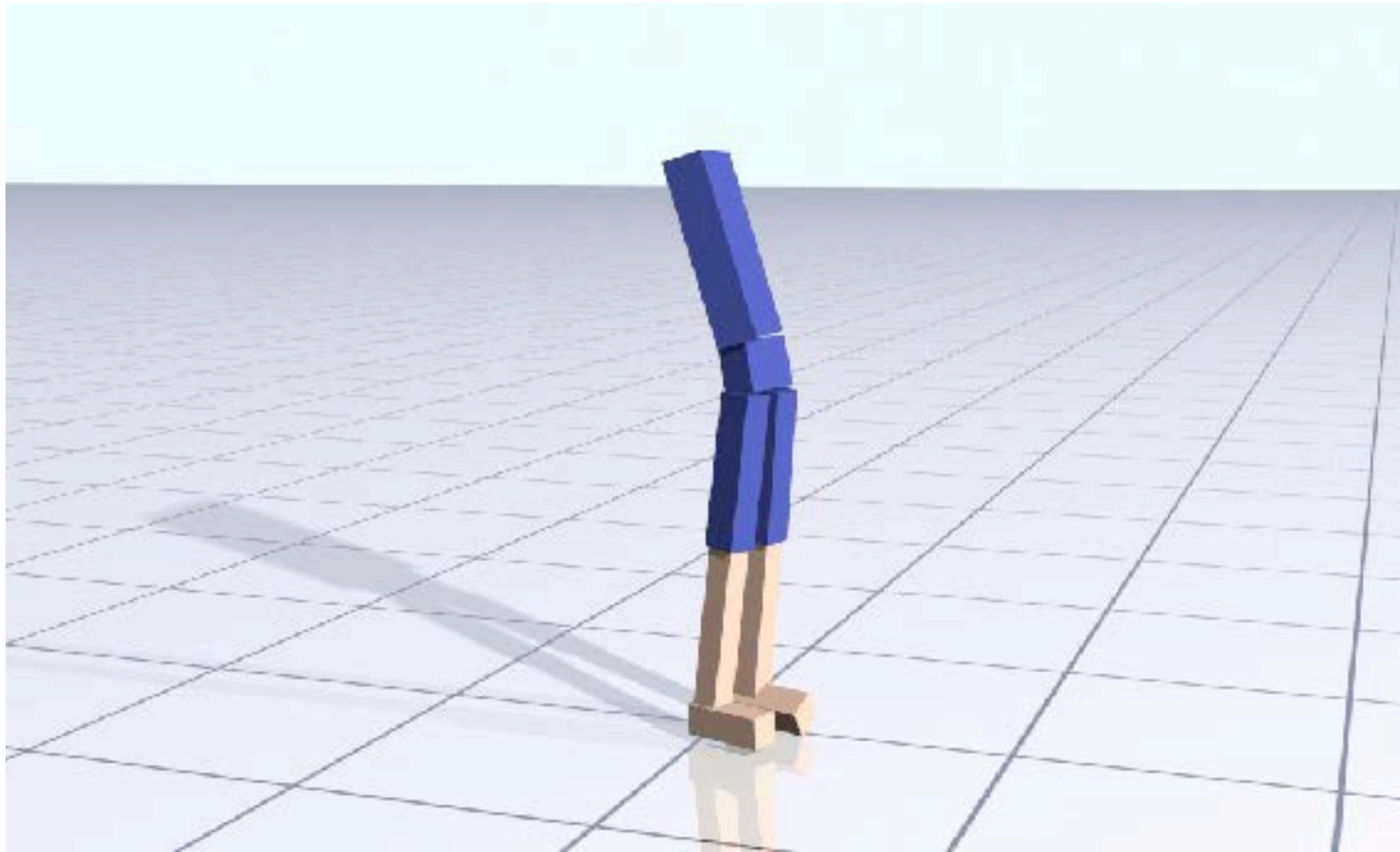
$$\mathbf{T}(\cdot) = \img alt="DART logo: a colorful hexagon with a black arrow pointing to the right." data-bbox="488 451 534 524"/> **DART**  
Dynamic Animation and Robotics Toolkit$$

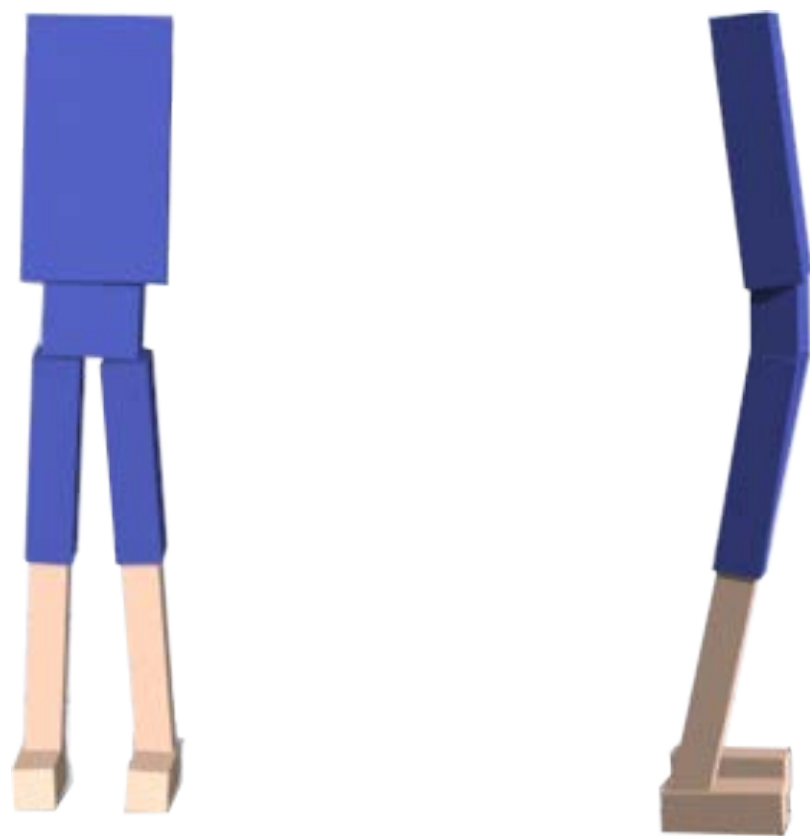
$$R(\mathbf{s}, \mathbf{a}) = -\|v - \bar{v}\| \quad *w_v$$
$$\quad -\|\mathbf{a}\|_1 \quad *w_a \leftarrow$$
$$\quad -\text{LateralDeviation} \quad *w_L$$
$$\quad -\text{TorsoRotation} \quad *w_T$$
$$\quad +\text{AliveBonus}$$



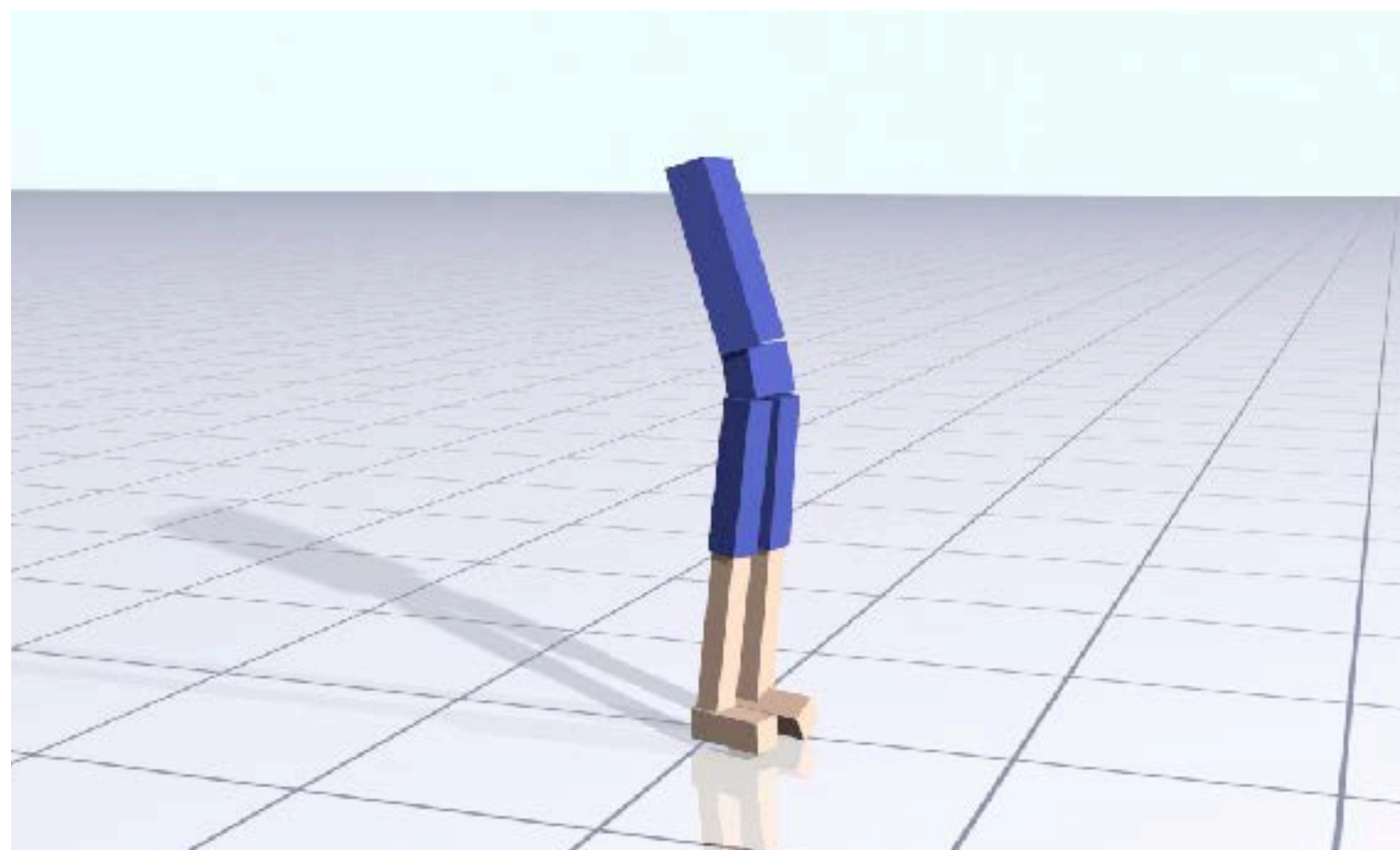


Deep Reinforcement Learning





Deep Reinforcement Learning



+

Curriculum Learning

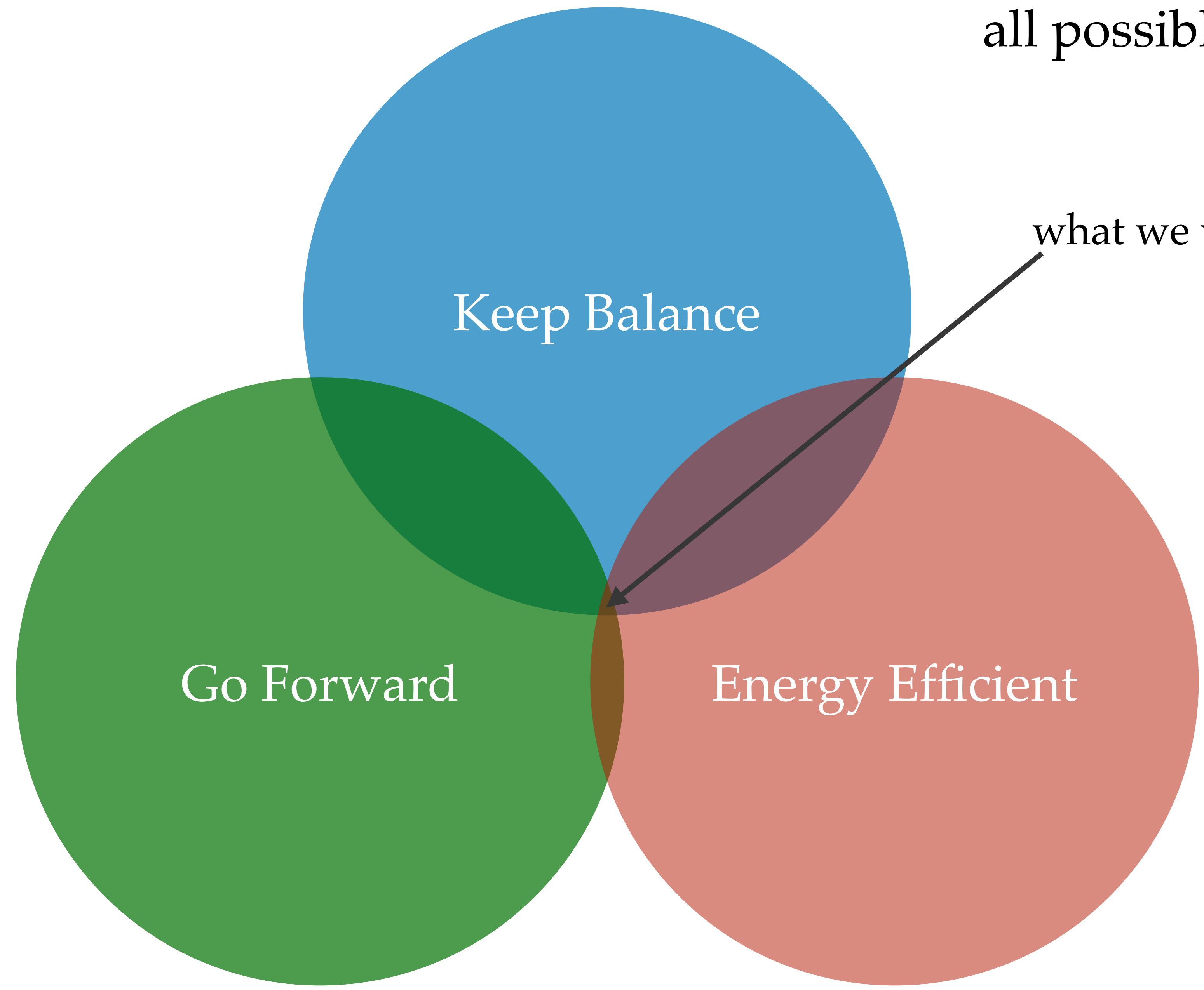


Energy Minimization



?

all possible gaits



Keep Balance

Go Forward

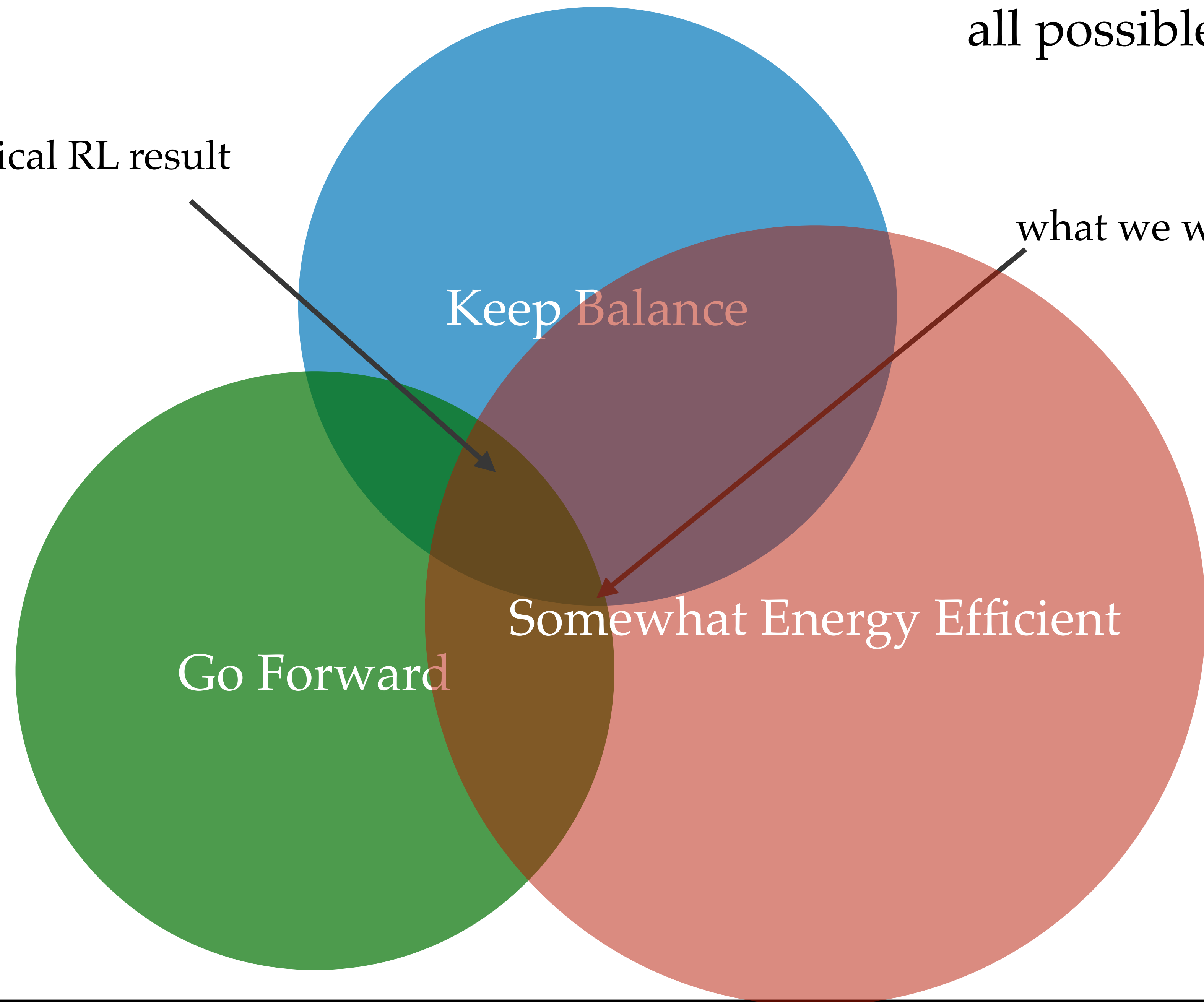
Energy Efficient

what we want

all possible gaits

typical RL result

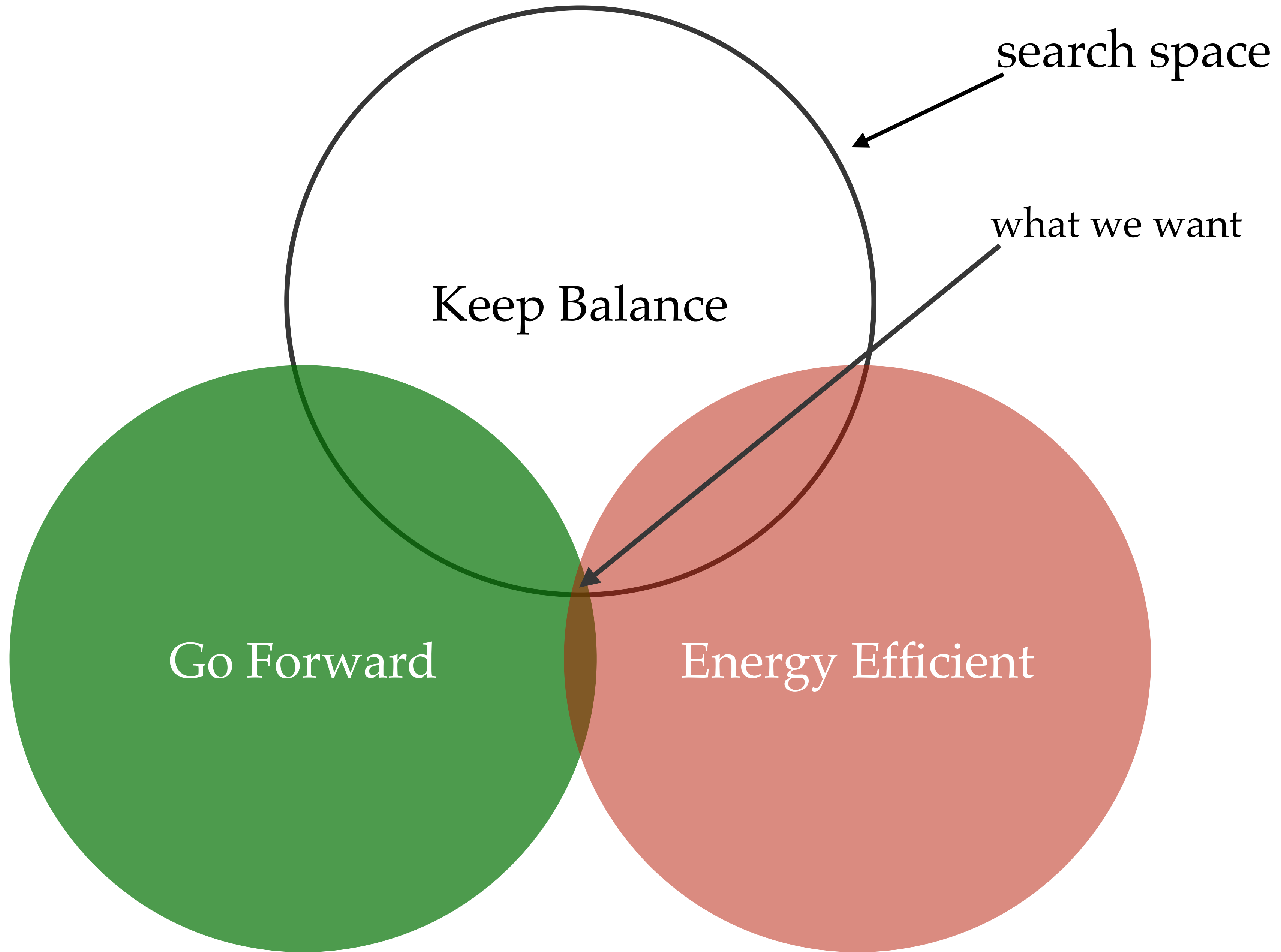
what we want

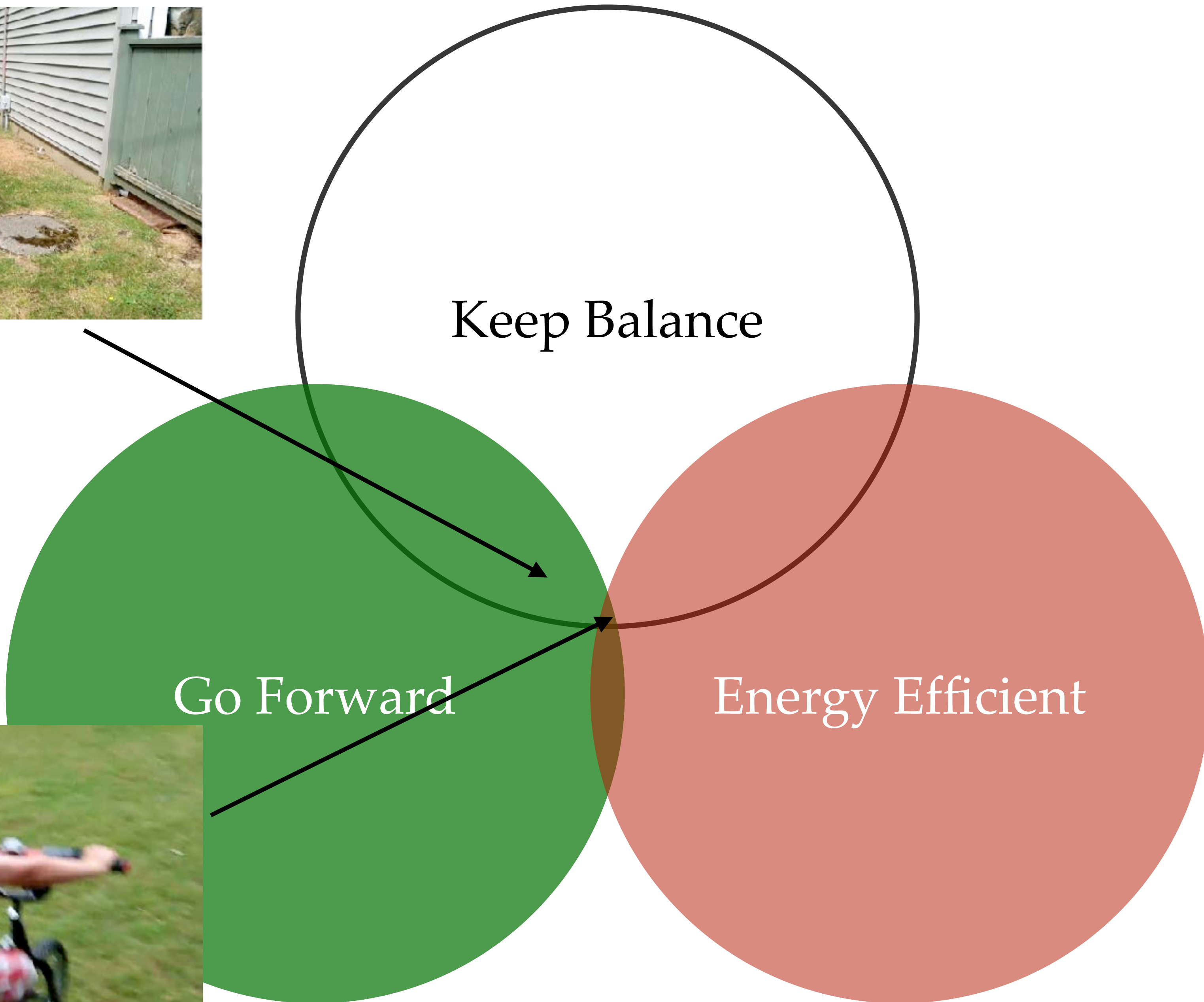


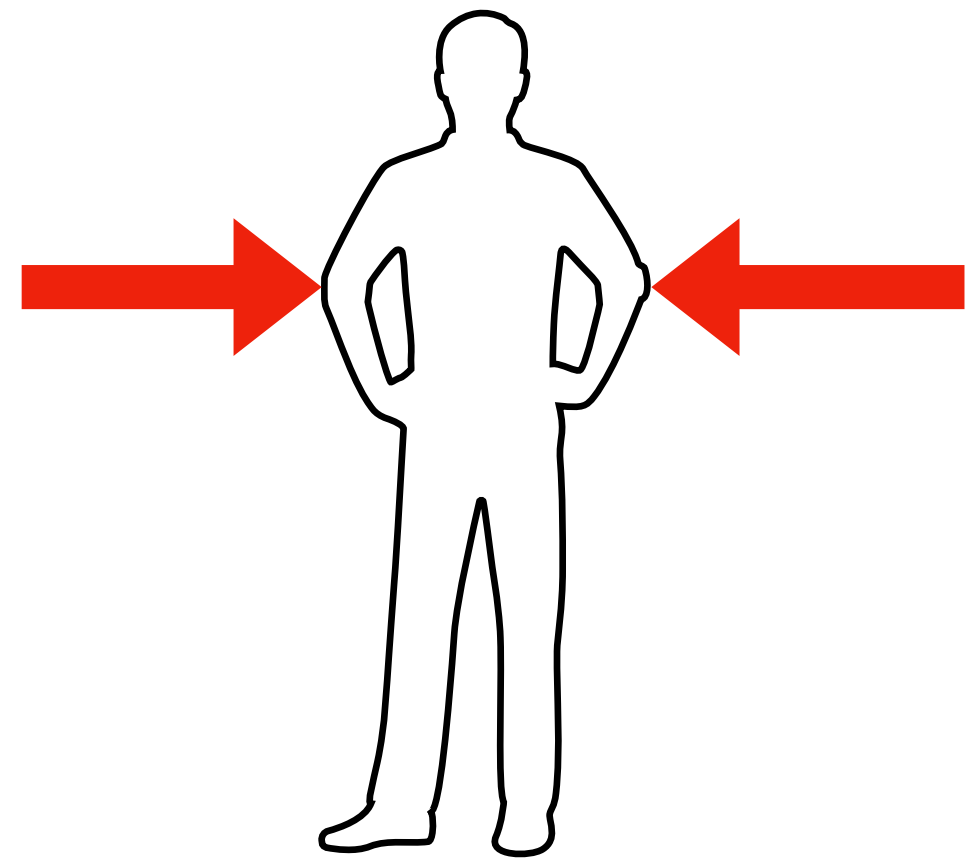
Keep Balance

Go Forward

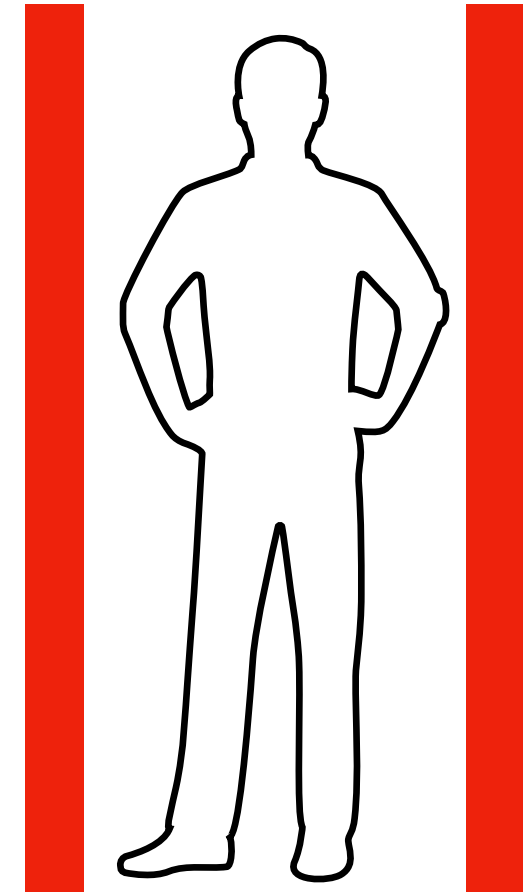
Somewhat Energy Efficient



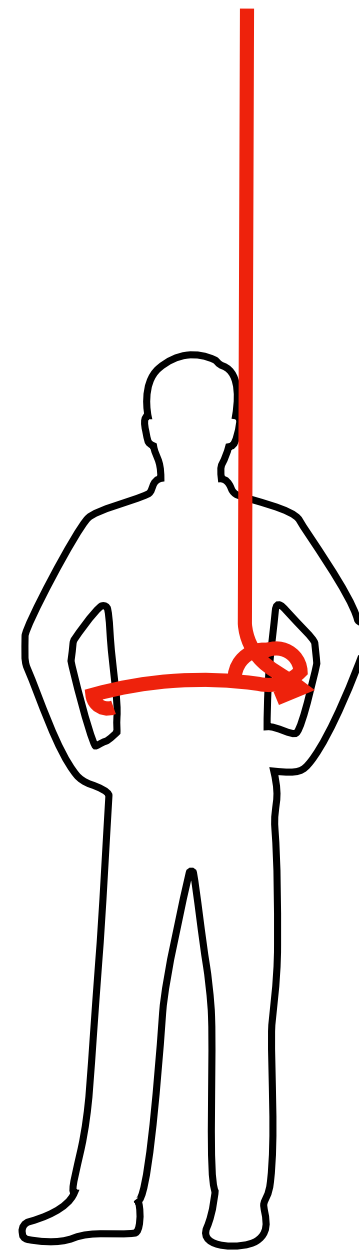




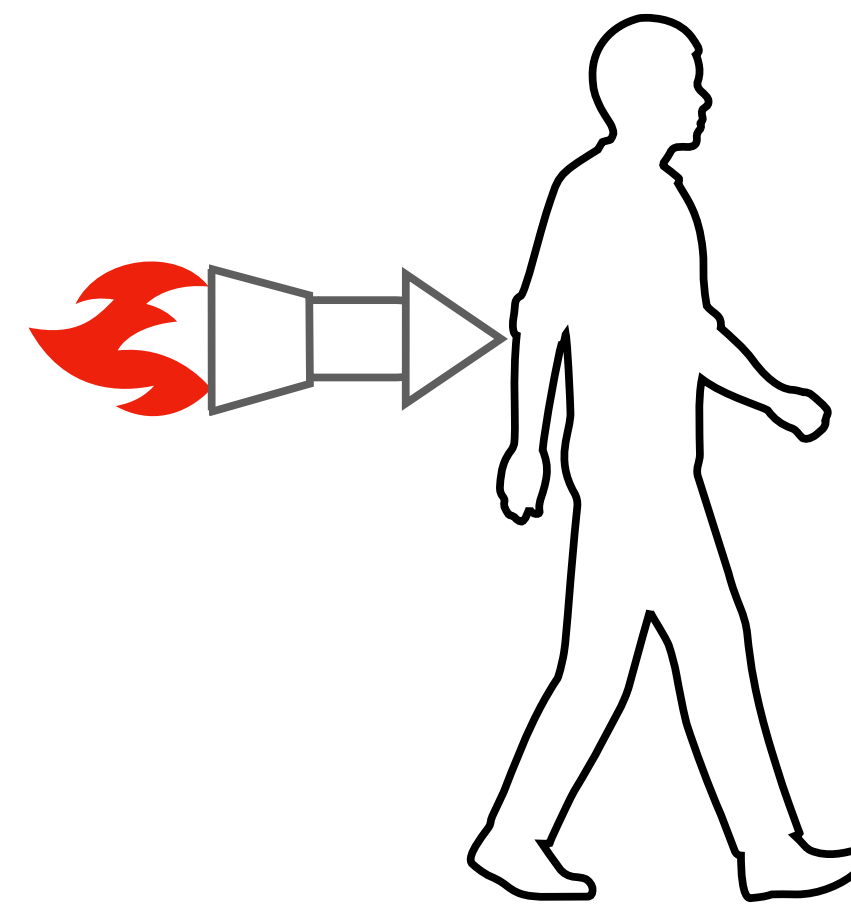
lateral push



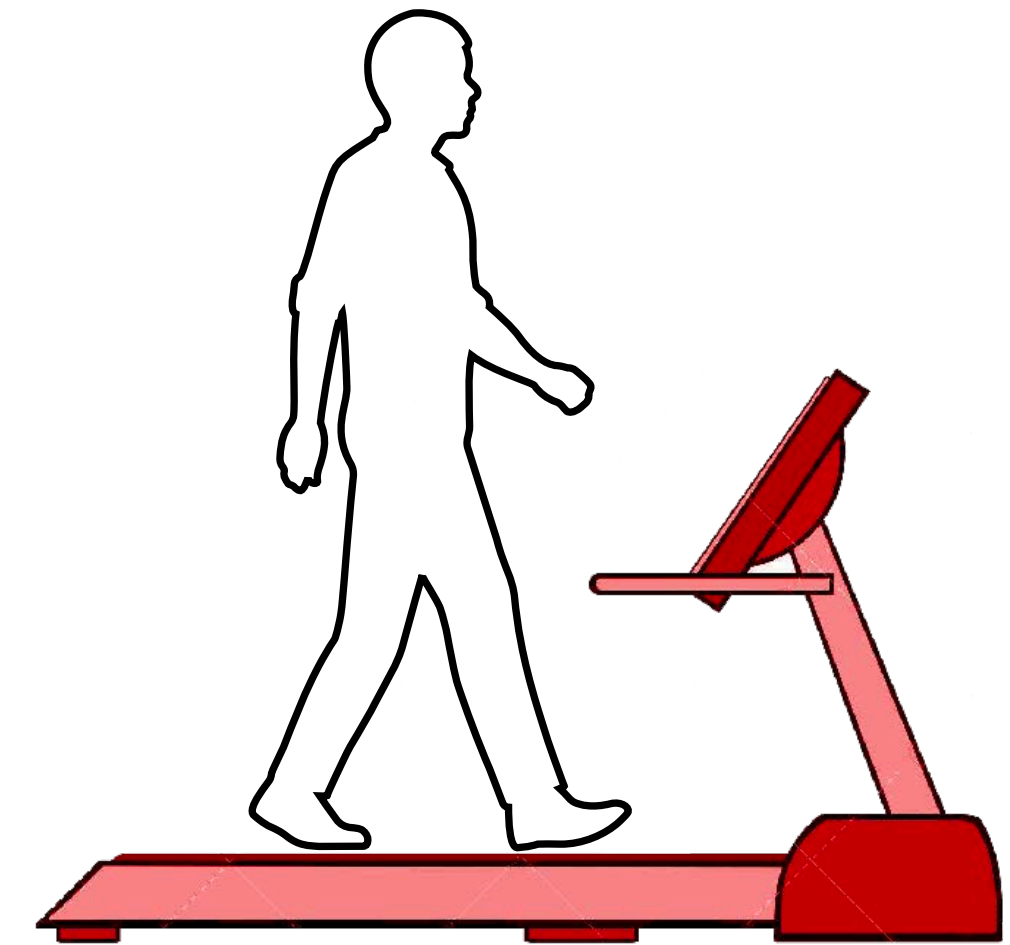
walls



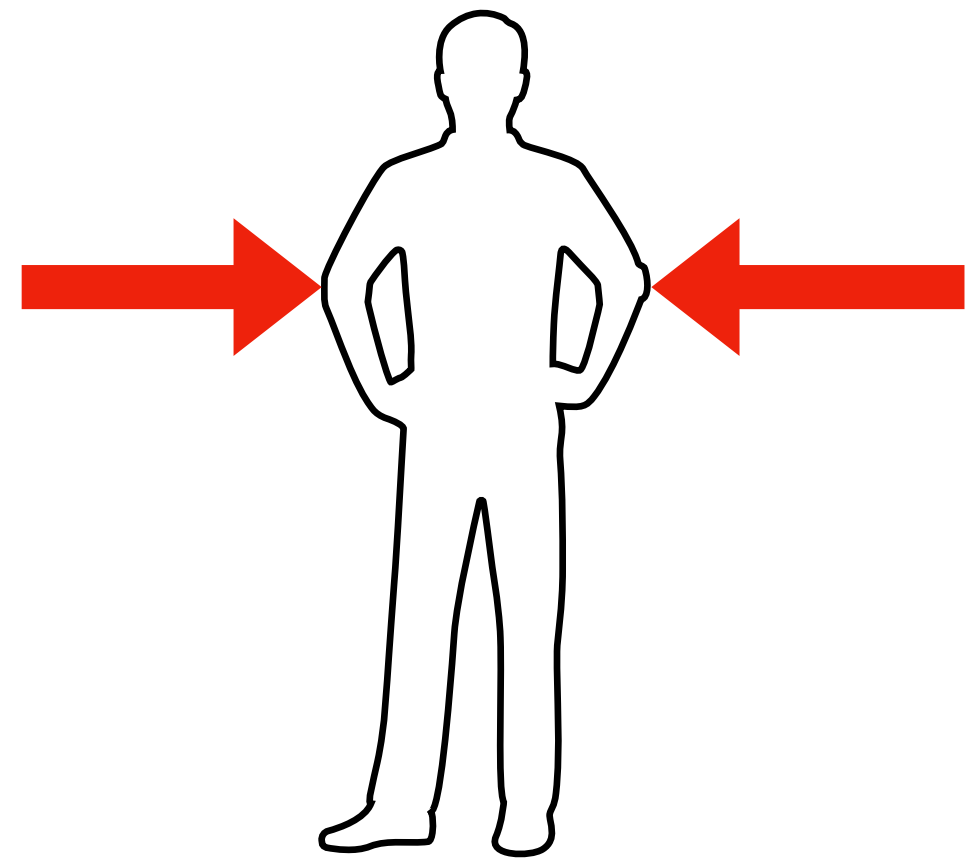
waist support



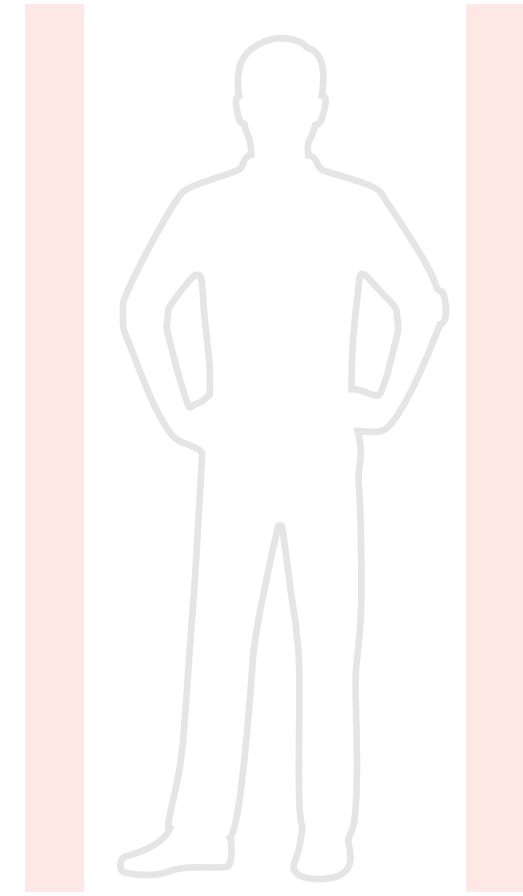
propel forward



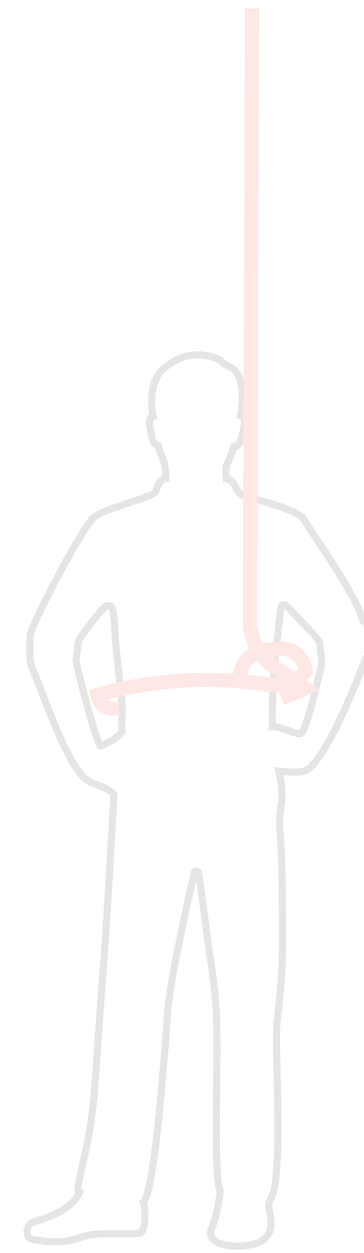
treadmill



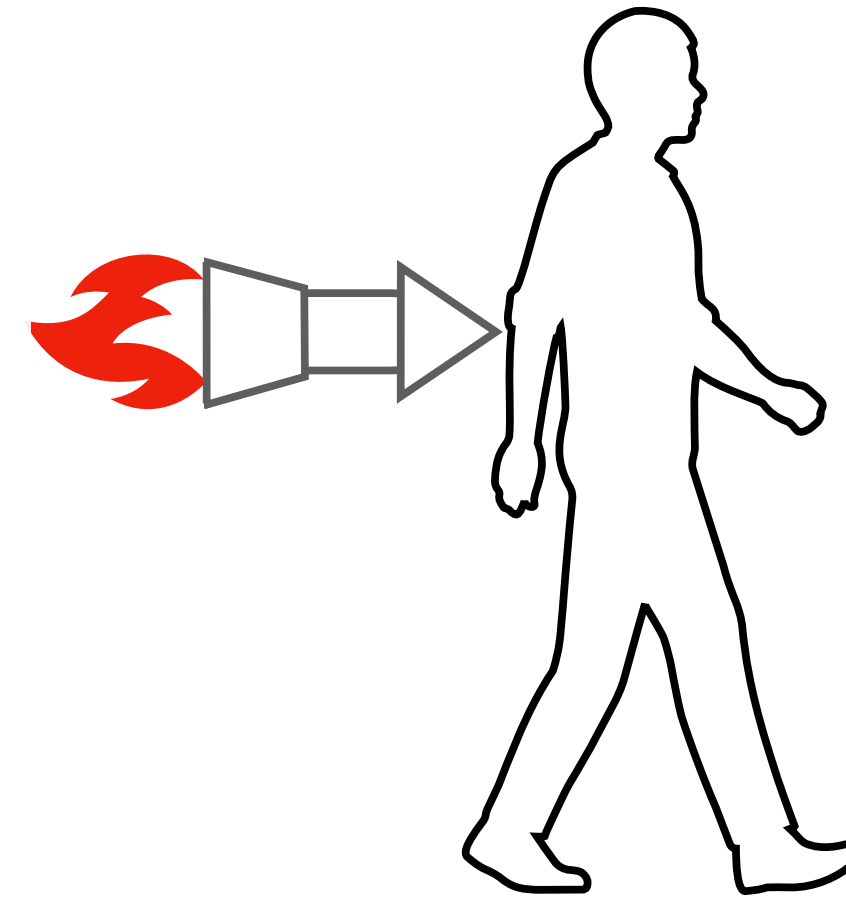
lateral push



walls



waist support



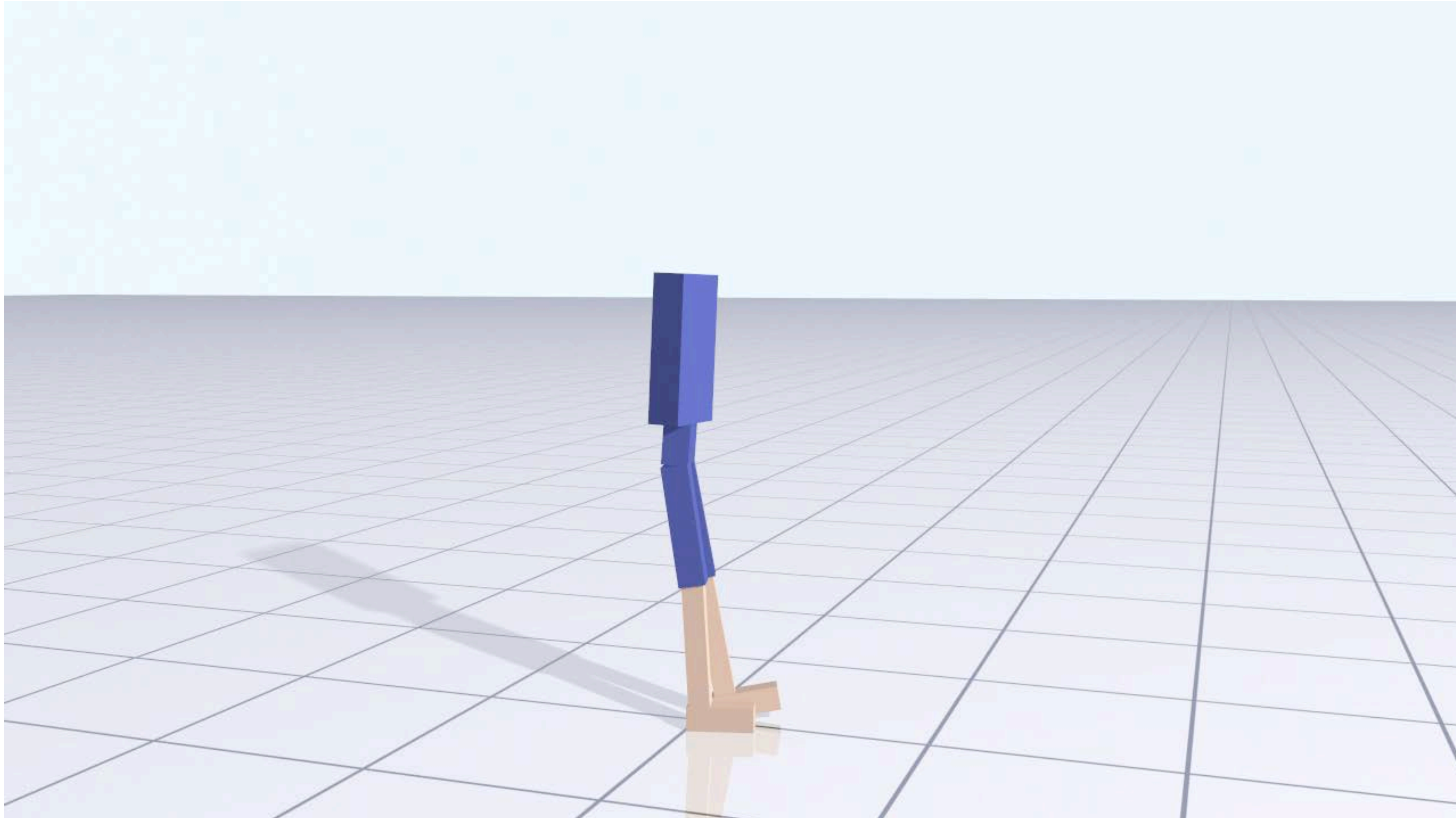
propel forward



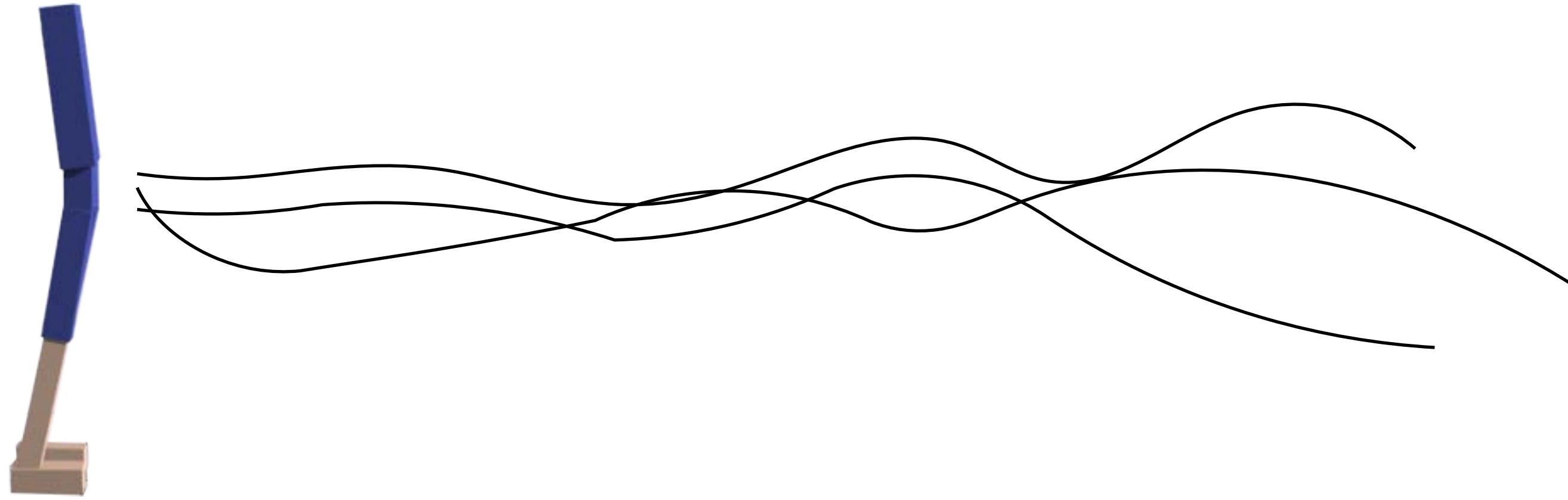
treadmill



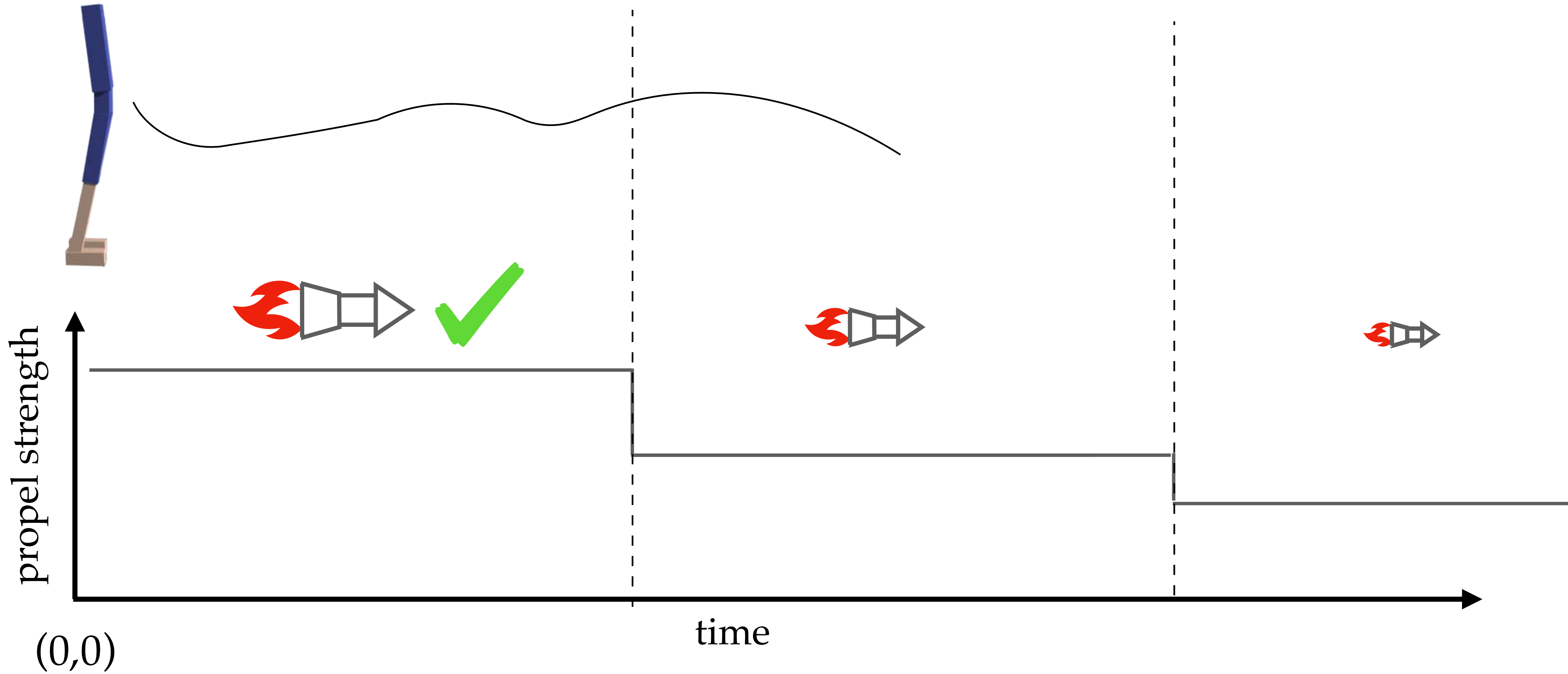
# With Assistance



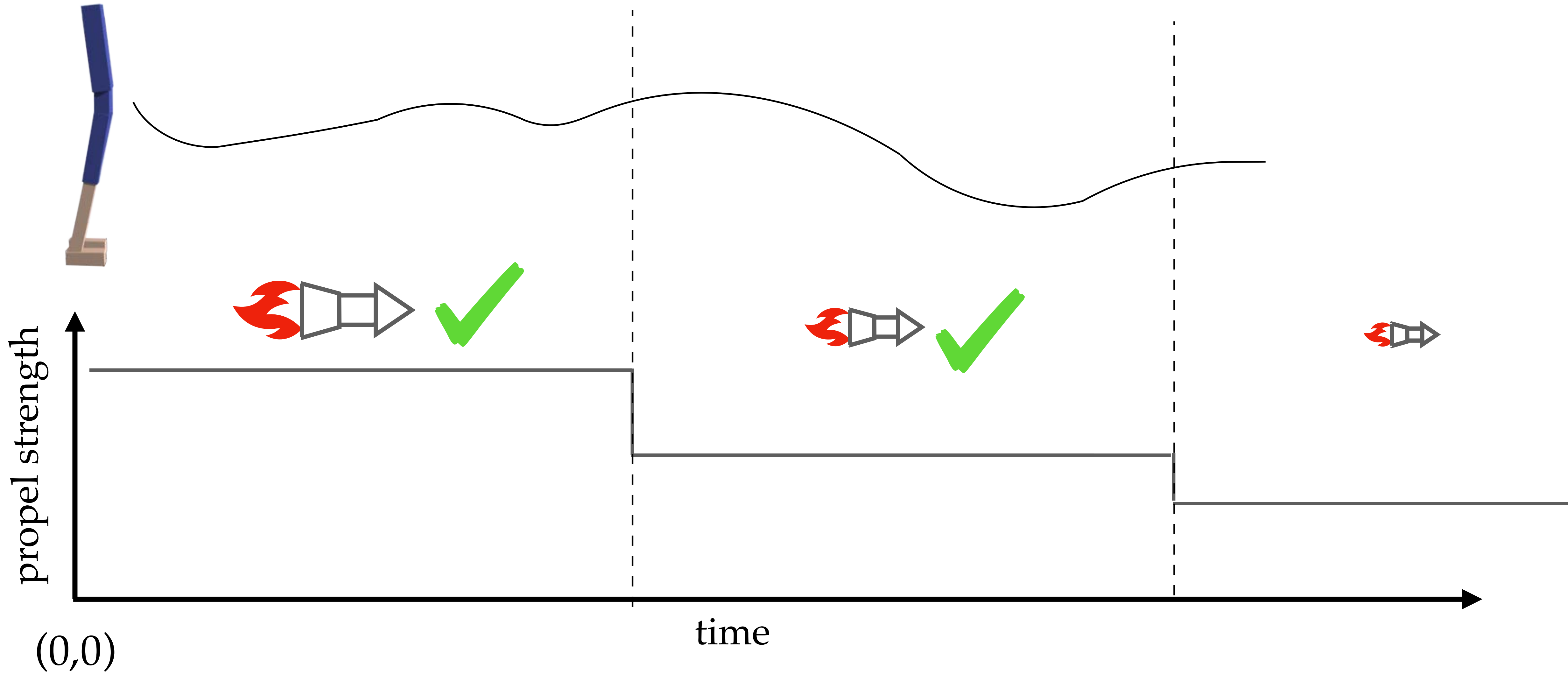
# Iteration i



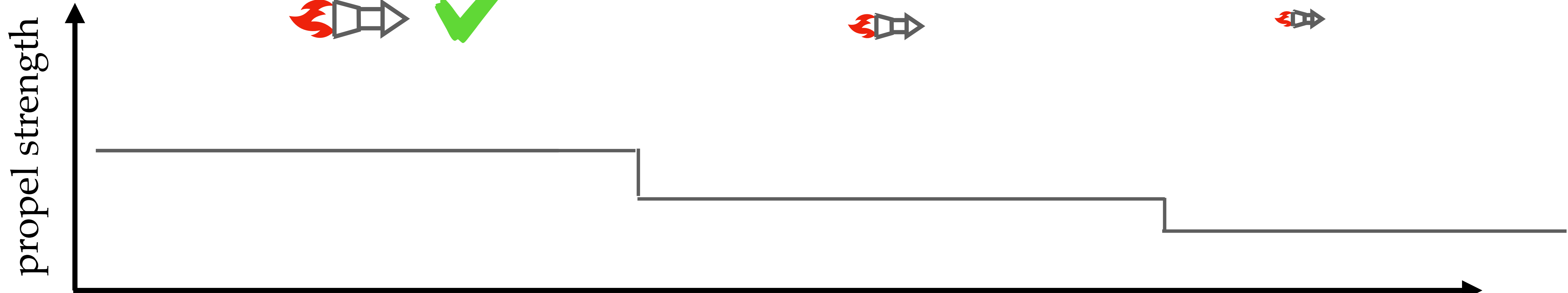
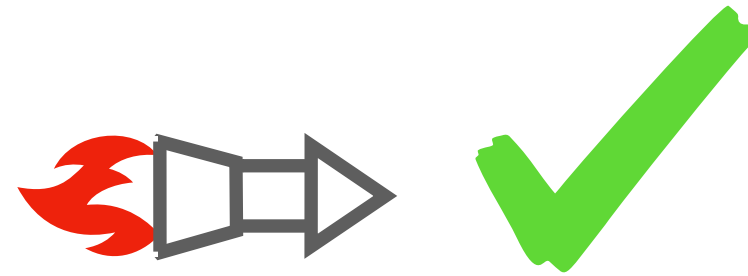
# Iteration i



# Iteration i

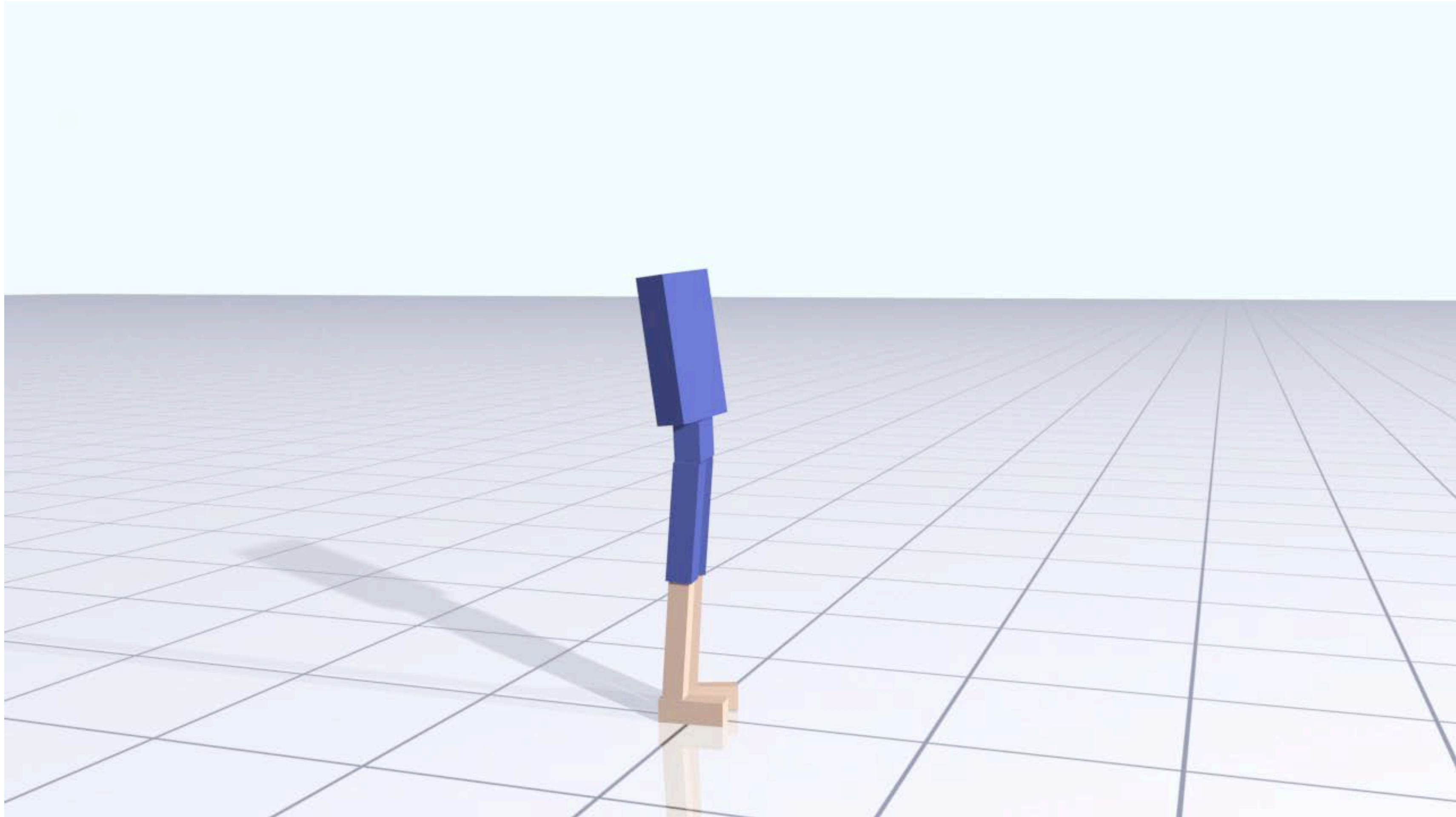


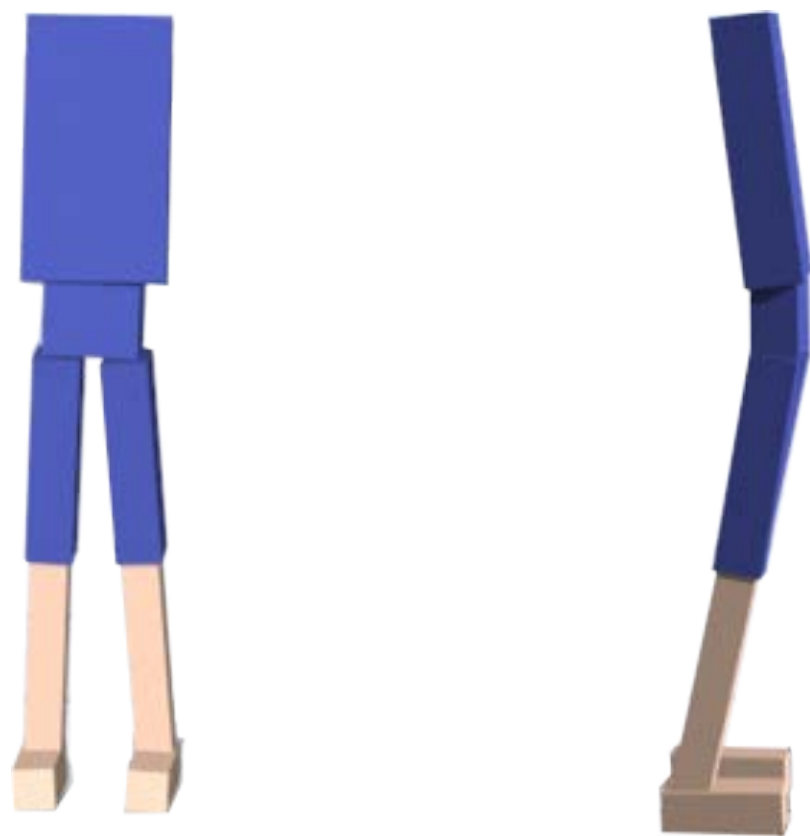
# Iteration i+1



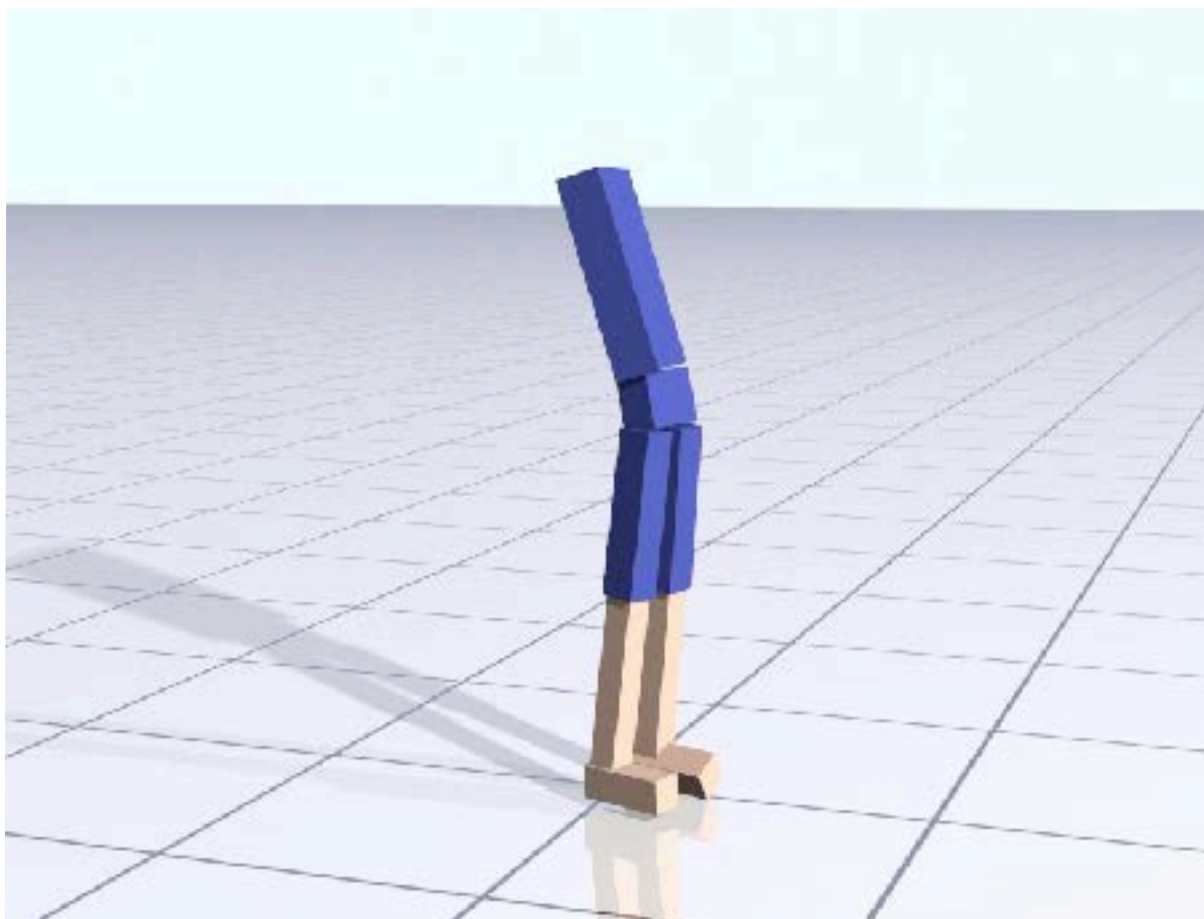
(0,0)

time





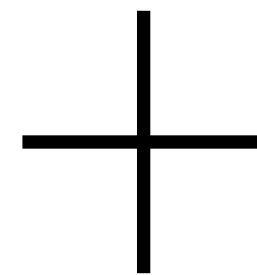
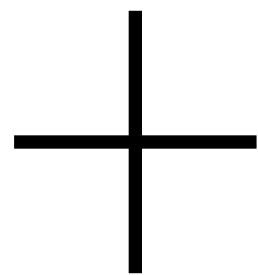
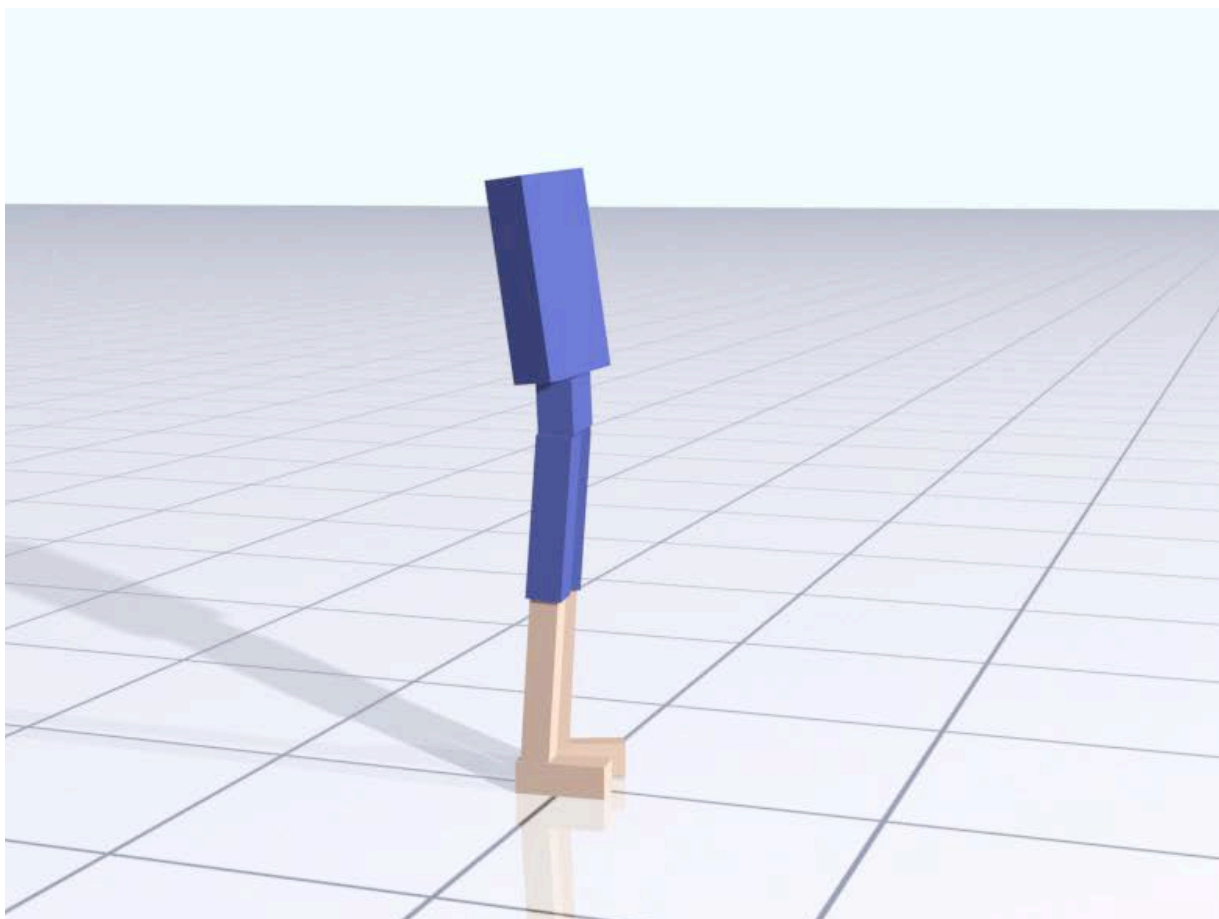
Deep Reinforcement Learning



Curriculum Learning



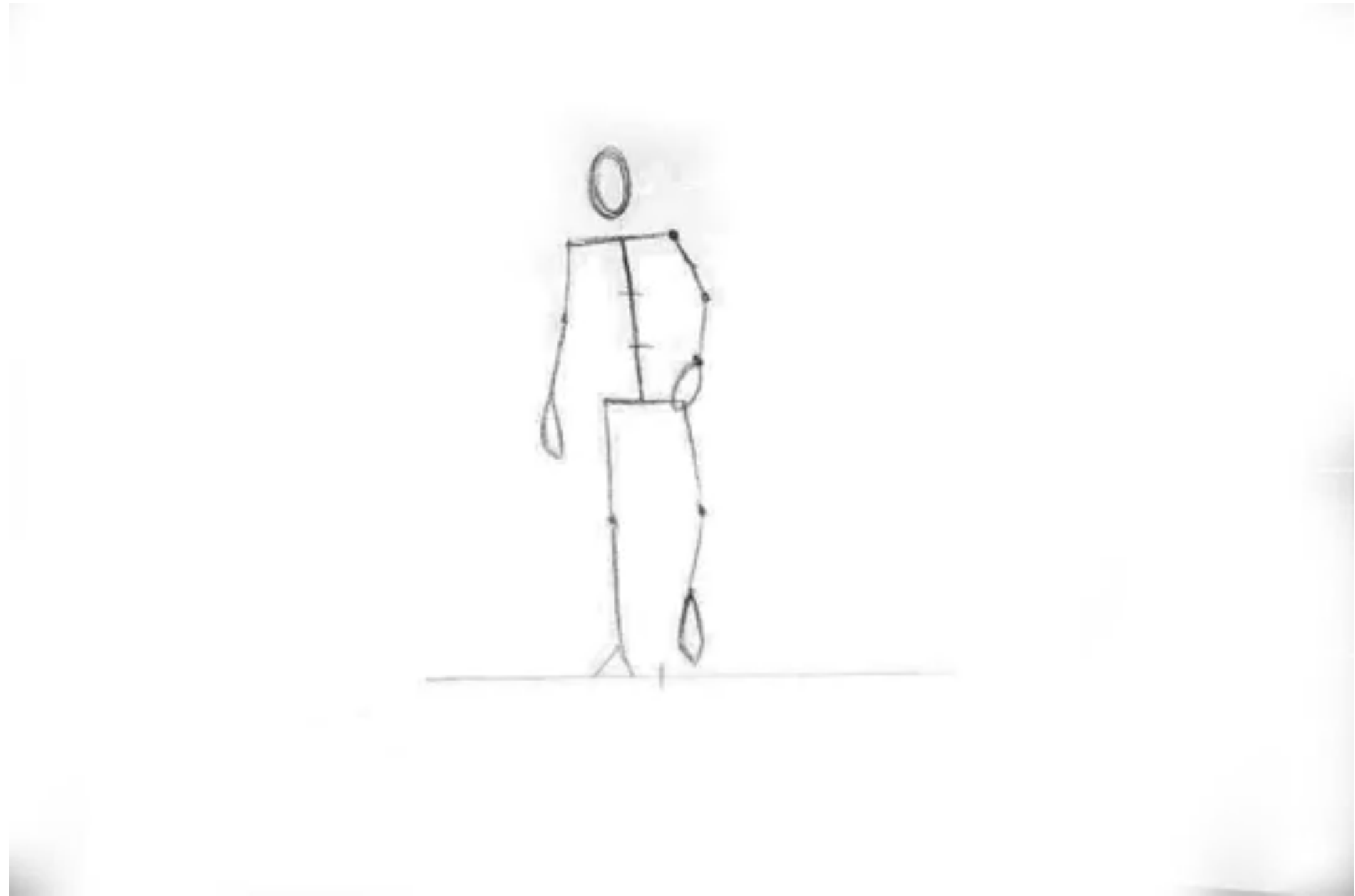
Energy Minimization



Gait Symmetry



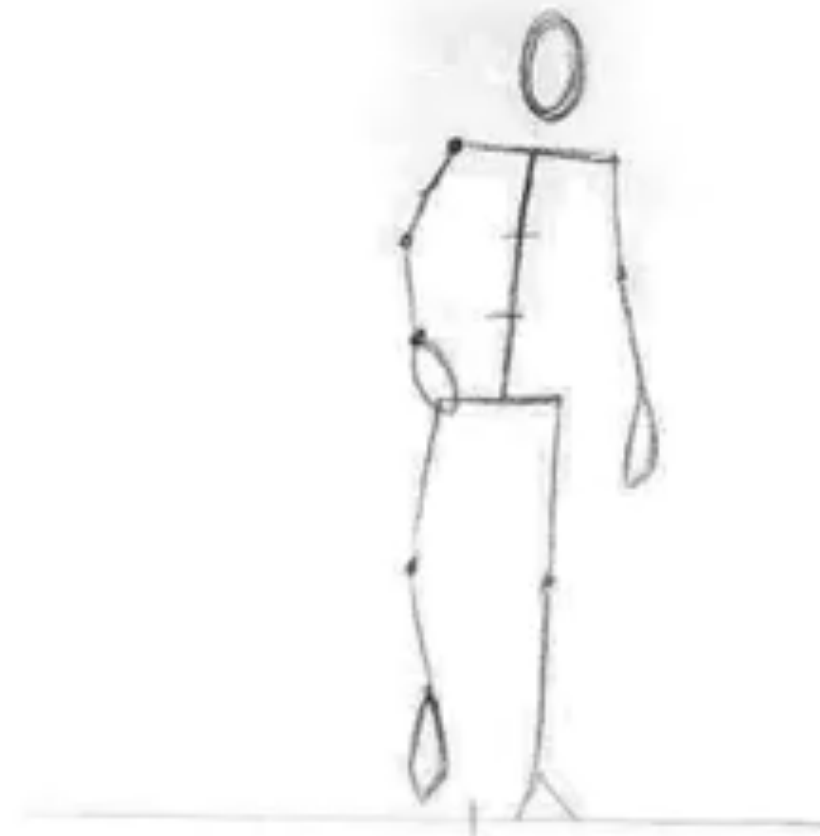
?

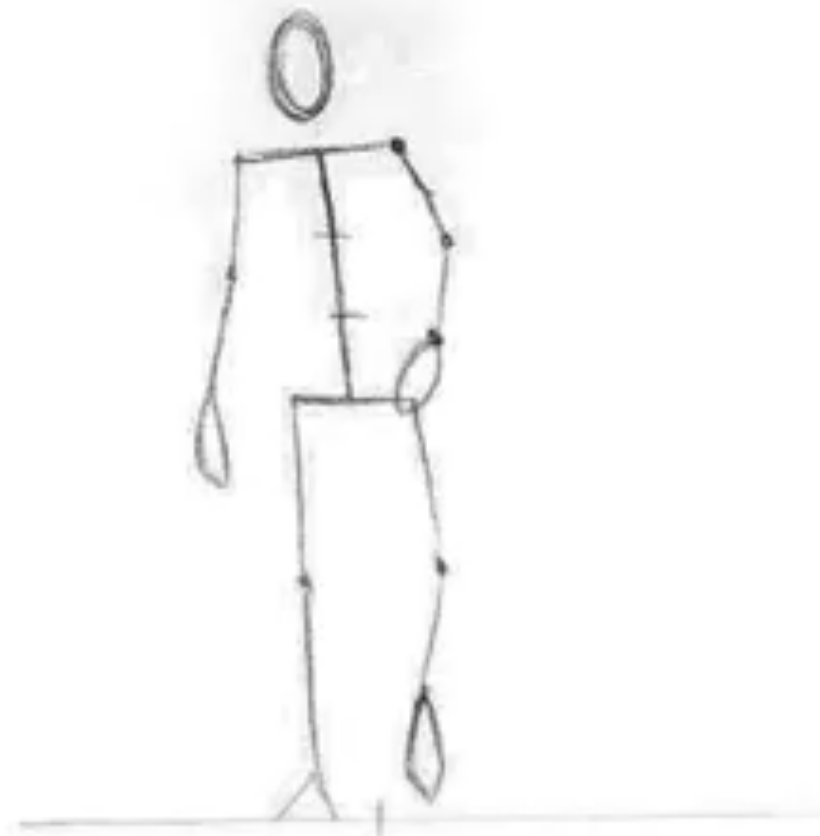




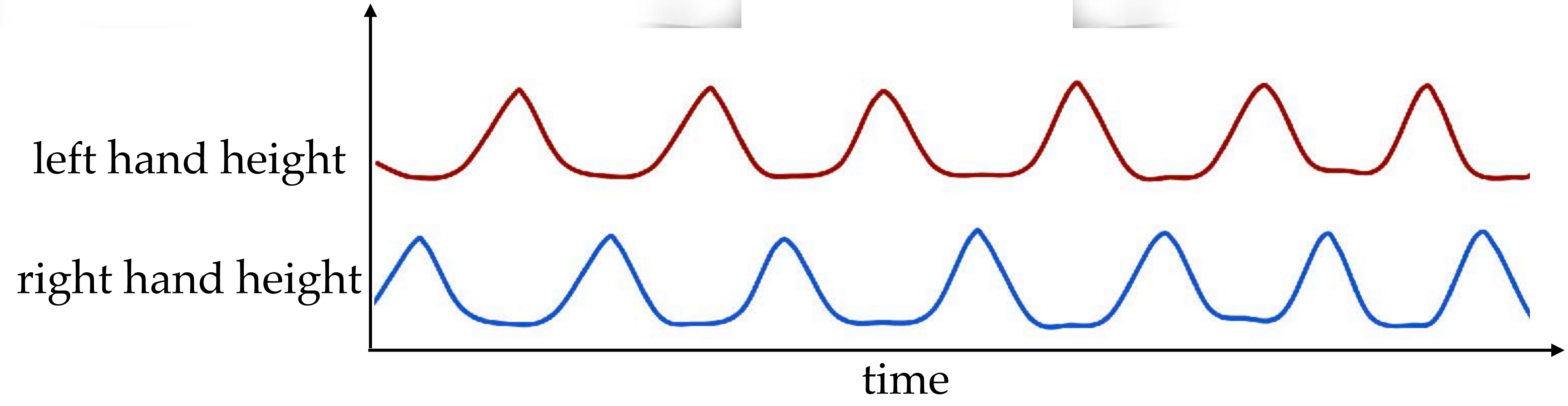
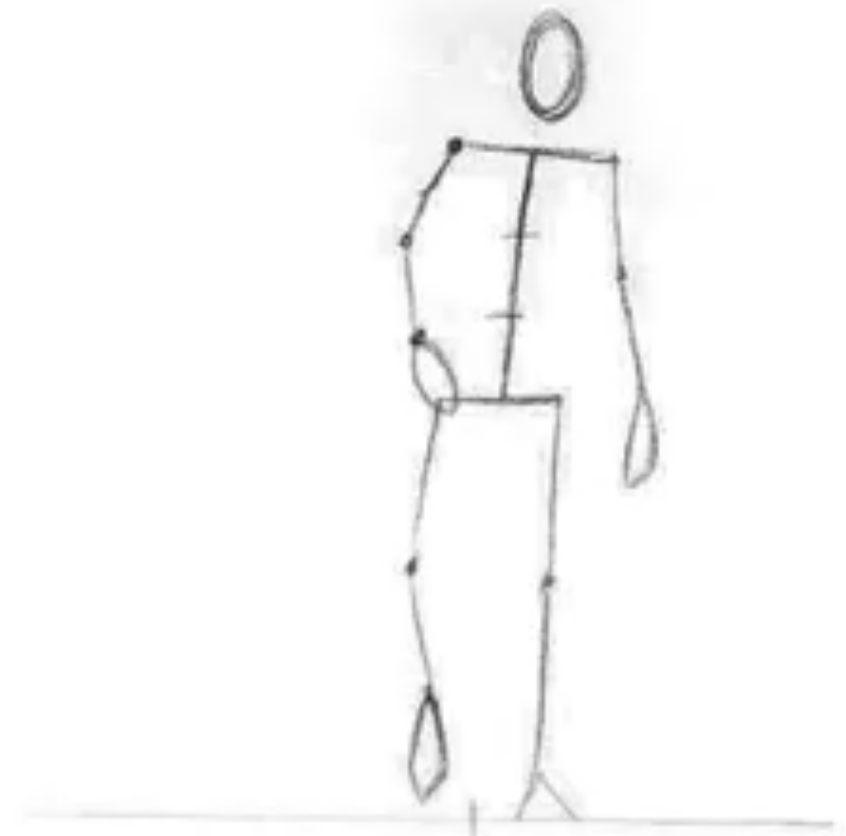


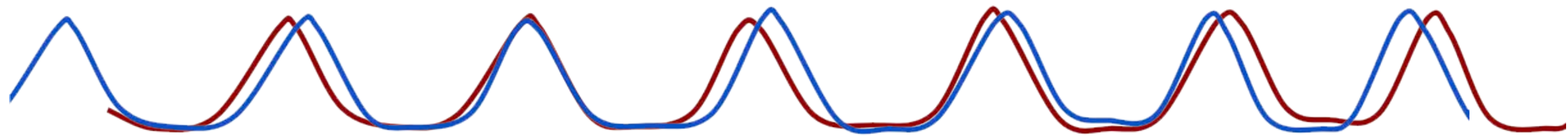
Flip  
→

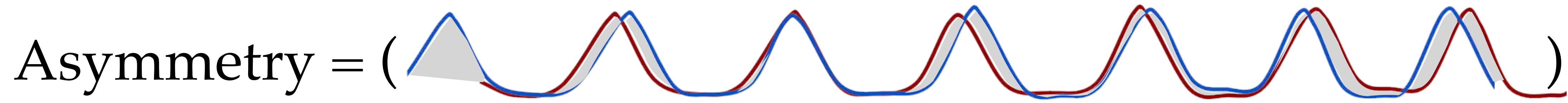


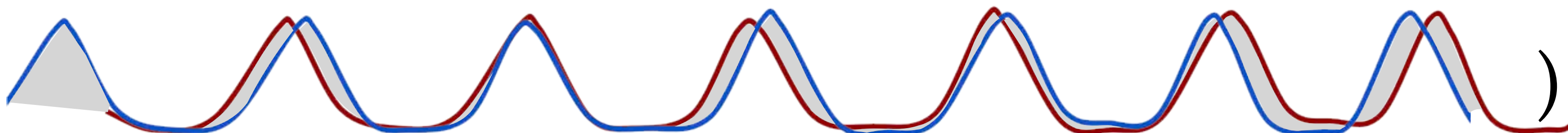


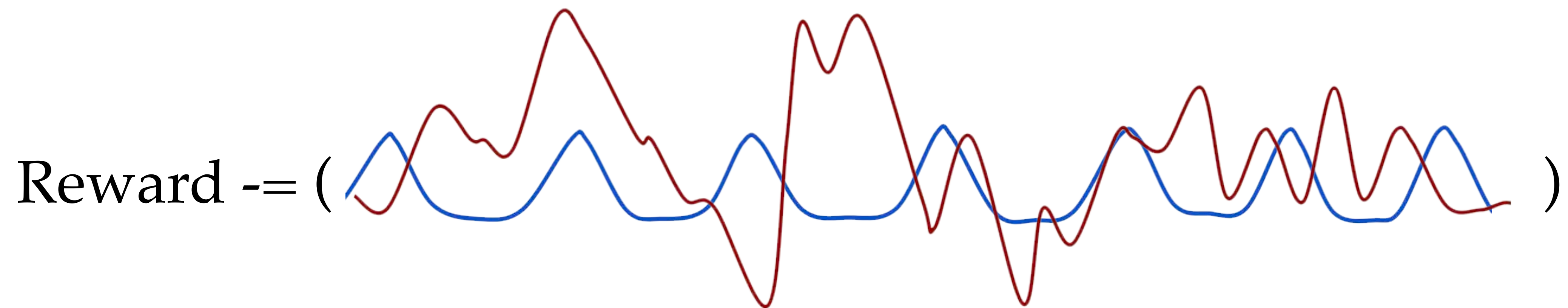
Flip  
→







Reward  $\hat{=}$  (  )

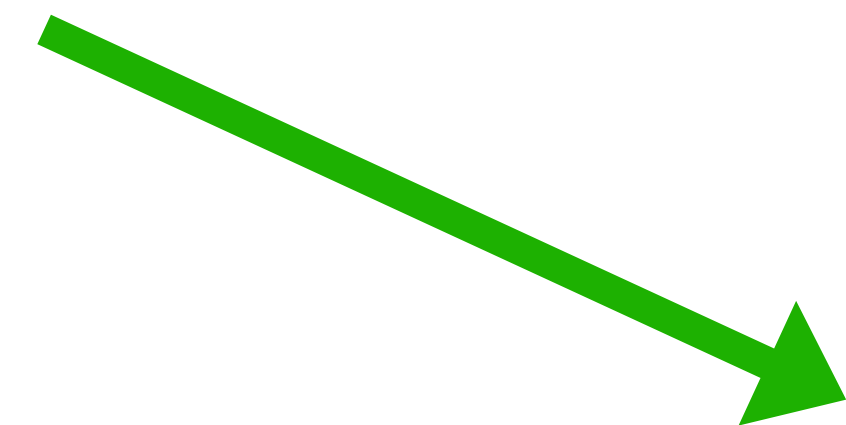
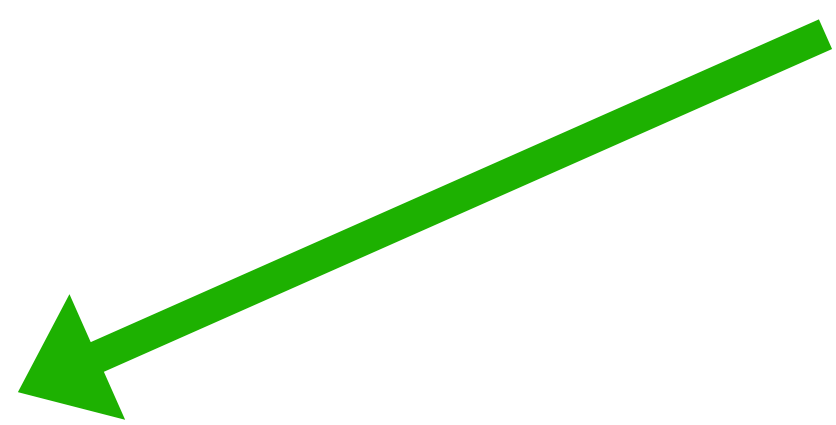
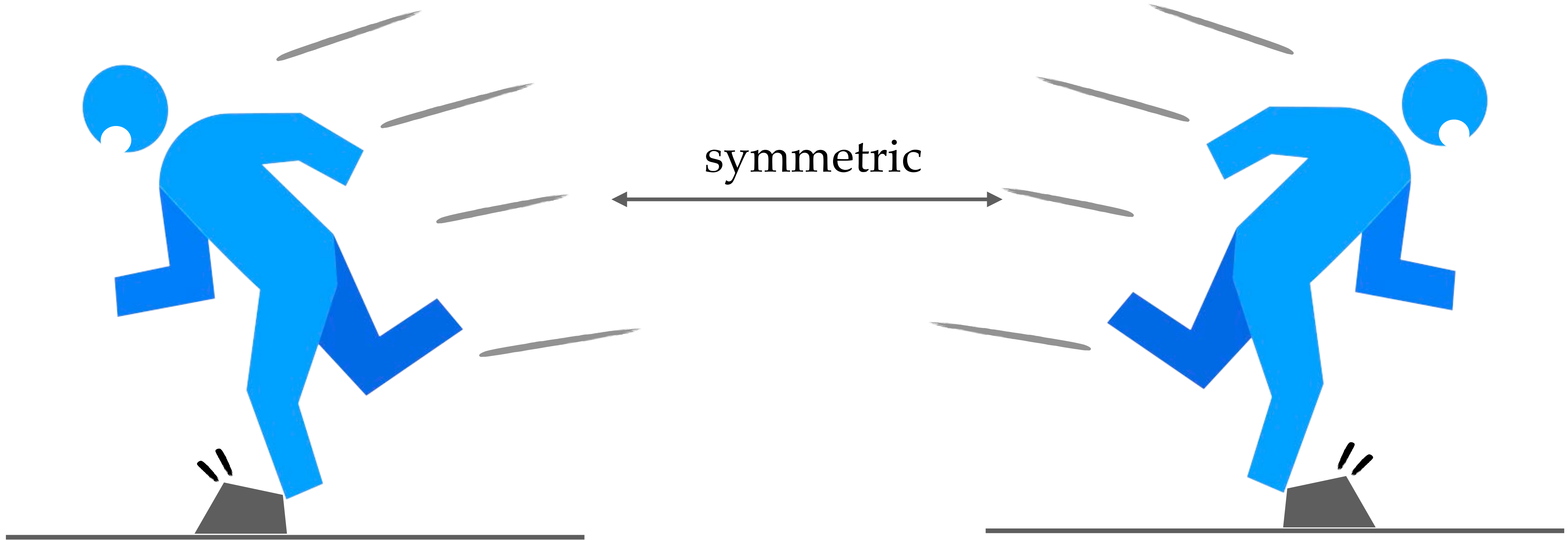


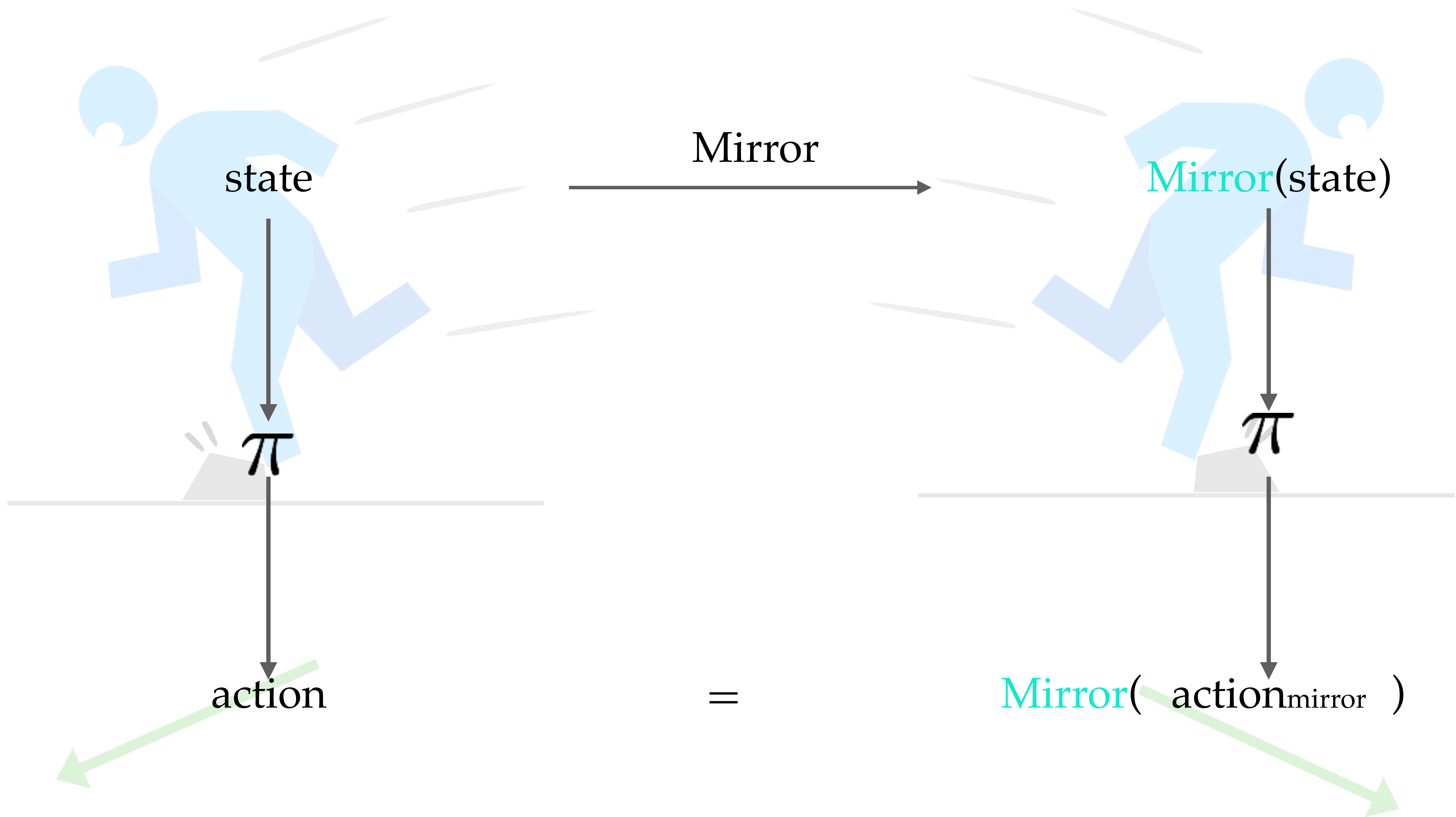












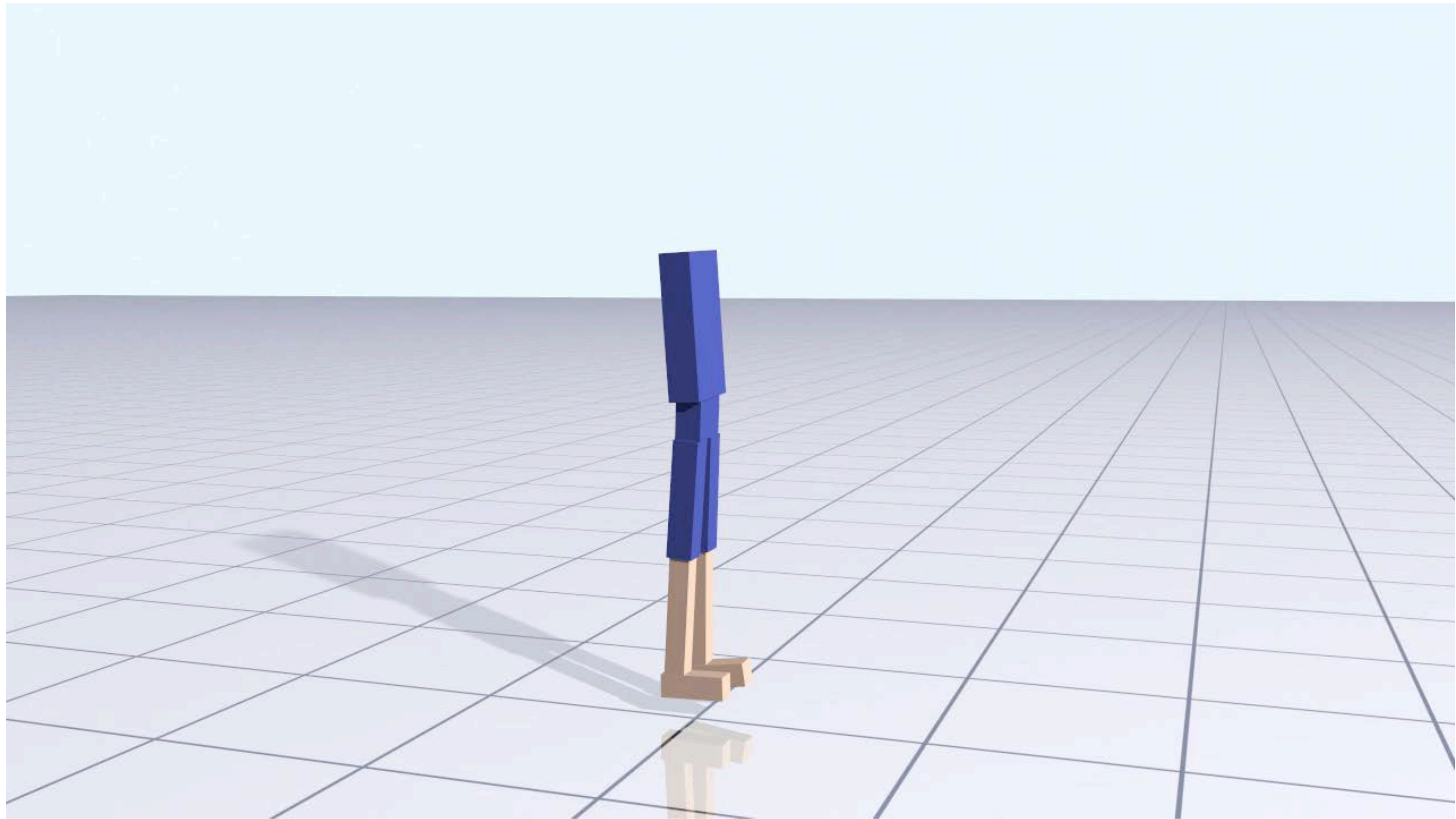
minimize:  $L_{RL}$   
 $\pi$

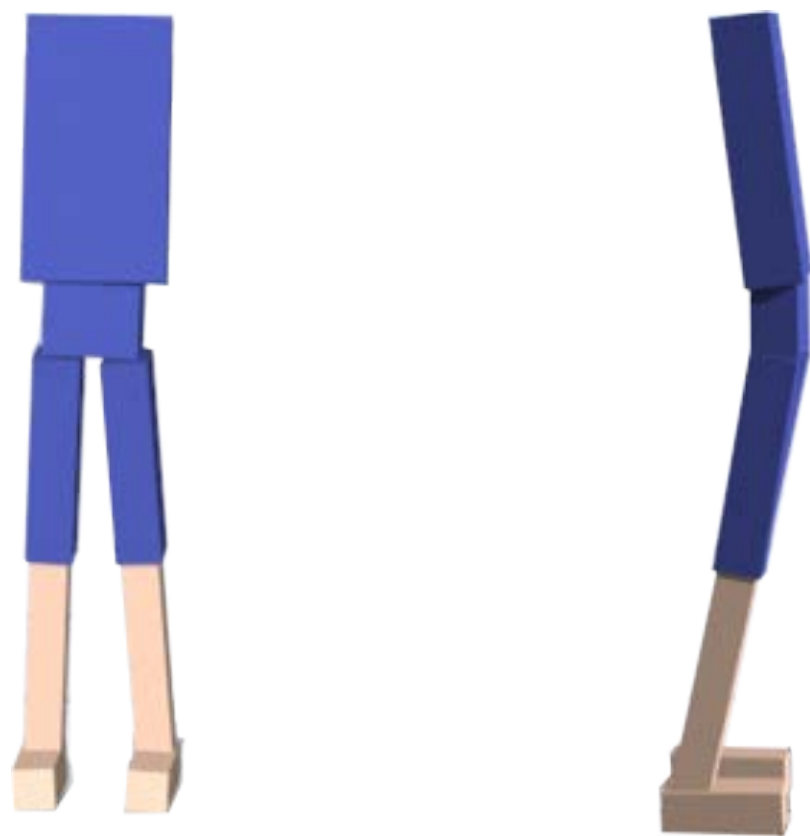
subject to:  $\text{action} = \text{Mirror}(\text{action}_{\text{mirror}})$

\*weights omitted for clarity

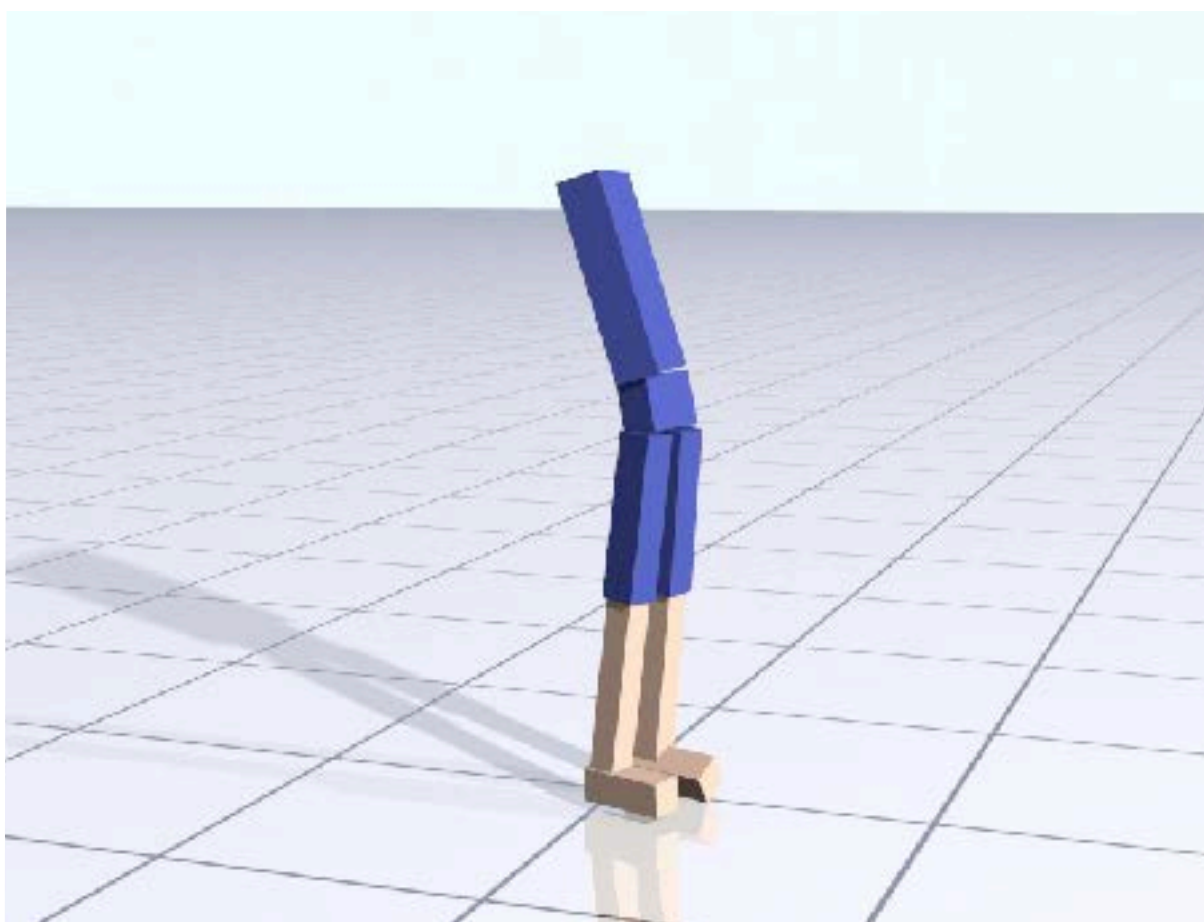
$$\underset{\pi}{\text{minimize:}} \quad \mathbf{L}_{\text{RL}} + \left\| \text{action} - \text{Mirror}(\text{action}_{\text{mirror}}) \right\|_2^2$$

\*weights omitted for clarity





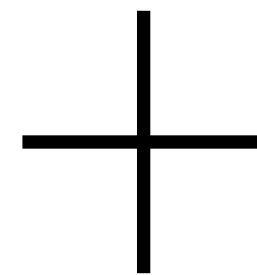
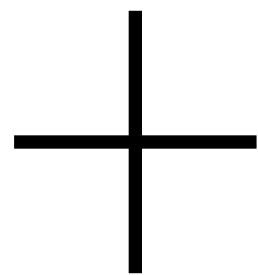
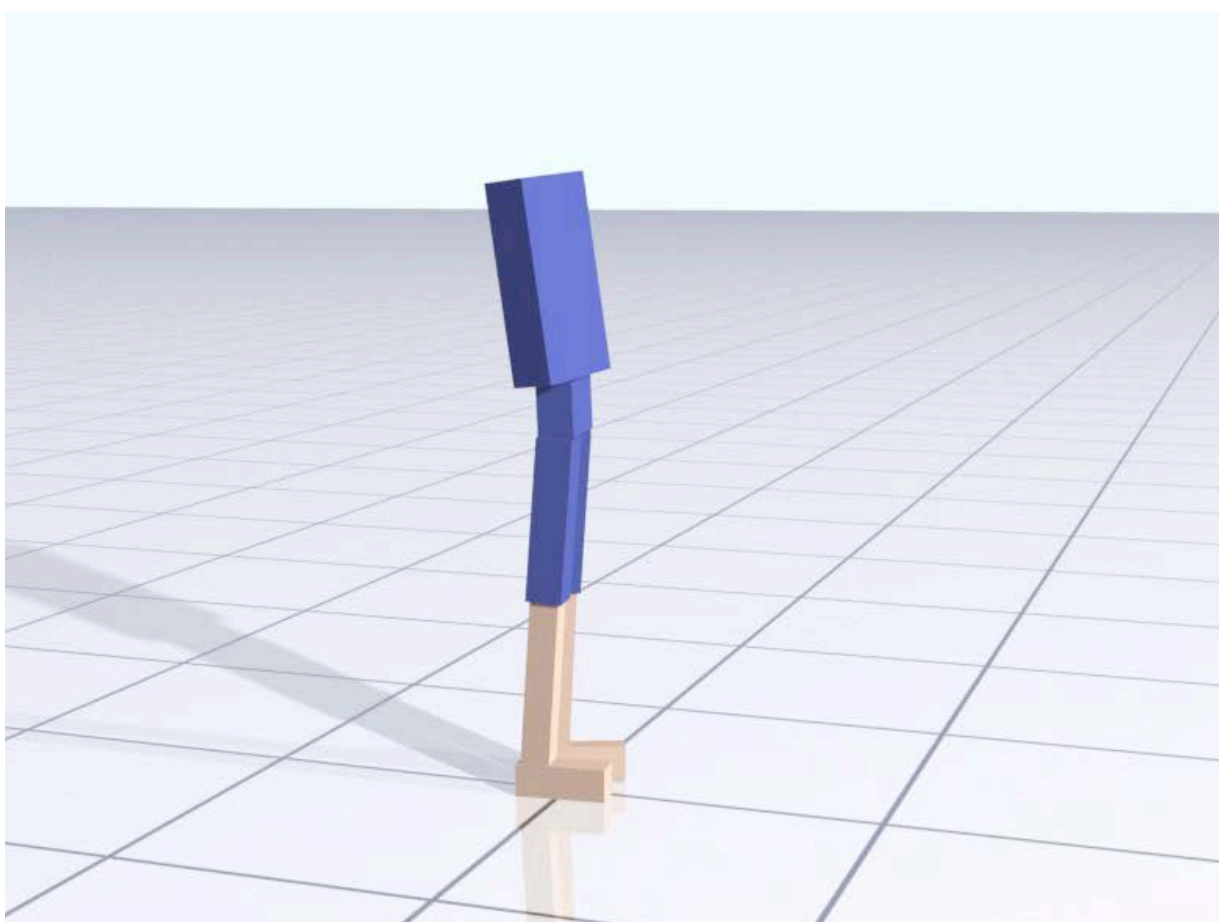
Deep Reinforcement Learning



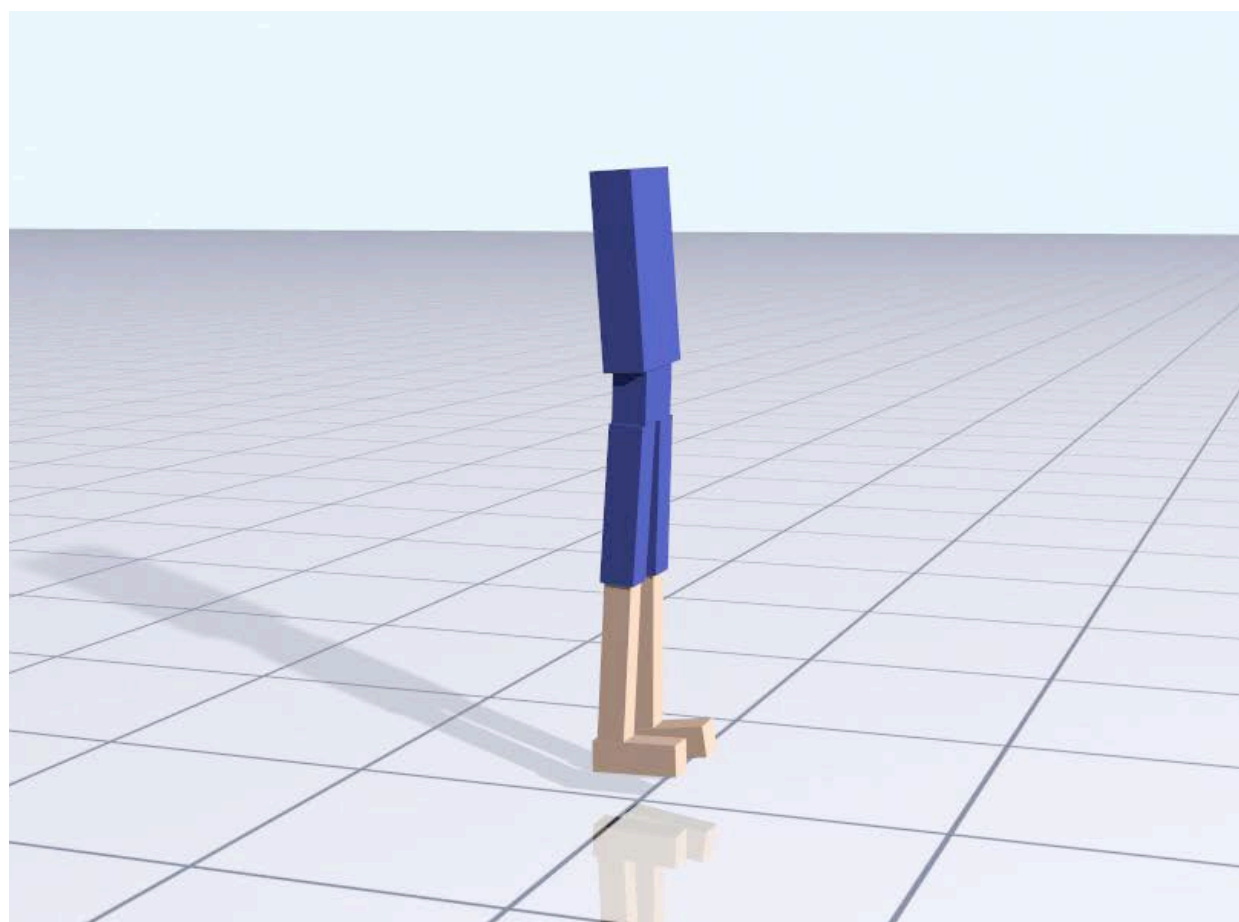
Curriculum Learning



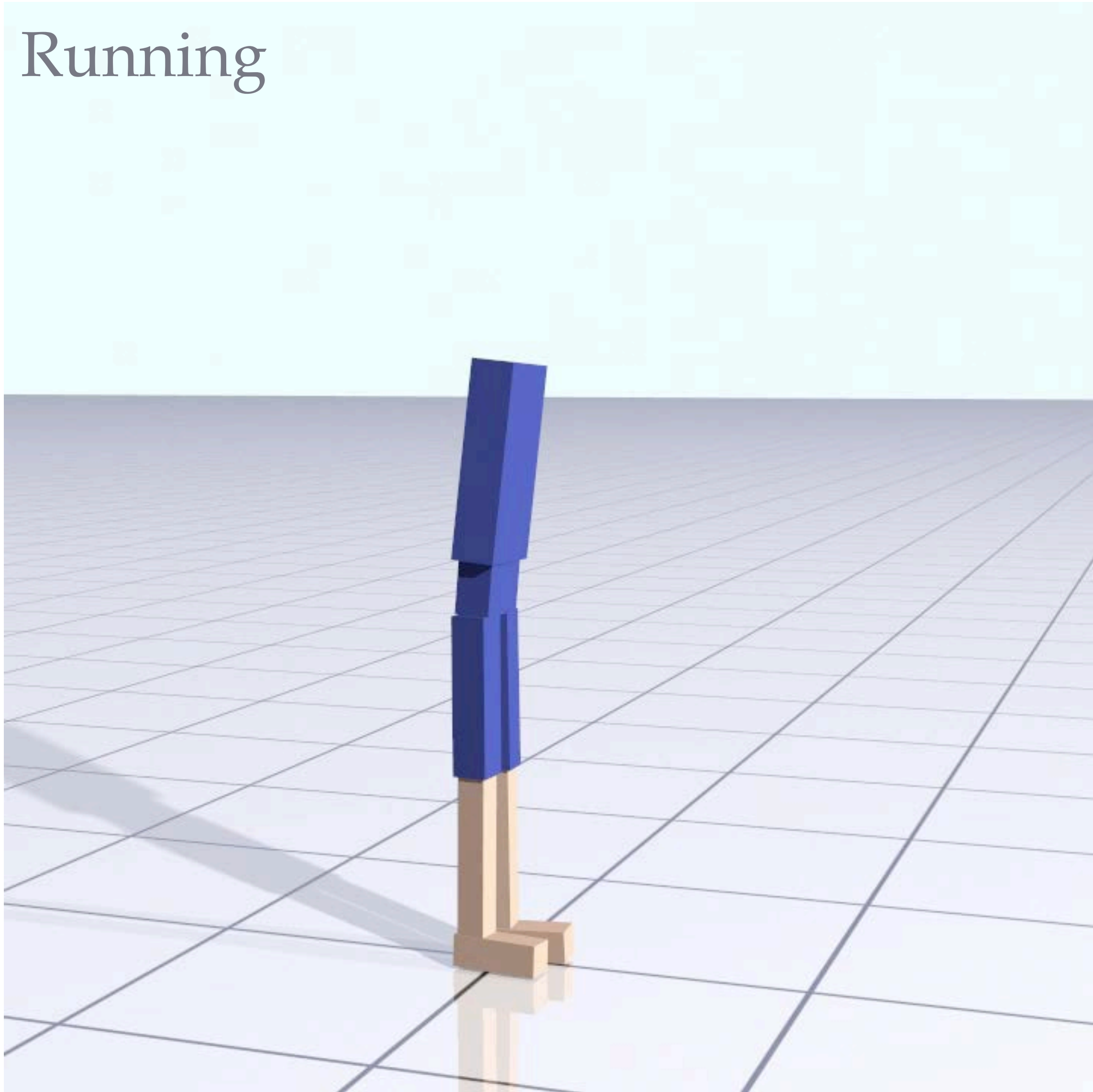
Energy Minimization



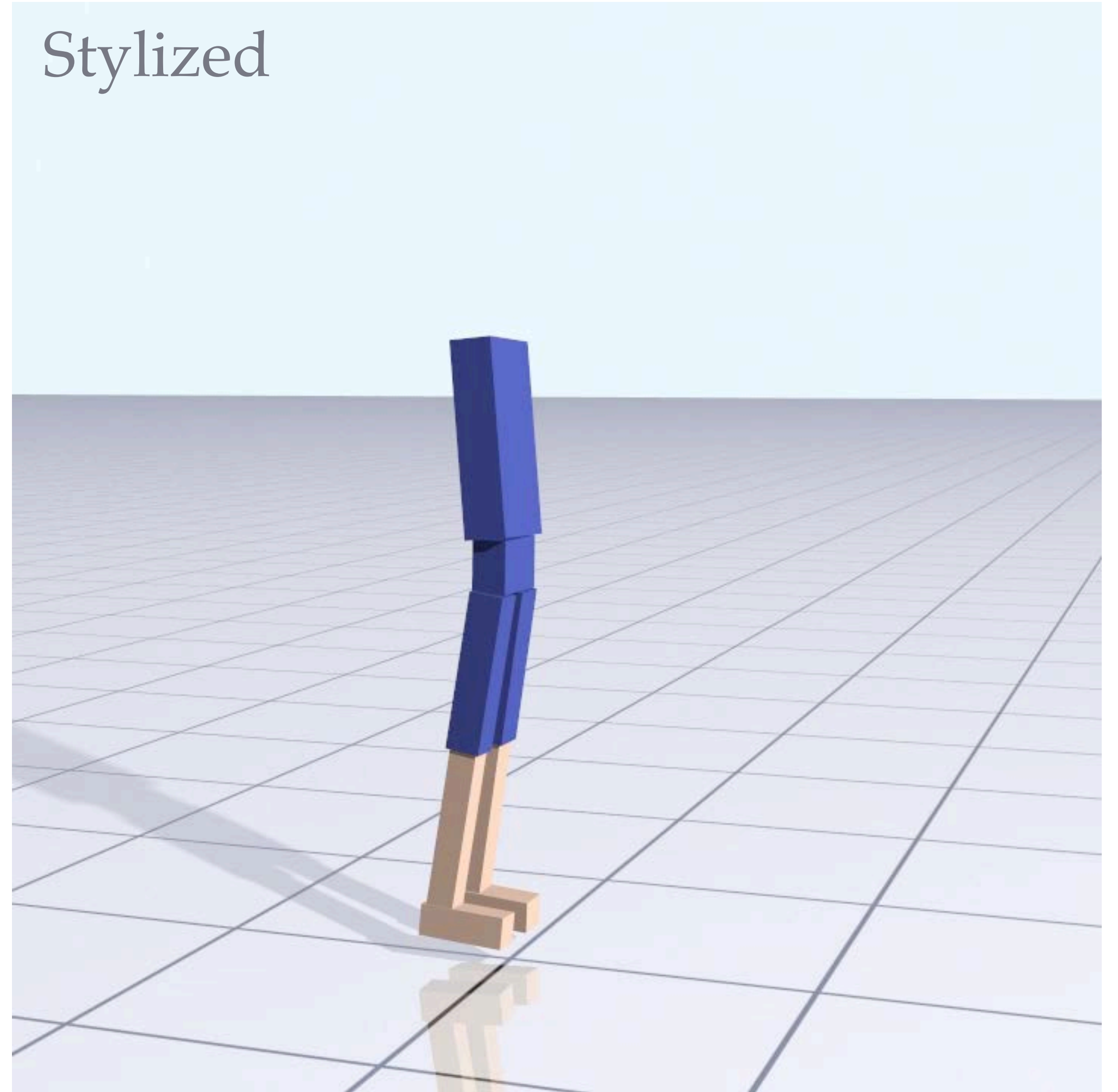
Gait Symmetry



Running

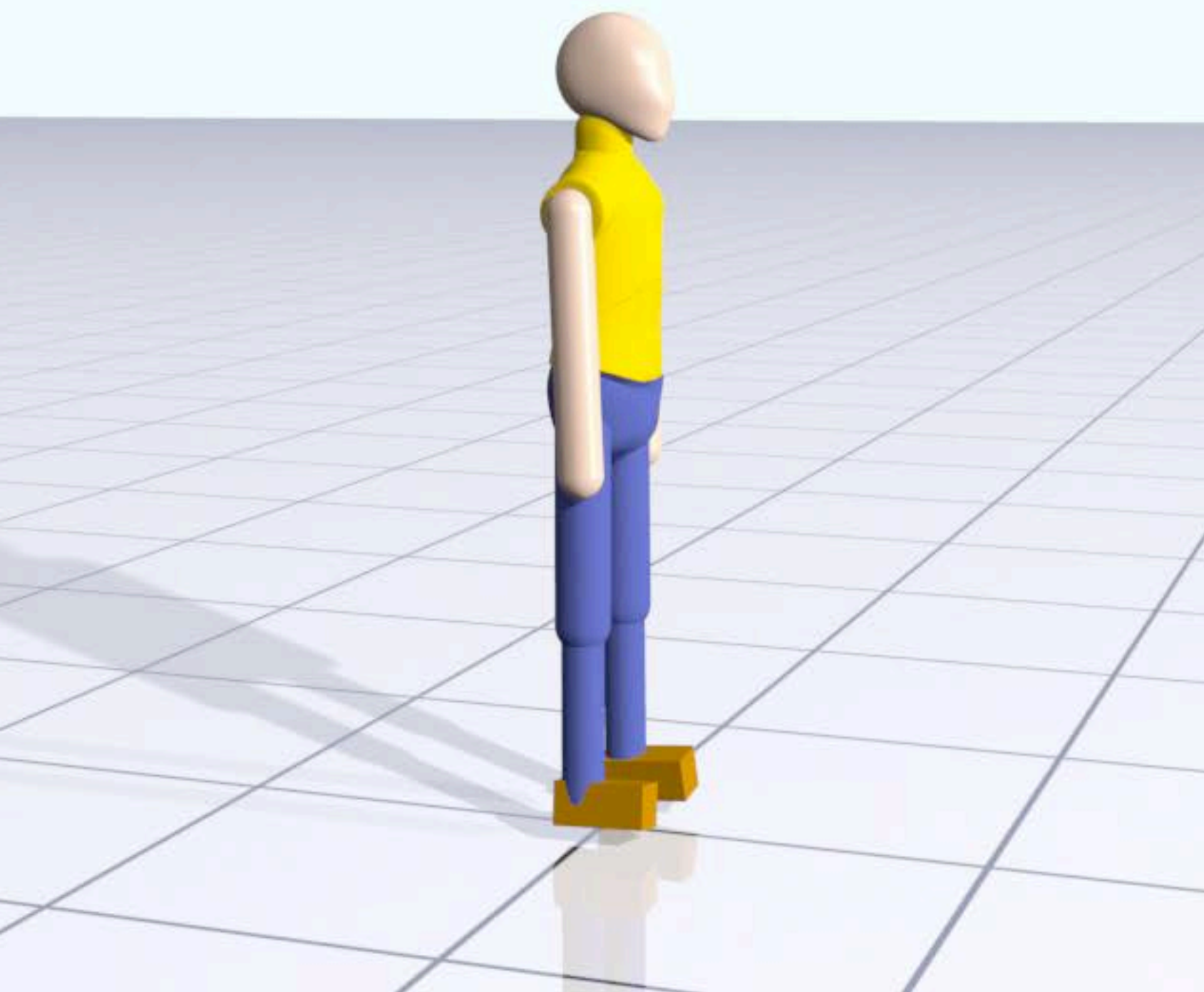


Stylized

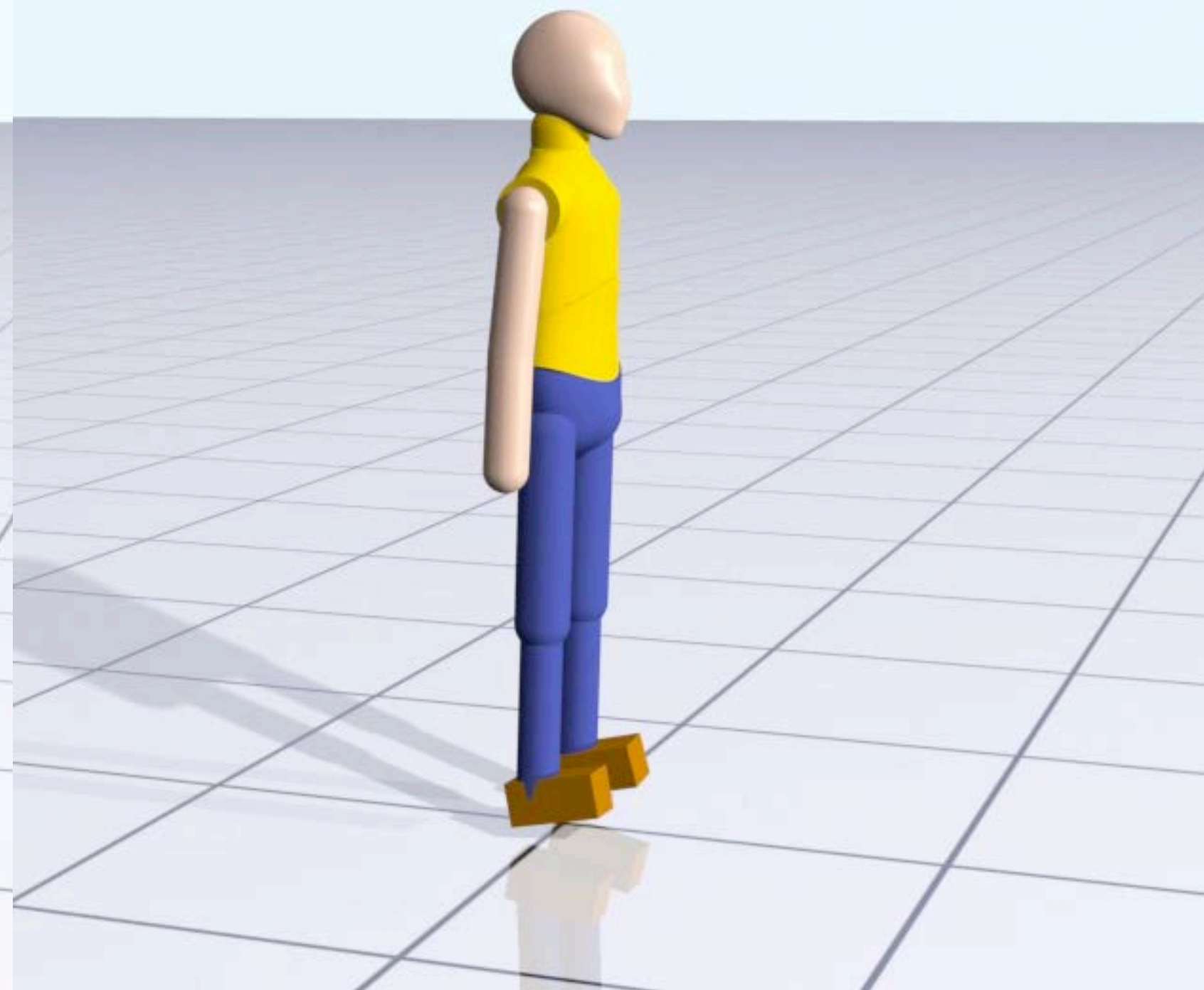




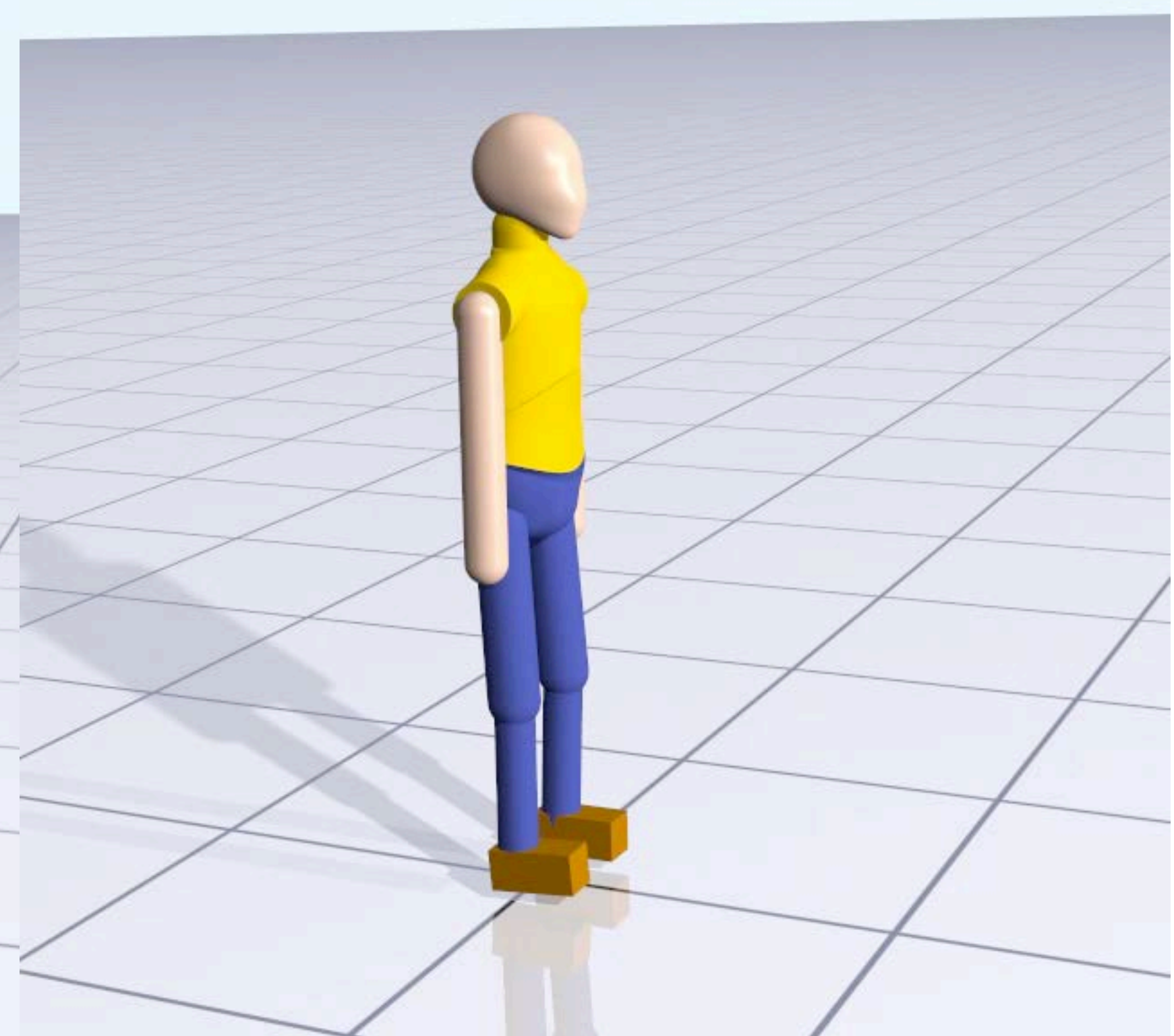
Walking



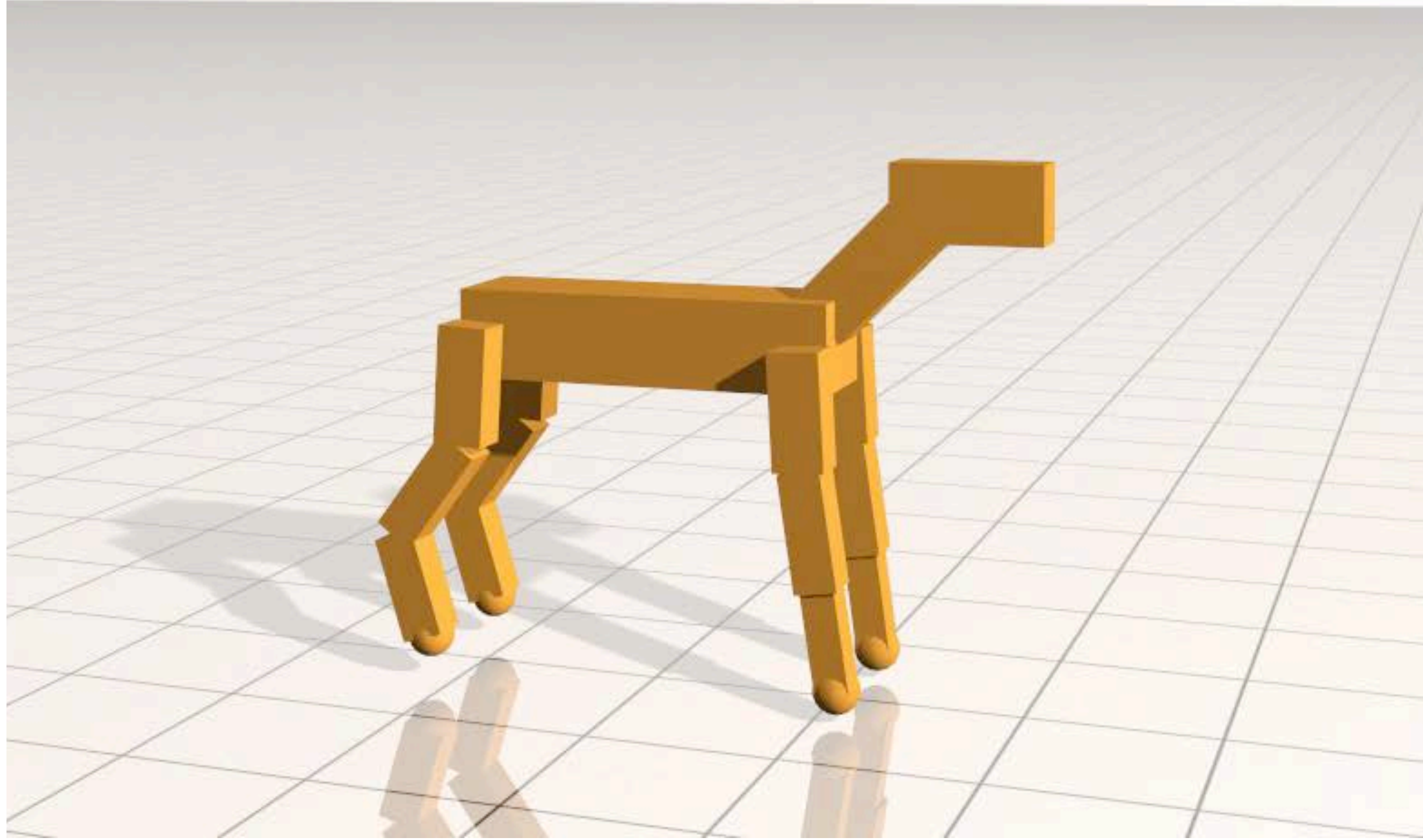
Running



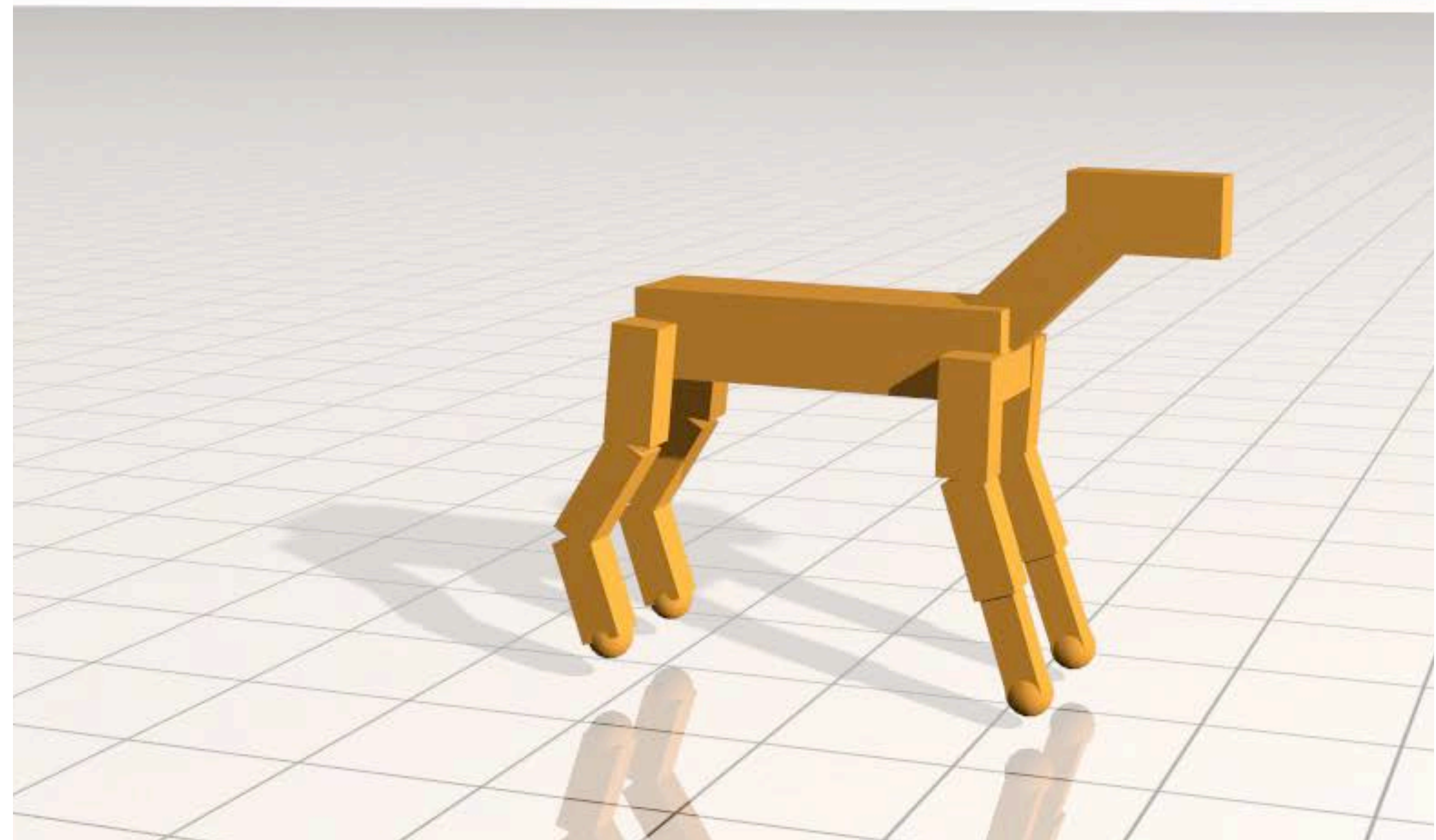
Walking back



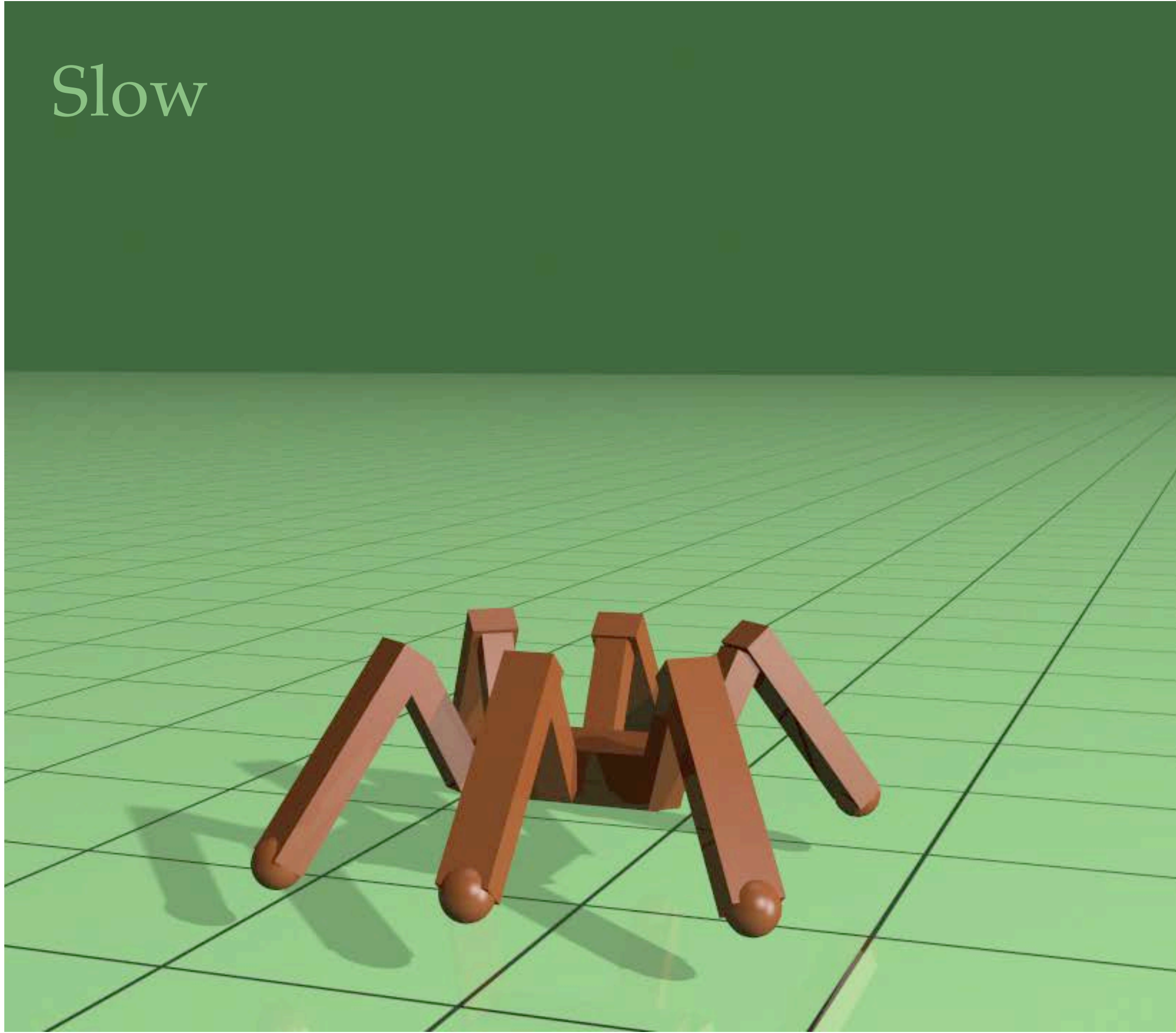
Trotting



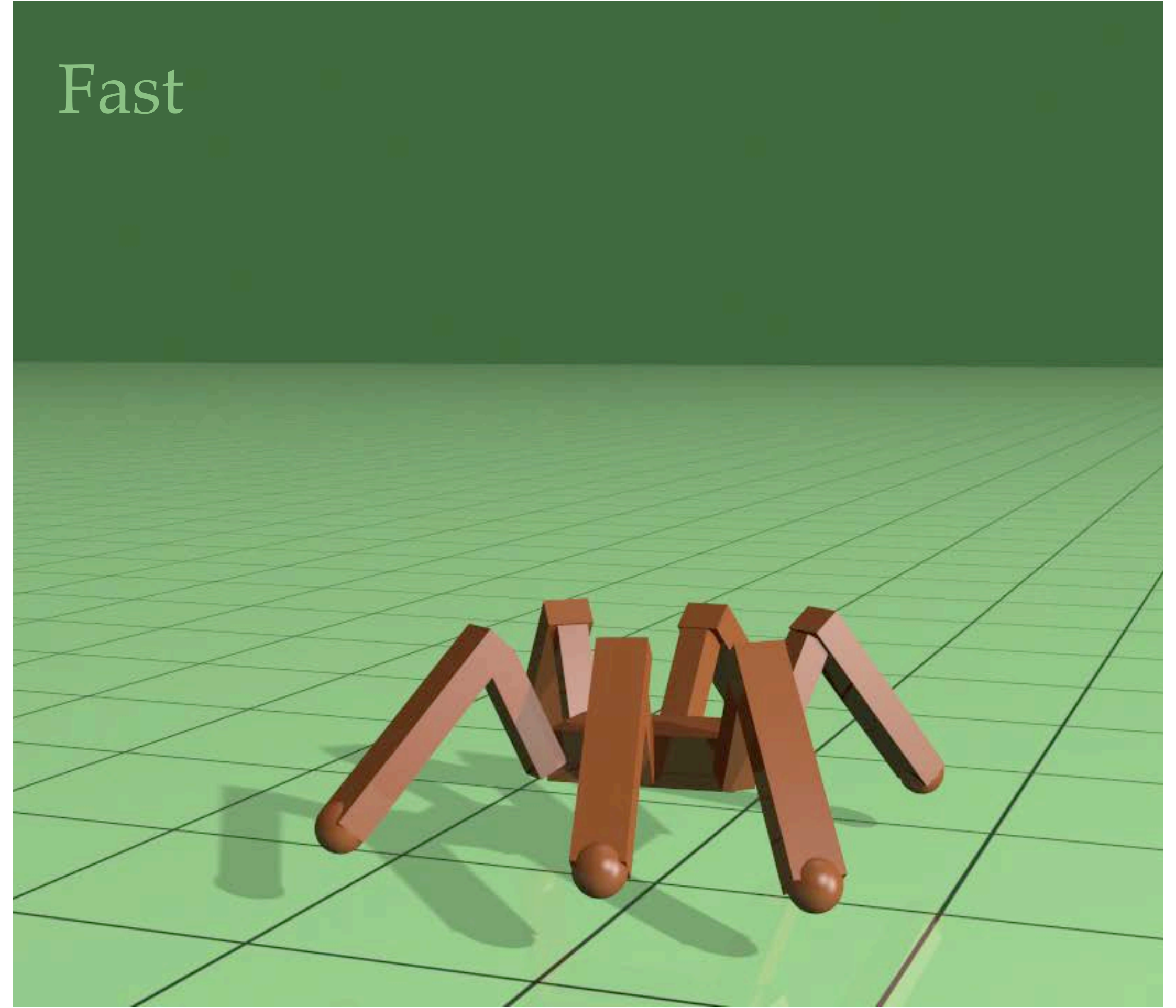
Galloping



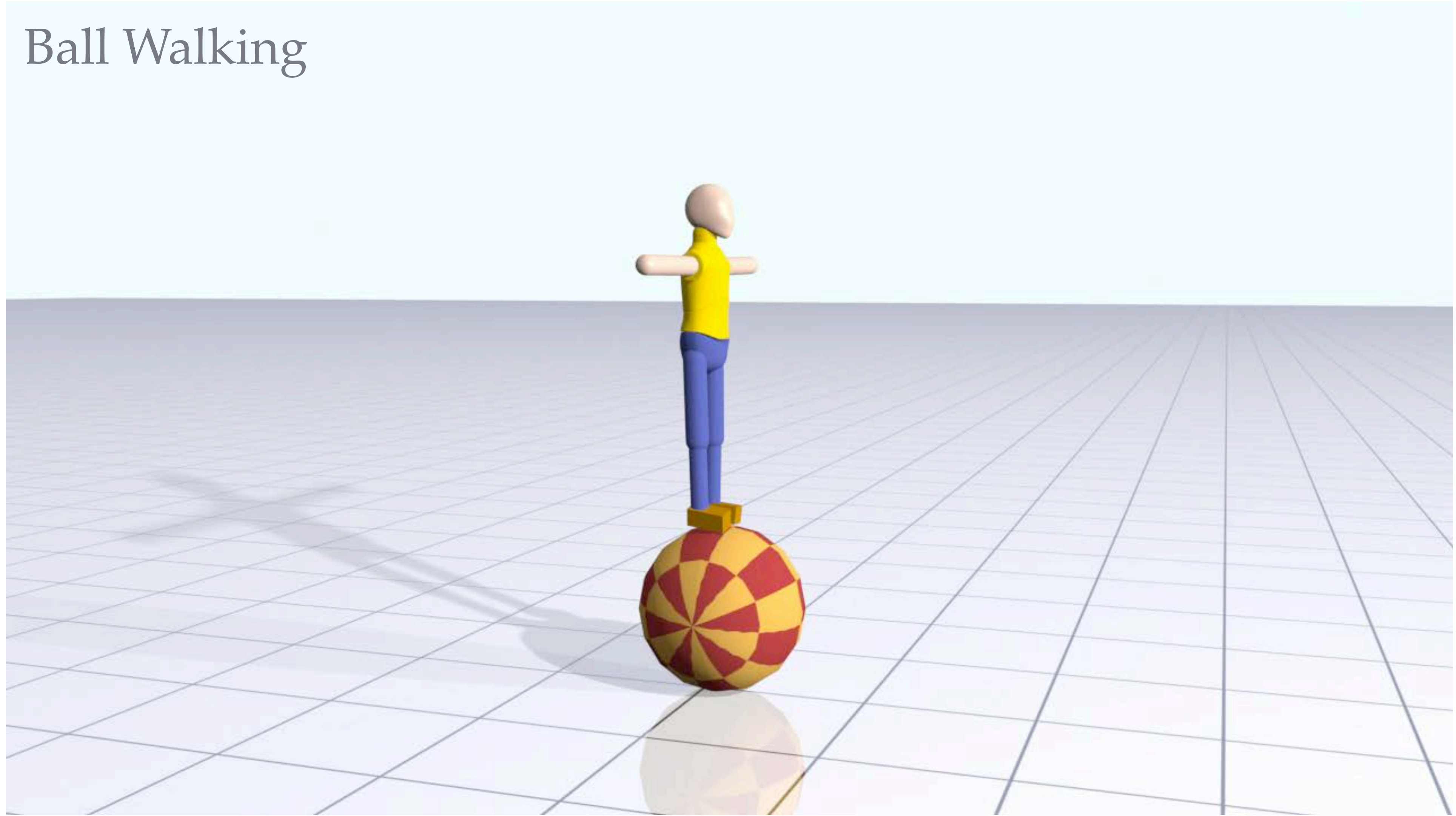
Slow



Fast

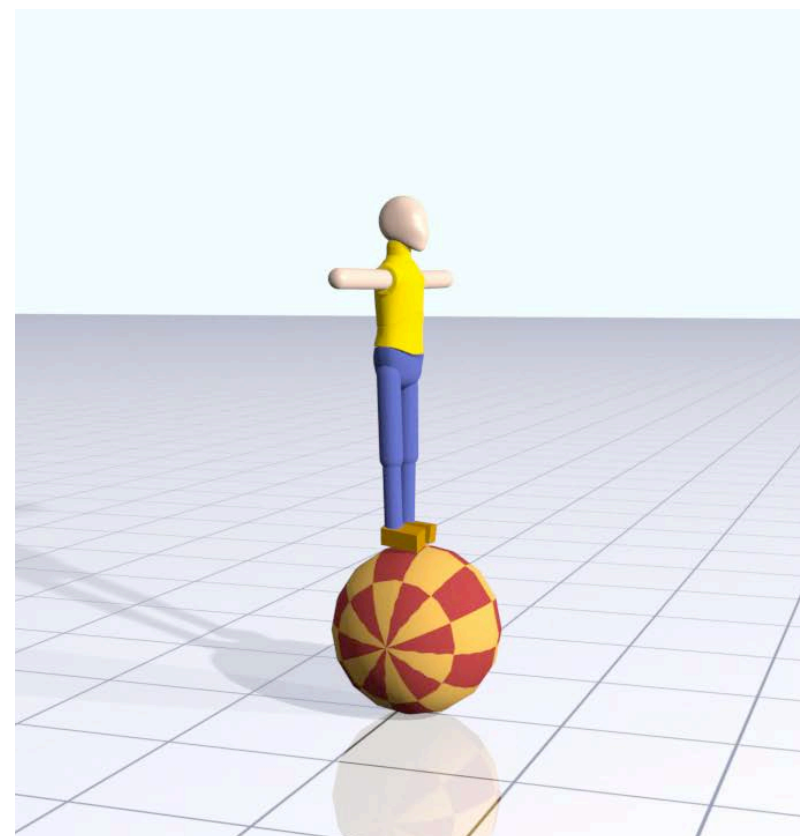
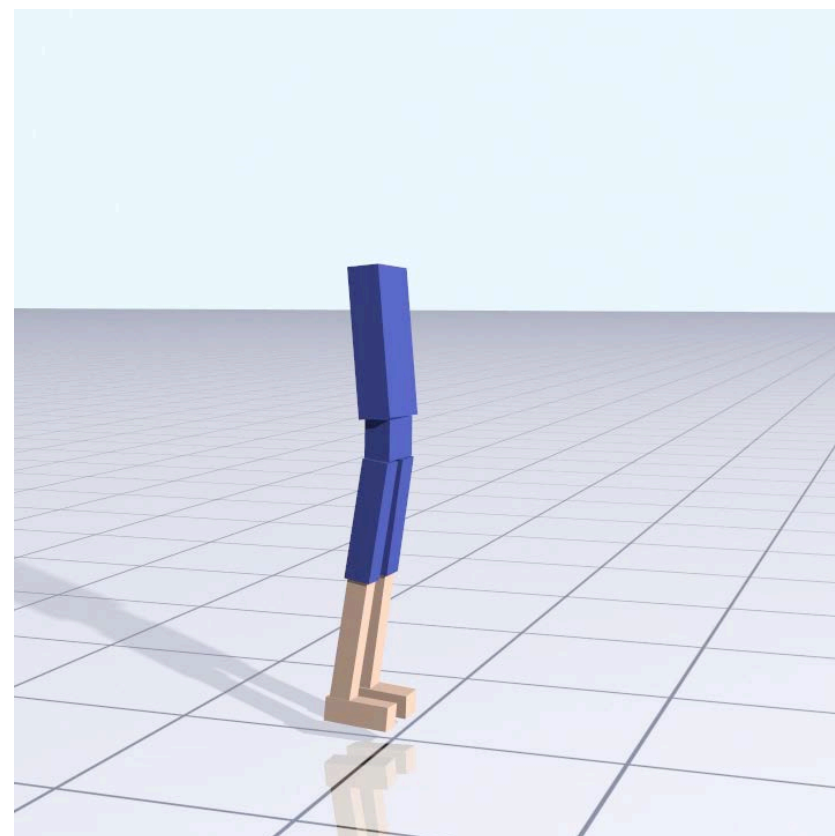


# Ball Walking



# What's Next?

- Biomechanics-based models
- Extend to more agile motions such as gymnastics
- Running on real-hardware



# Thank you!

- paper link: <https://arxiv.org/abs/1801.08093>
- code link: <https://github.com/VincentYu68/SymmetryCurriculumLocomotion>
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- email: [wenhaoyu@gatech.edu](mailto:wenhaoyu@gatech.edu)