



GENERATIONS / VANCOUVER
12-16 AUGUST
SIGGRAPH2018



Stitch Meshing

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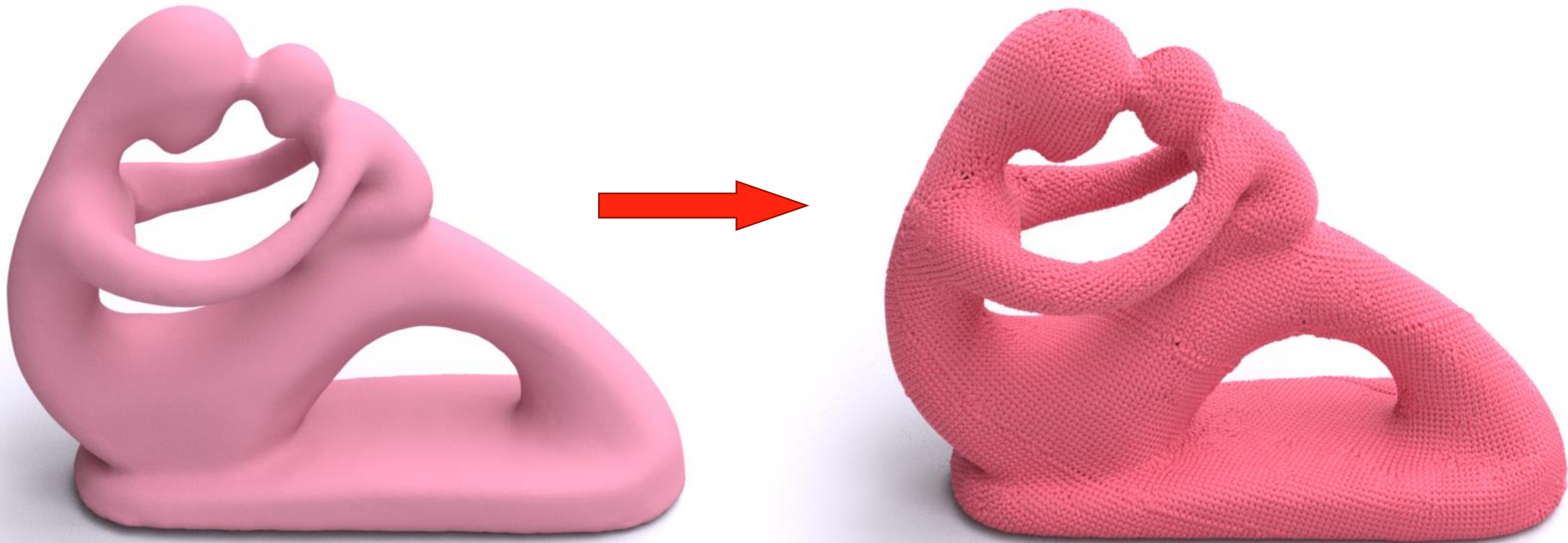
¹ University of Utah

² New York University



Stitch Meshing

Convert arbitrary 3D shapes into knit models **fully automatically**



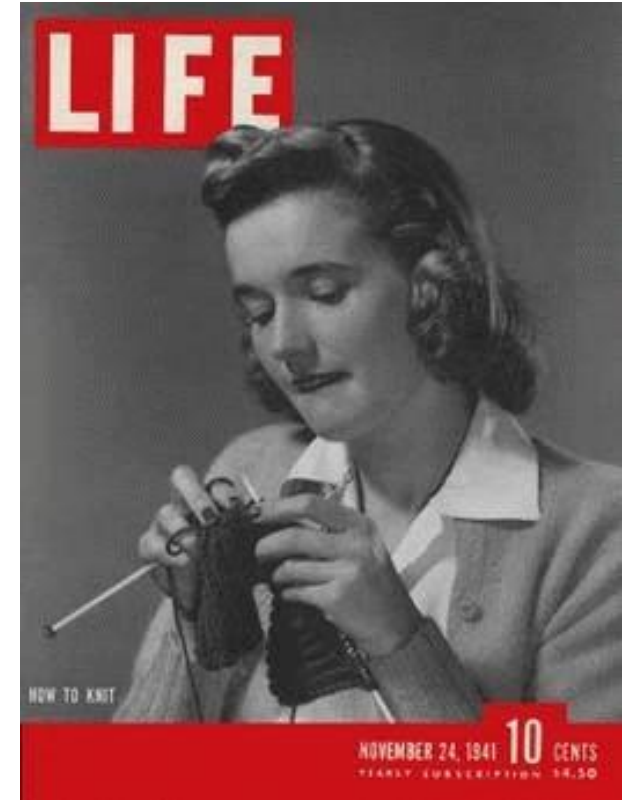
Knitting has a long history



Sock in Ancient Egypt
200 - 400
From: the British Museum



Madonna Knitting
by Bertram of Minden
1400 - 1410



Life magazine's cover story
November 24, 1941

Common Products



Fashion Element

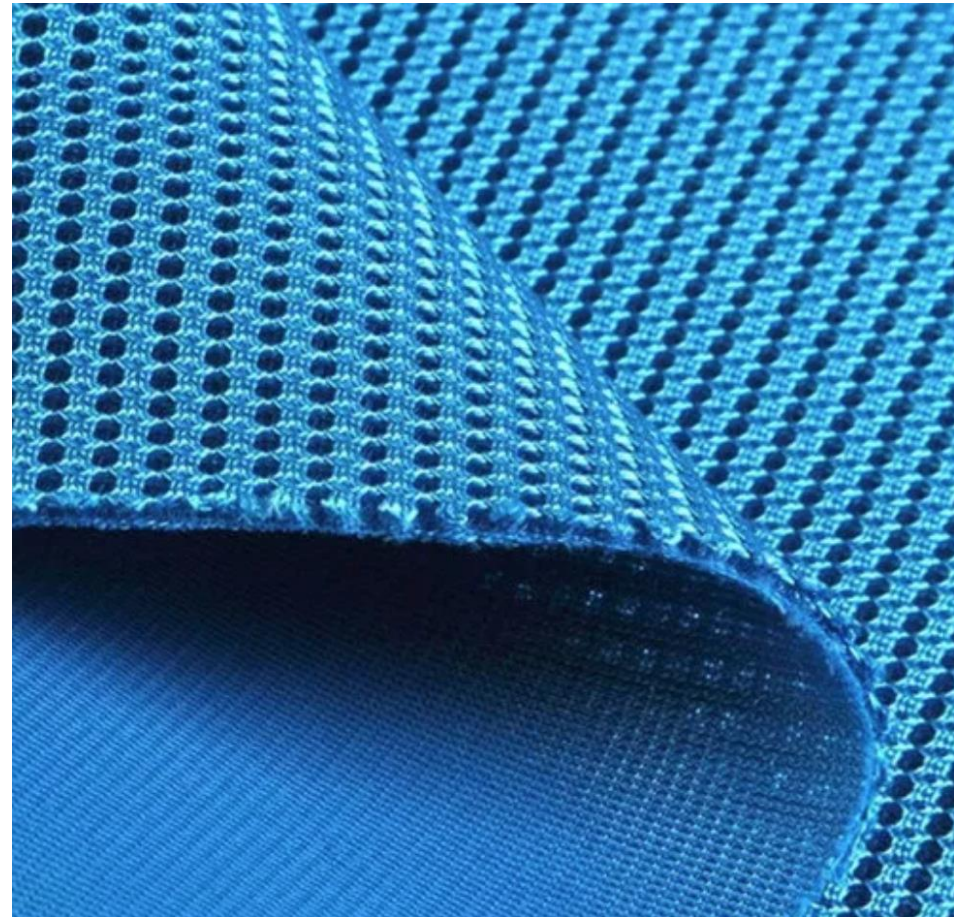


Paris Fashion Week, Fall/Winter 2016/17

New Manufacture Materials



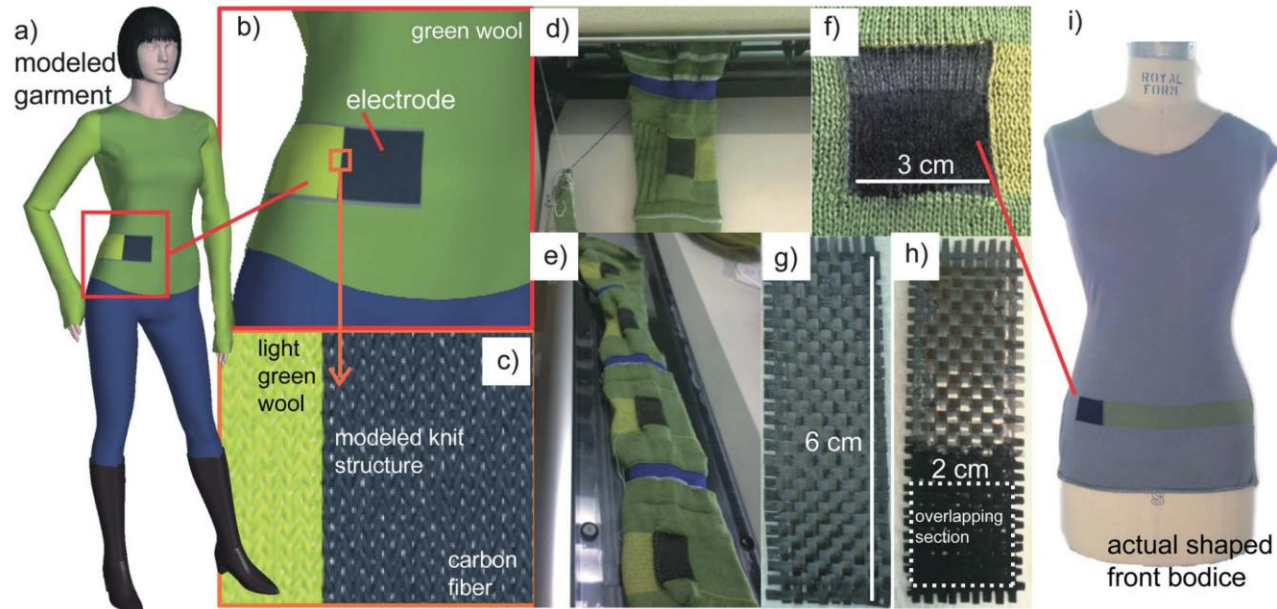
Nike Flyknit



Car Seat Cover

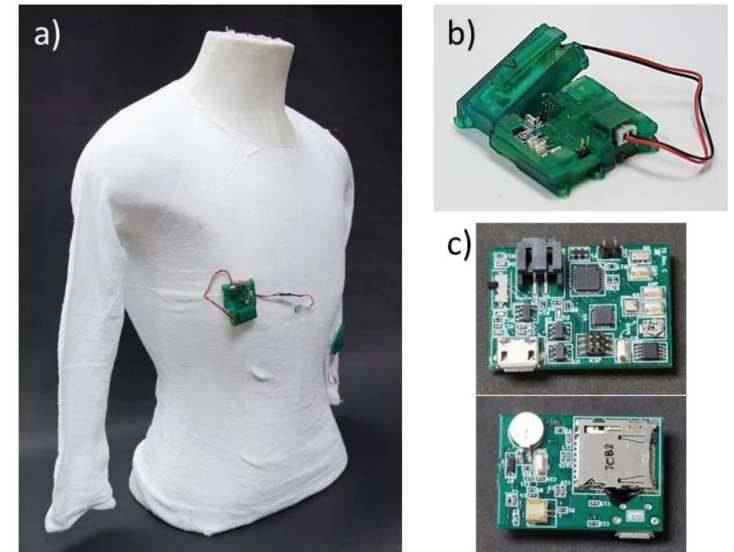
More Applications in Future

- Knitted carbon fiber electrodes



[Jost et al. 2013]

- Wearable thermal energy harvesting



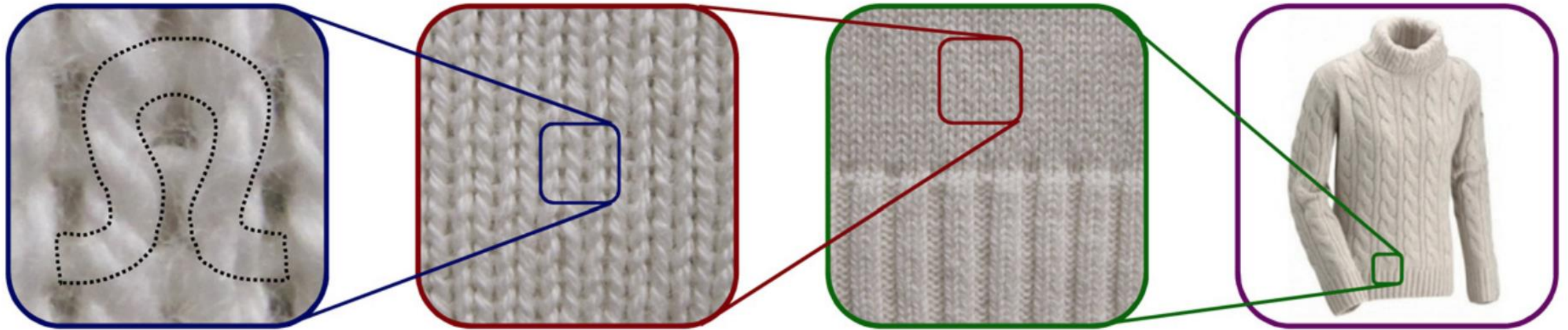
[Myers et al. 2017]

Knitted structure allows some stretches



[Kaldor et al. 2008]

Knit Structure



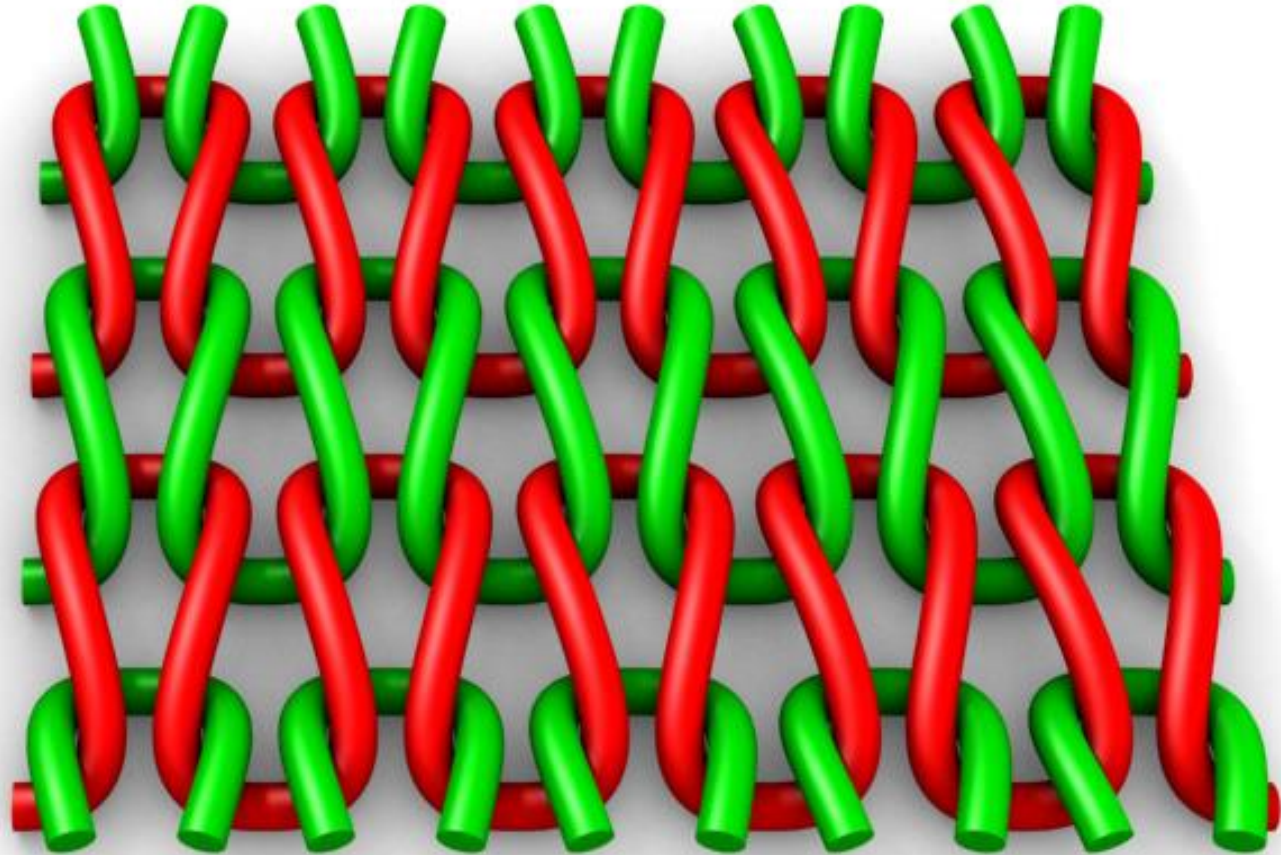
Yarn Loop

[Abel et al. 2013]

Knit Structure

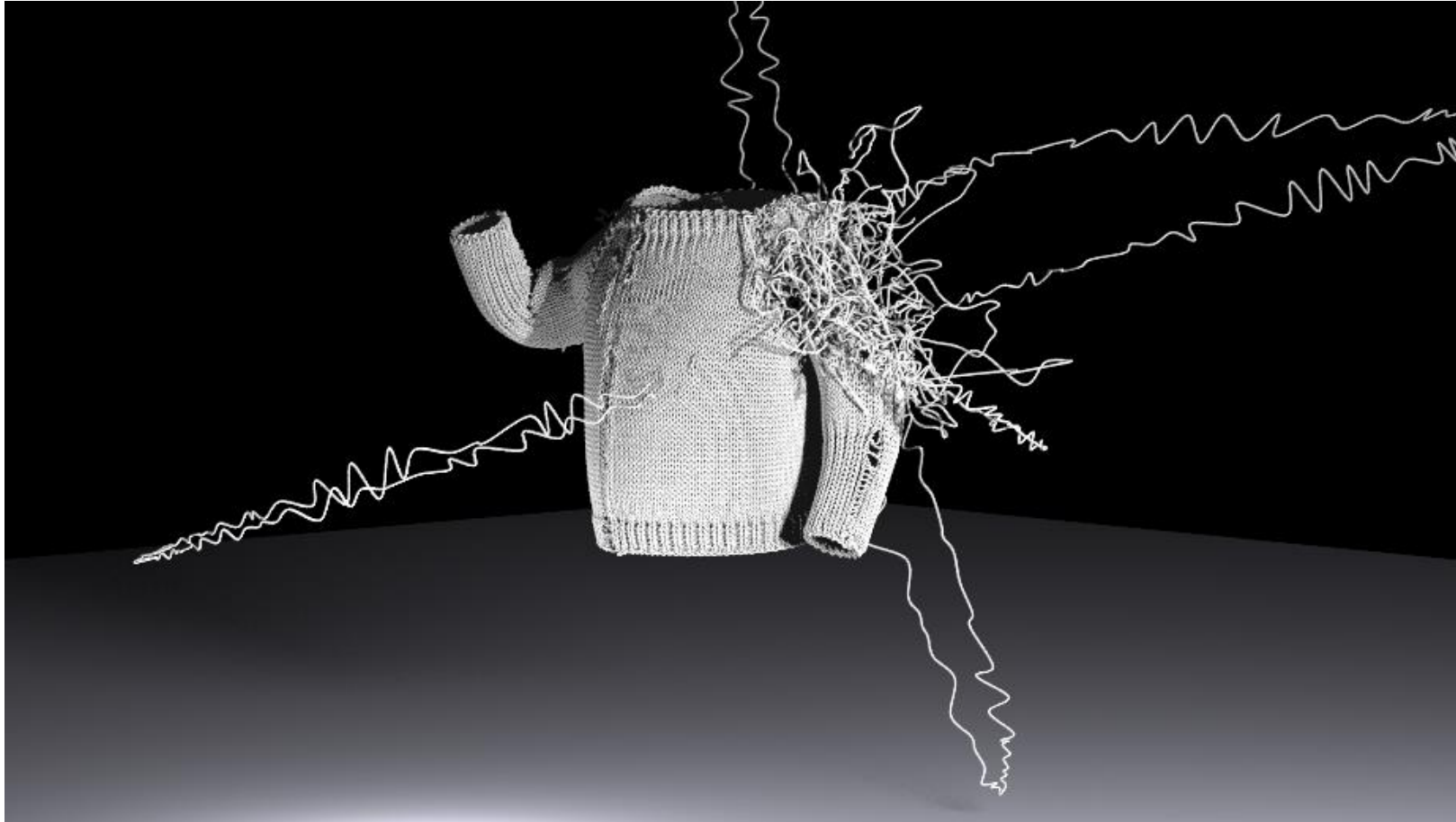


Yarn Loop



[Yuksel et al. 2012]

But not too much

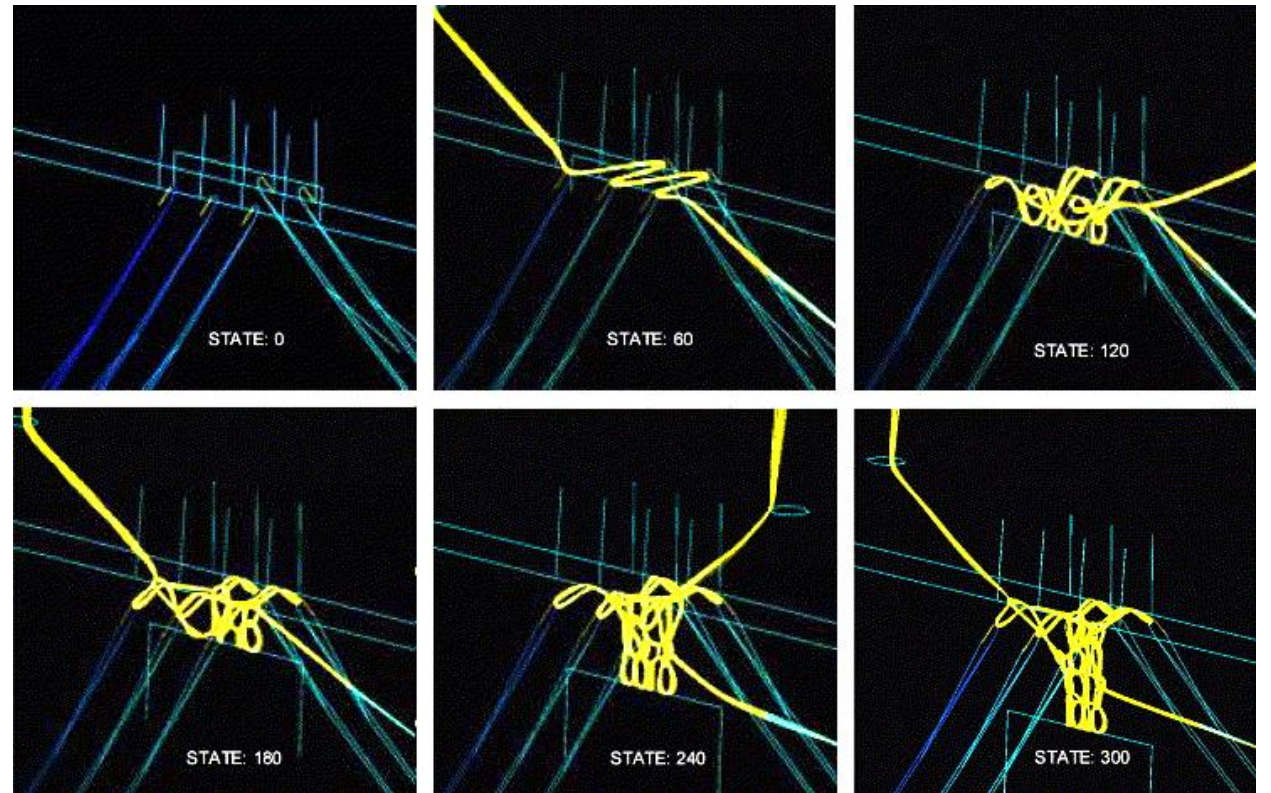
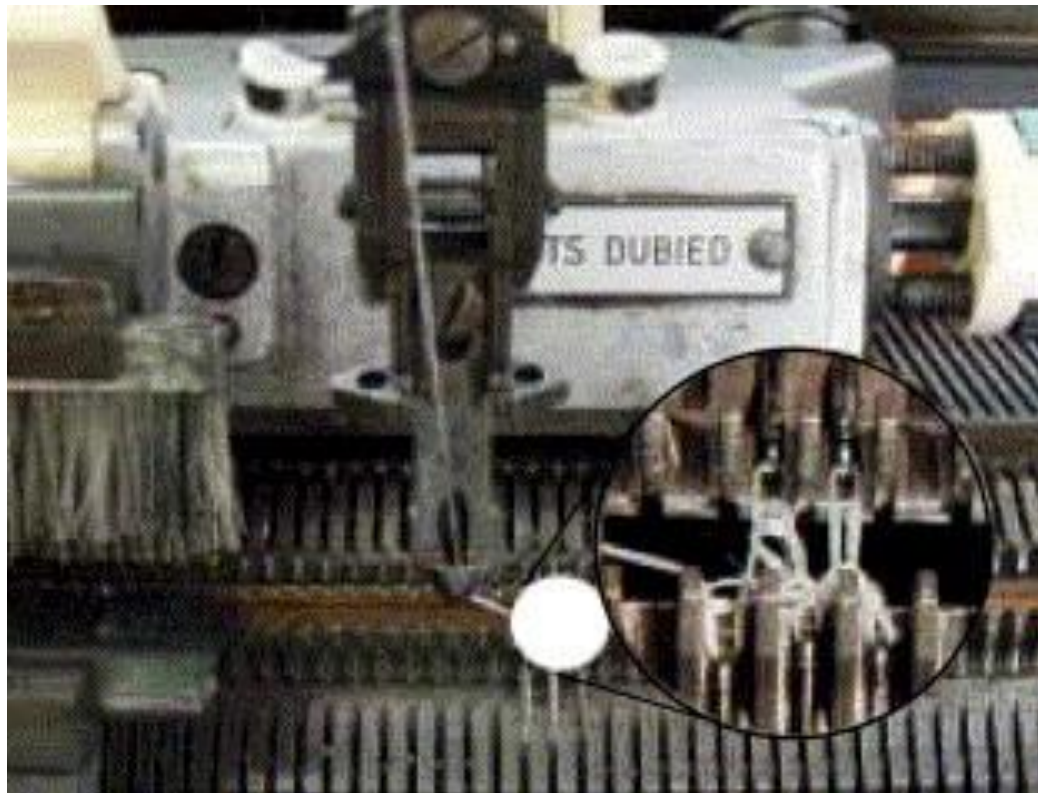


But not too much



Prior Work

- Replicating the process of **knitting machines**

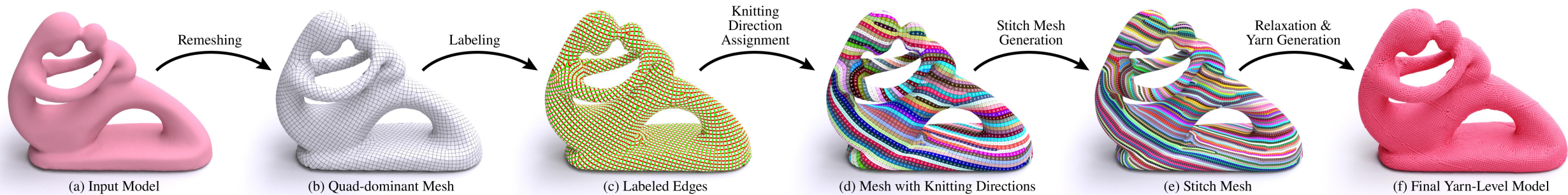


[Duhovic and Bhattacharyya 2006]

Stitch Meshes [Yuksel et al. 2012]



Stitch Meshing

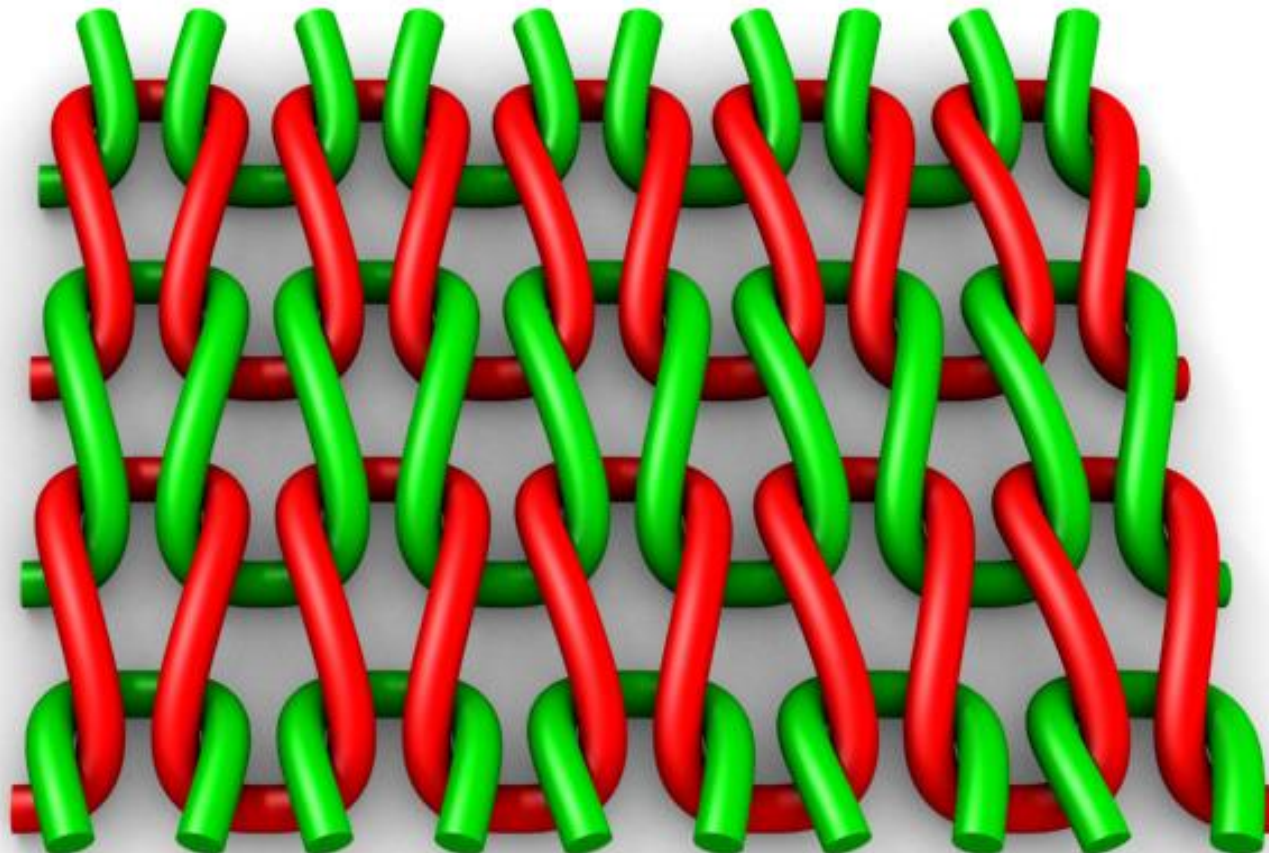


Yarn Loops & Stitches [Yuksel et al. 2012]



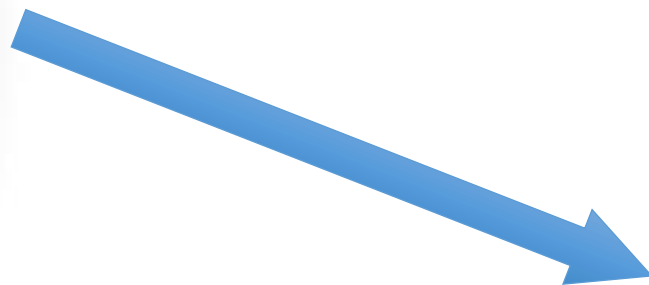
Yarn Loop

wale



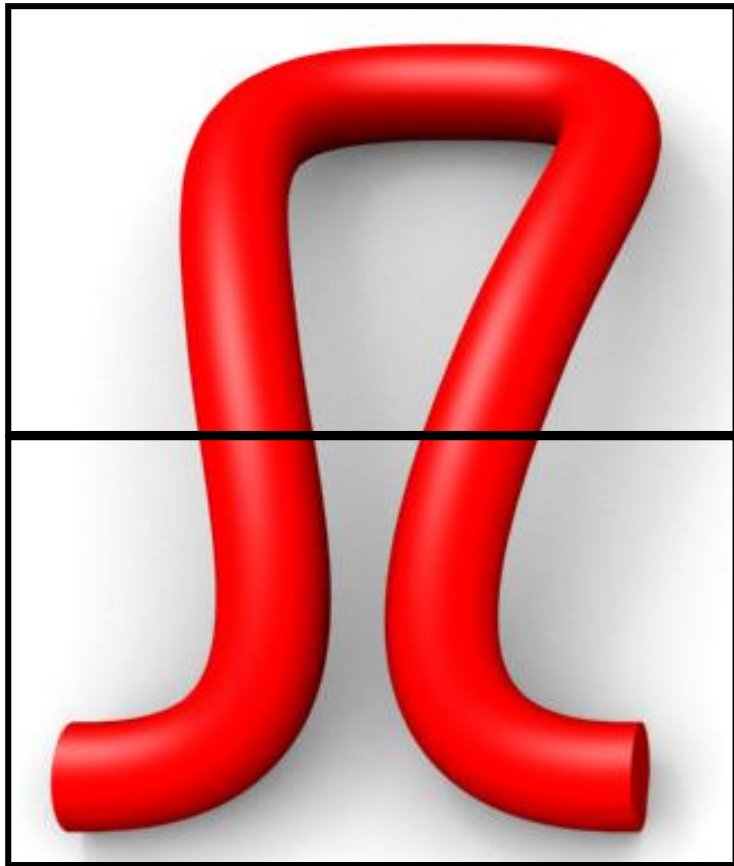
course

Yarn Loops & Stitches [Yuksel et al. 2012]

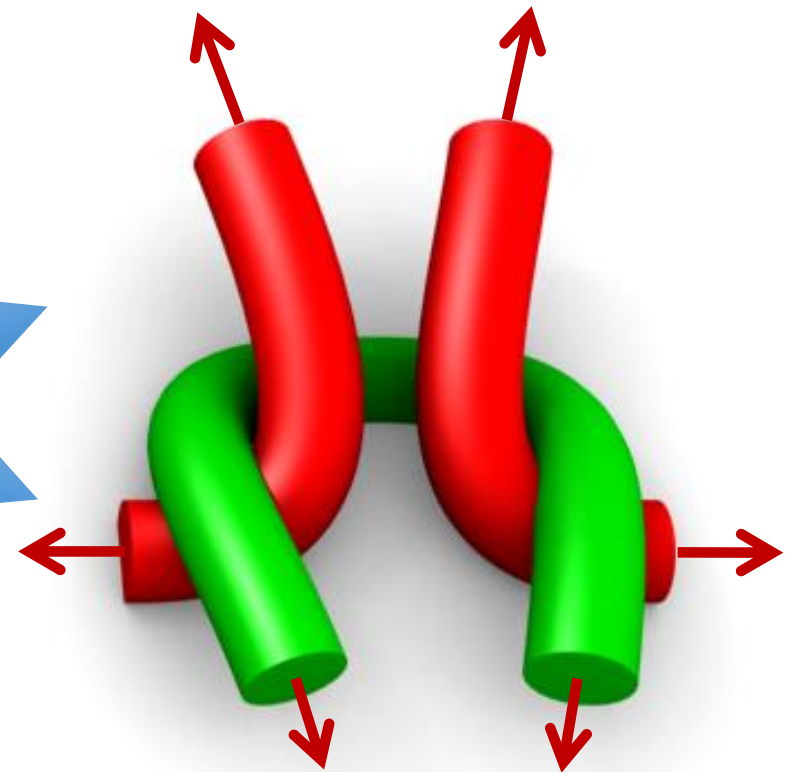
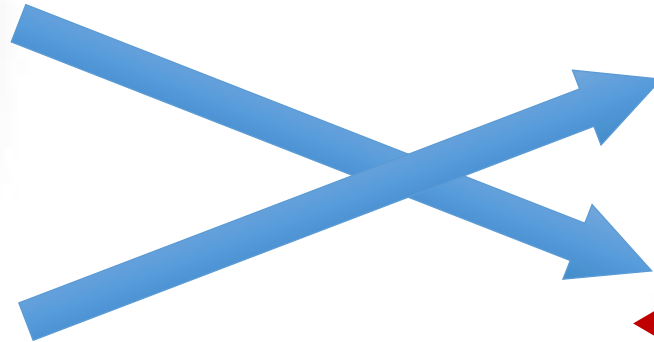


Yarn Loop

Yarn Loops & Stitches [Yuksel et al. 2012]



Yarn Loop



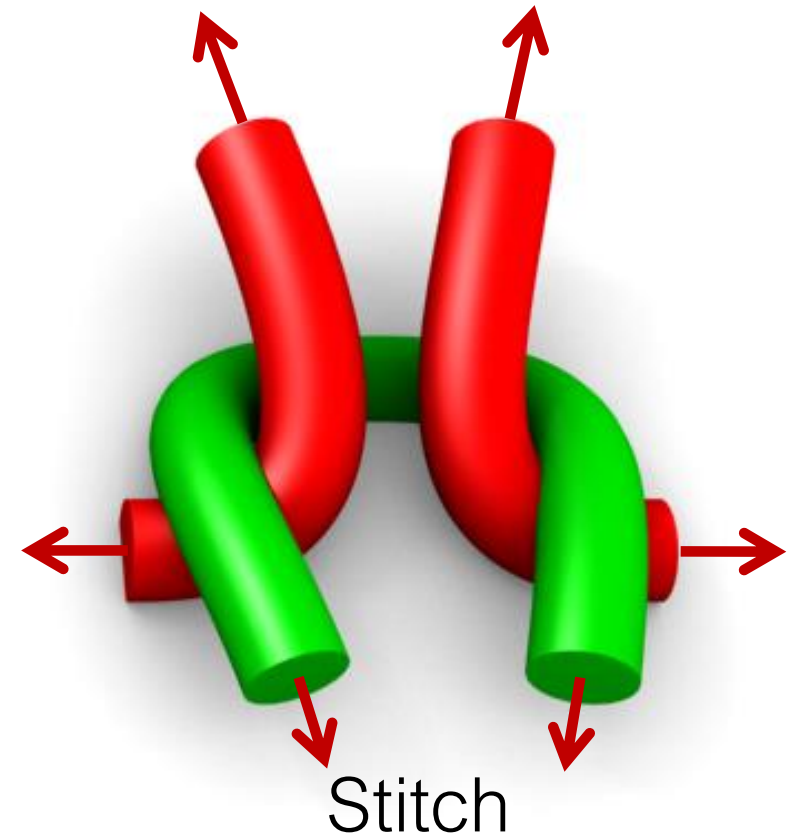
Stitch

Stitch Mesh Face

[Yuksel et al. 2012]



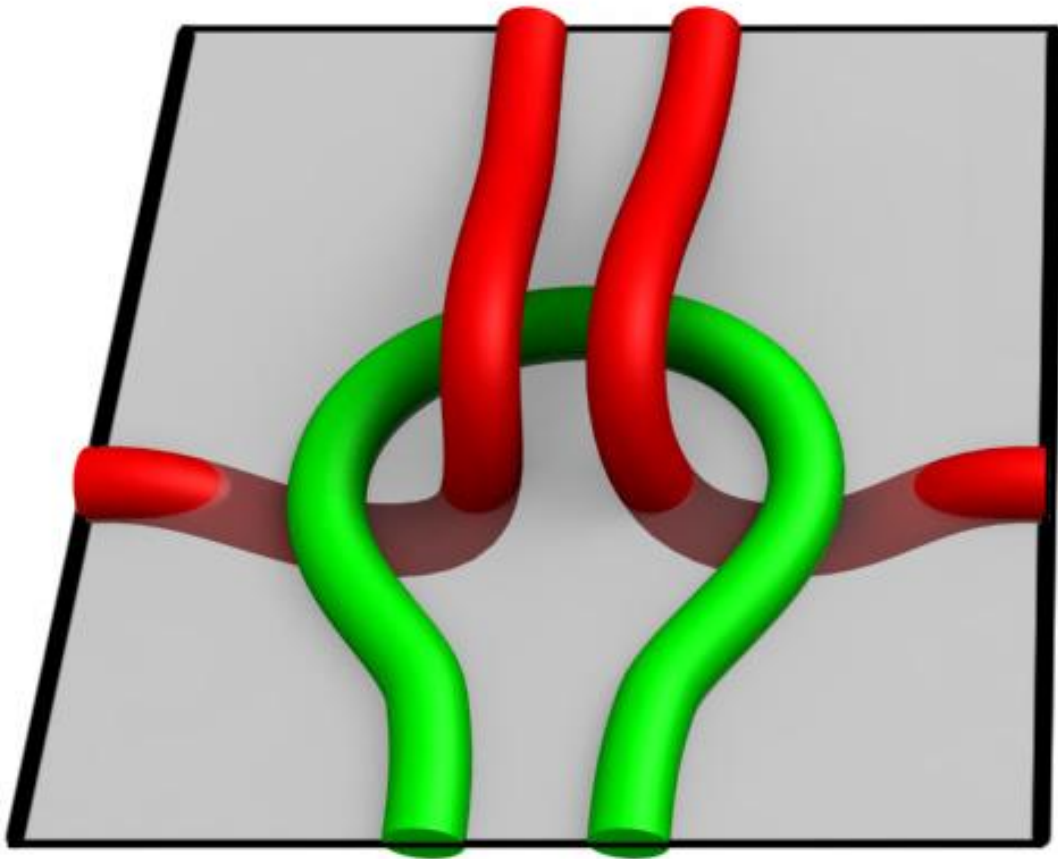
Stitch Mesh Face



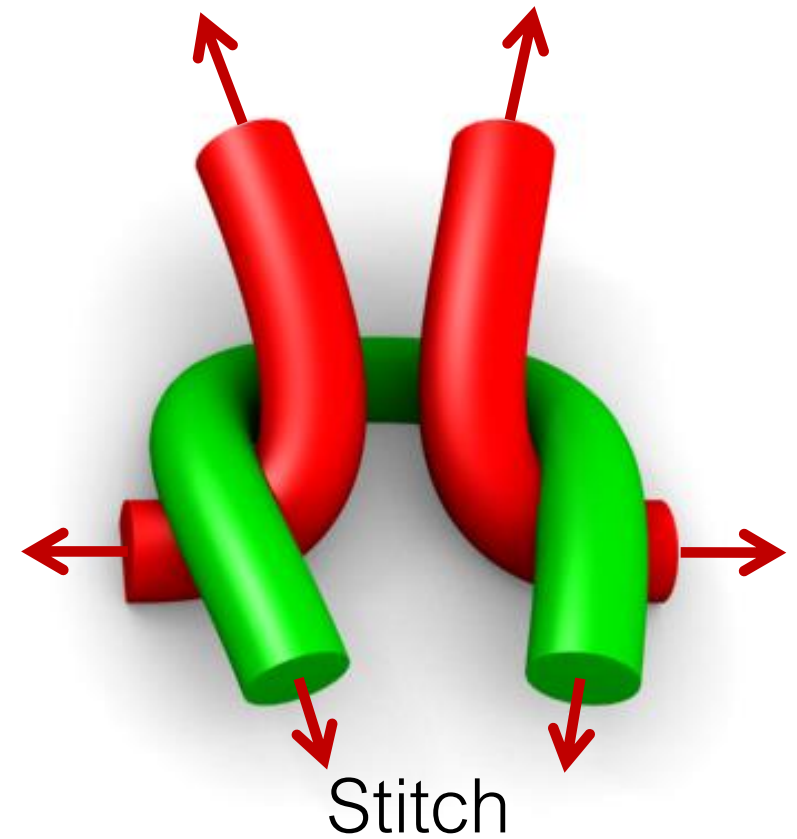
Stitch

Stitch Mesh Face

[Yuksel et al. 2012]

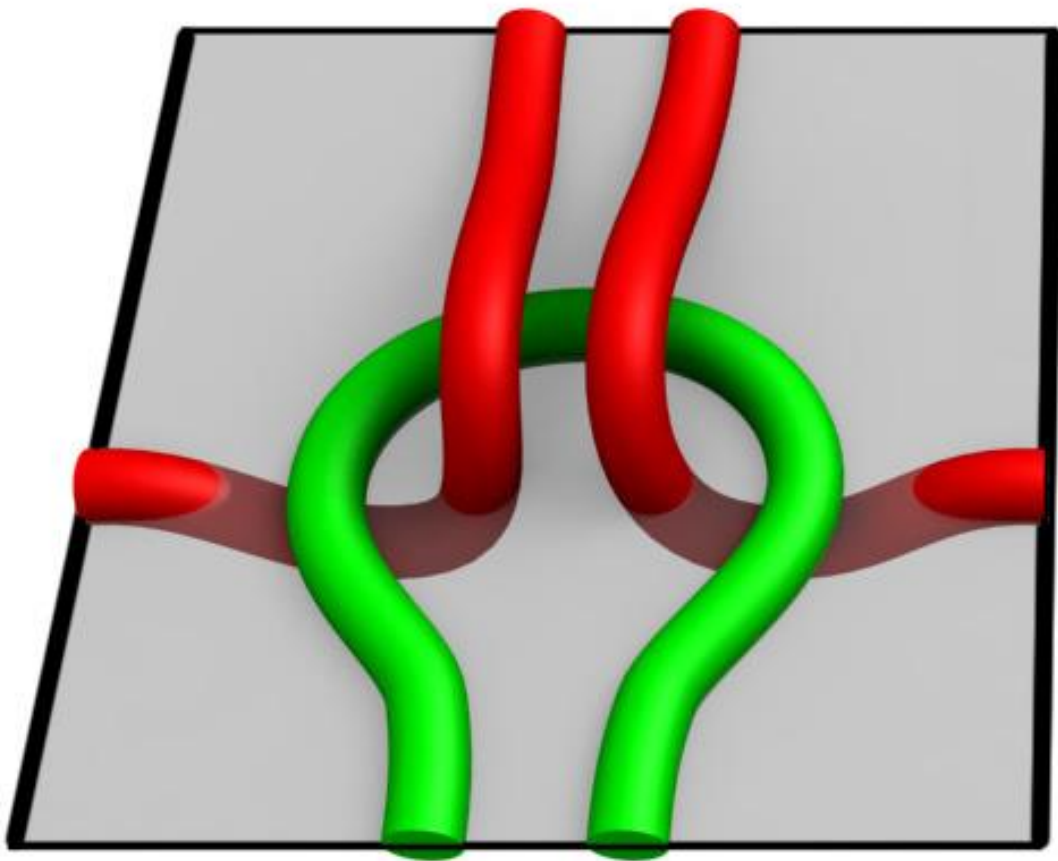


Stitch Mesh Face

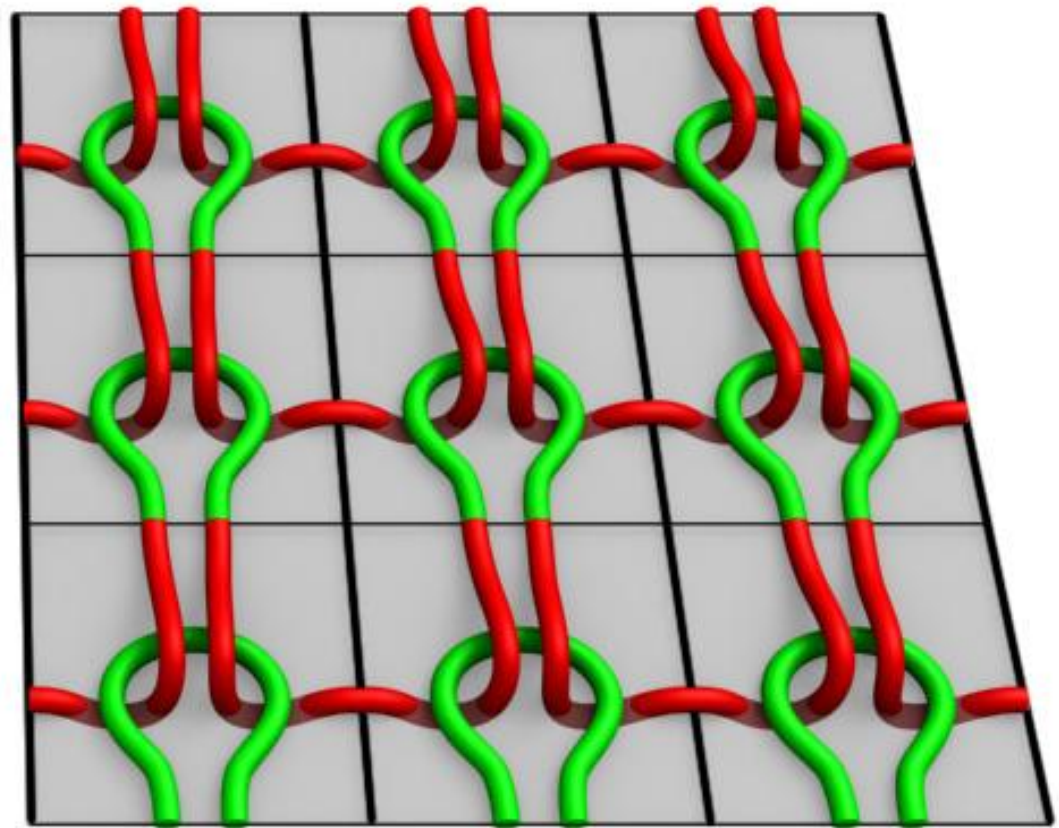


Stitch

The Stitch Mesh Face [Yuksel et al. 2012]

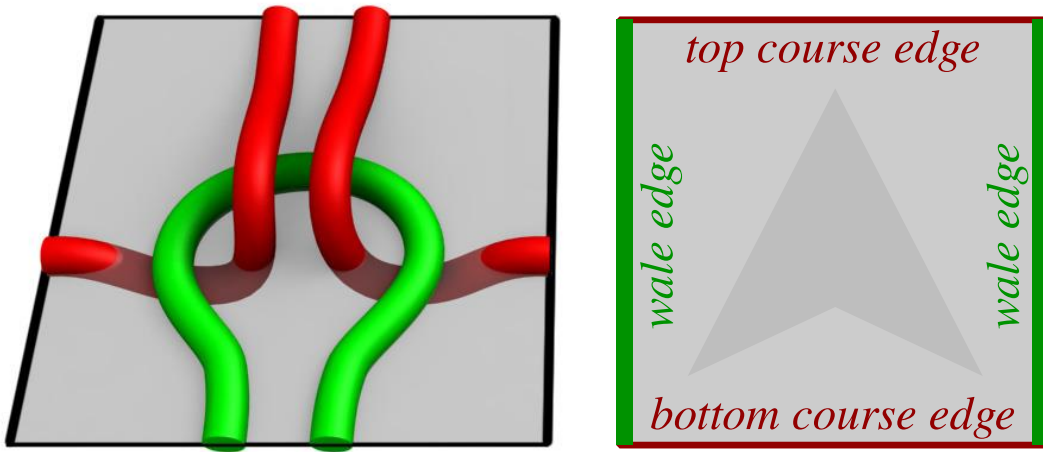


Stitch Mesh Face

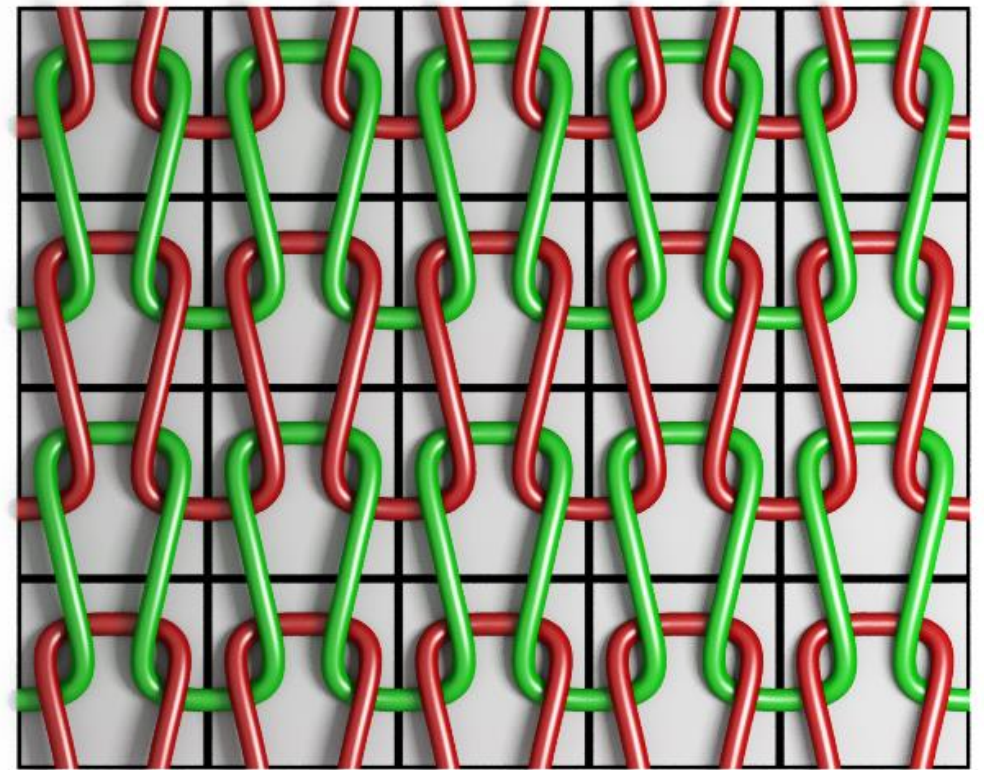


Stitch Mesh

Stitch Meshes

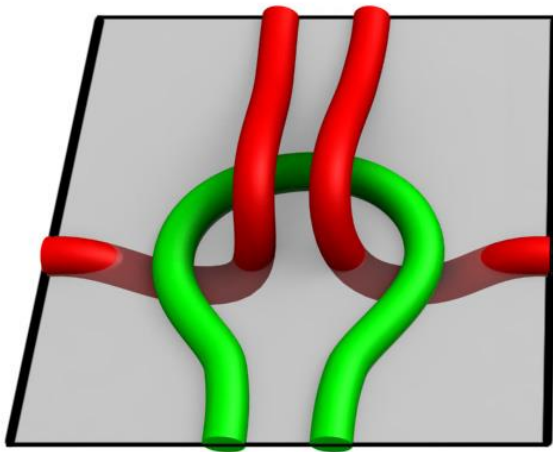


Stitch Mesh Face

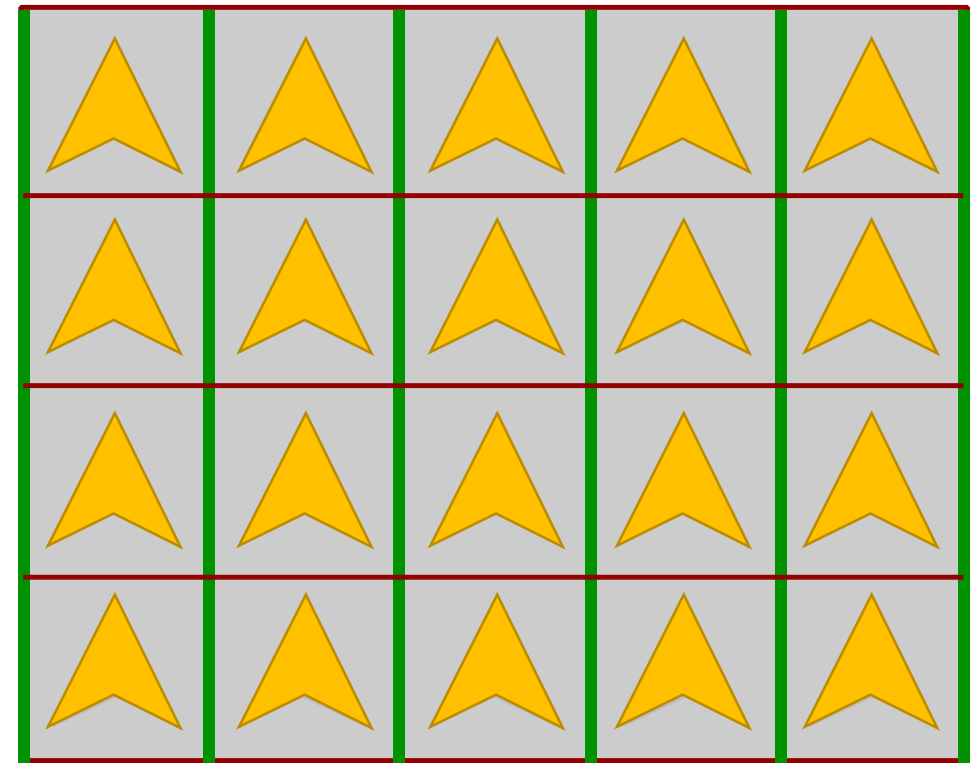
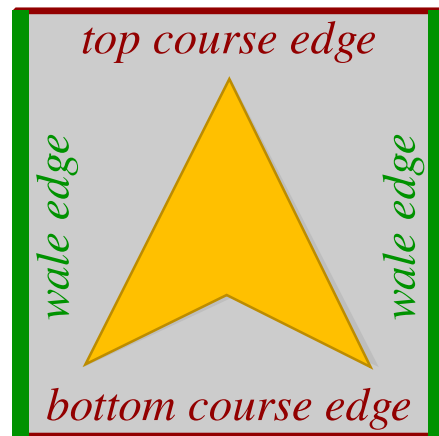


Stitch Mesh

Stitch Meshes

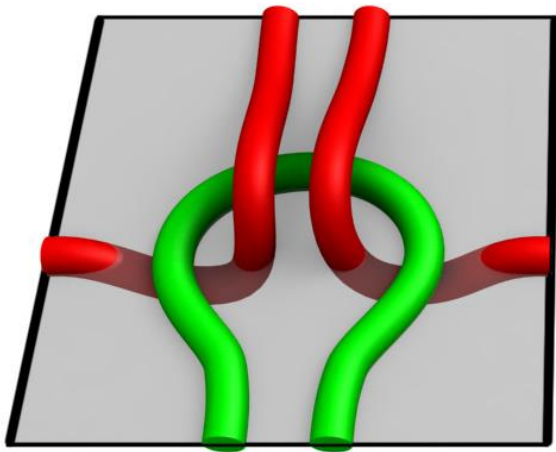


Stitch Mesh Face

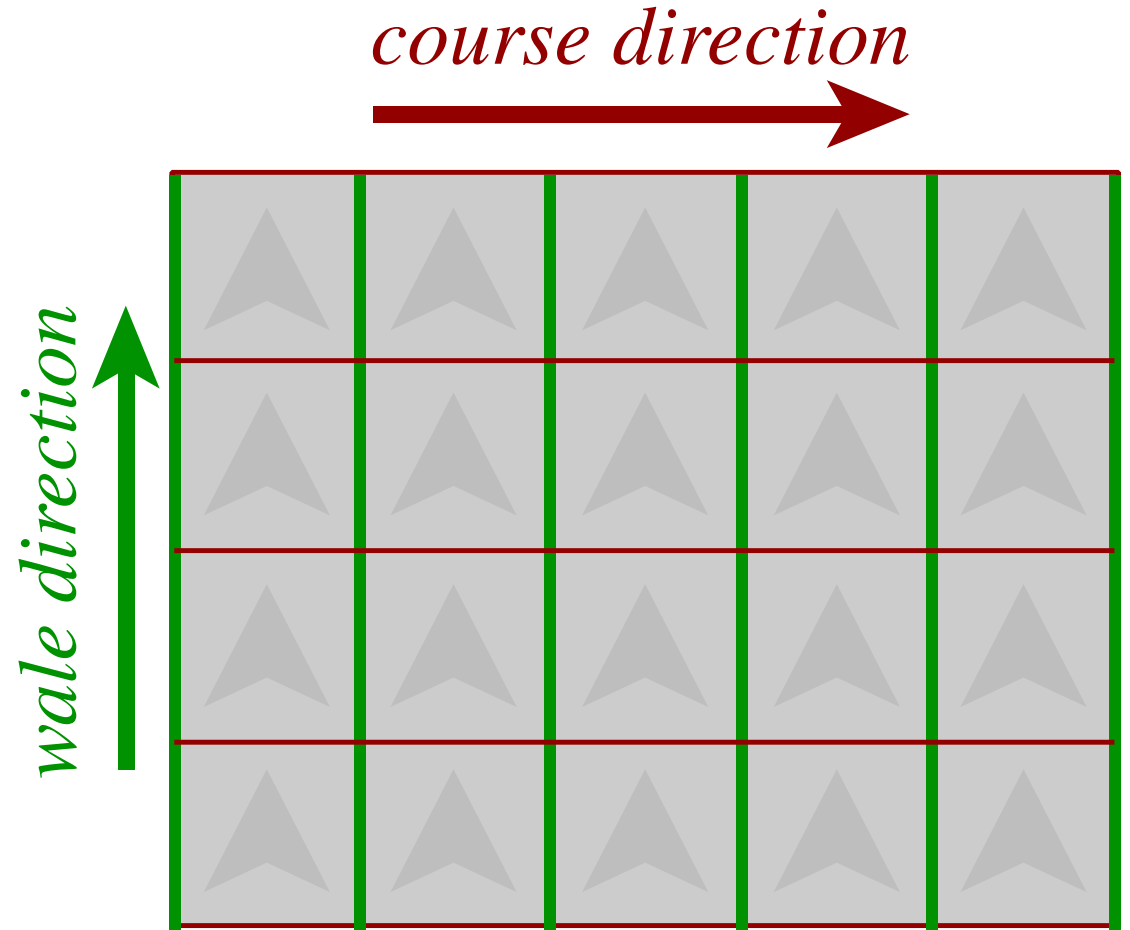
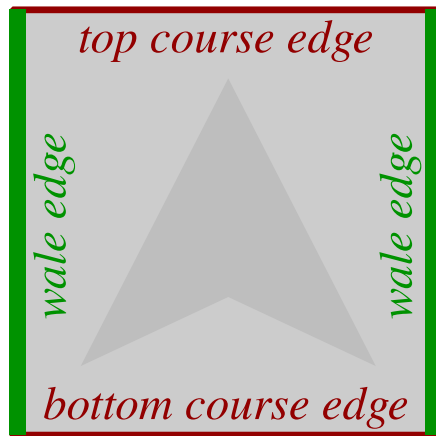


Stitch Mesh

Stitch Meshes

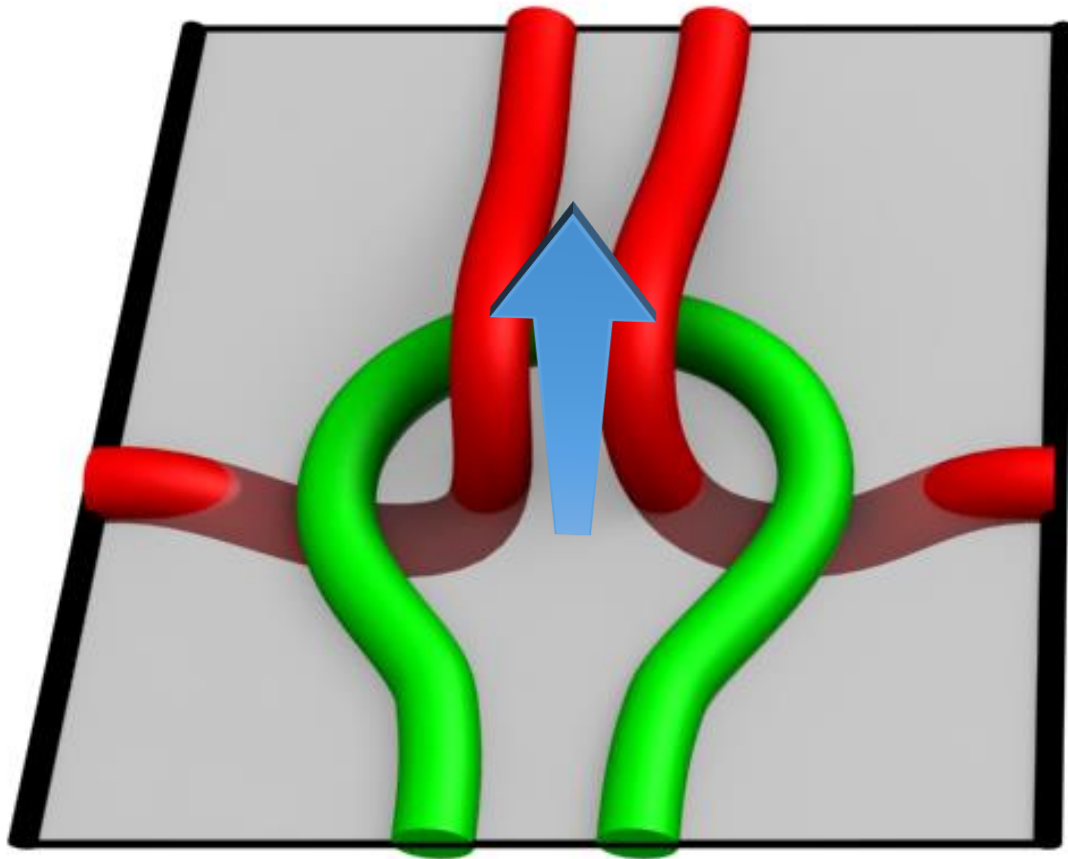


Stitch Mesh Face

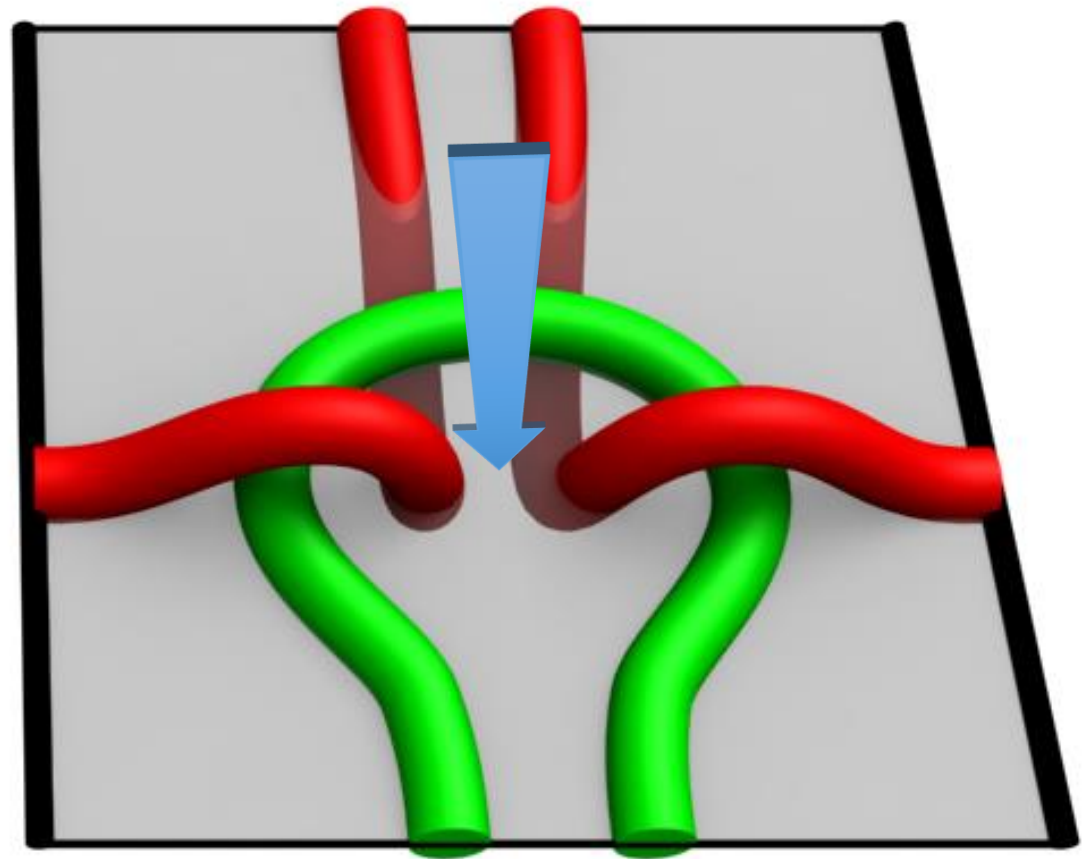


Stitch Mesh

The Stitch Mesh Face [Yuksel et al. 2012]

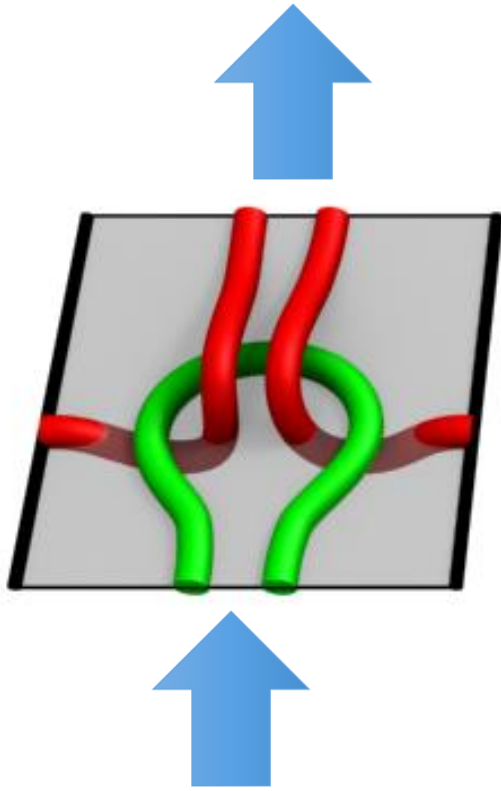


knit

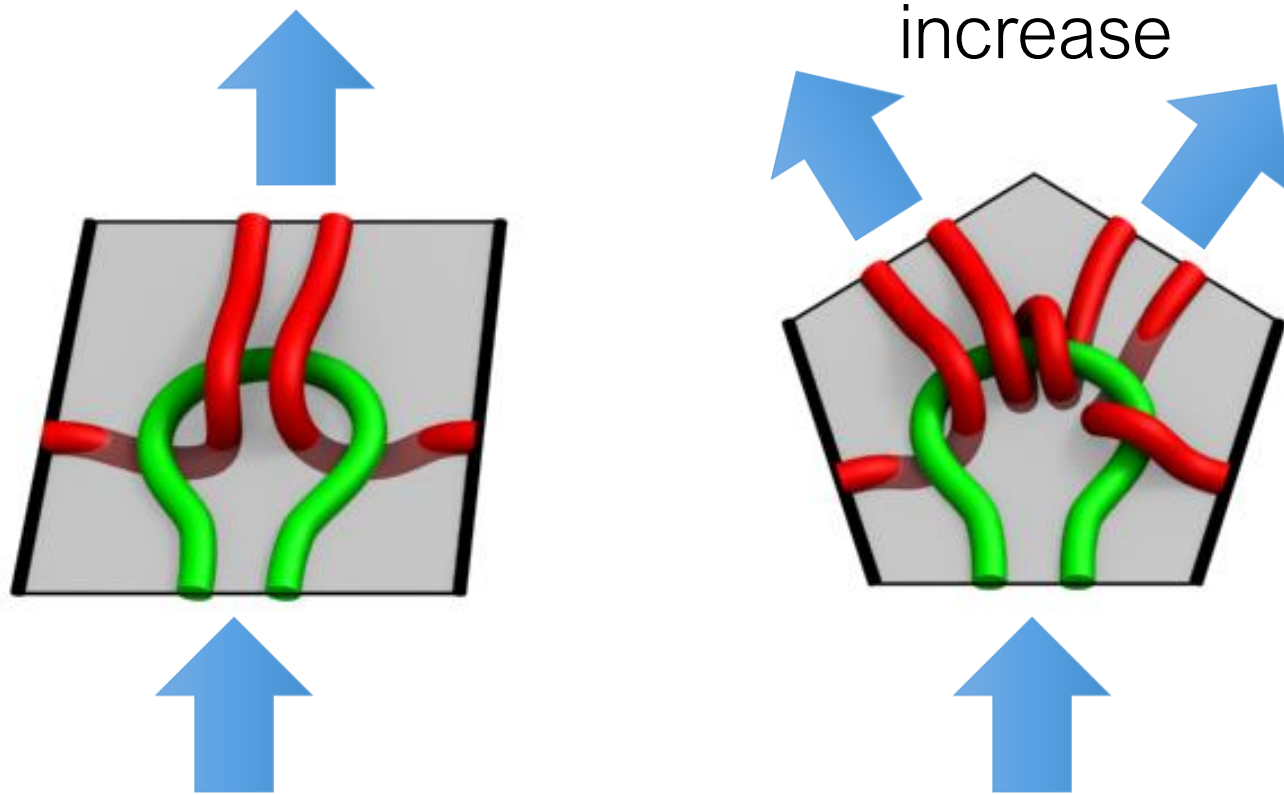


purl

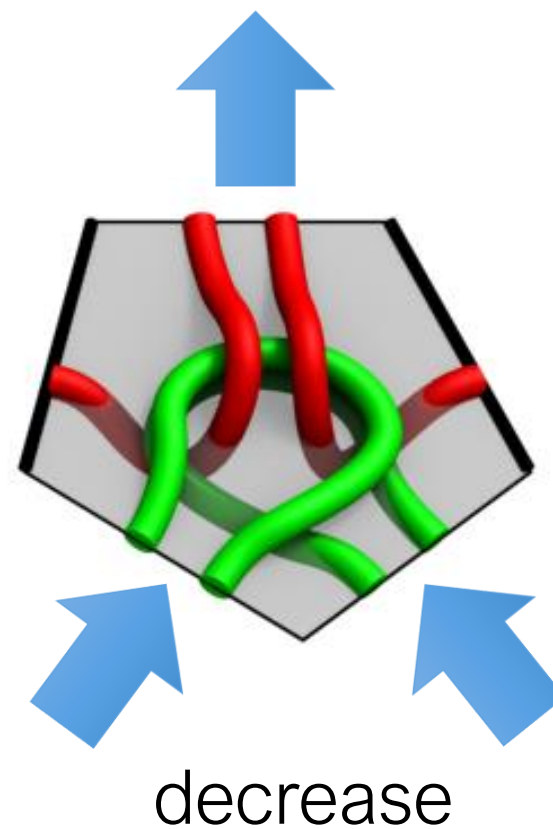
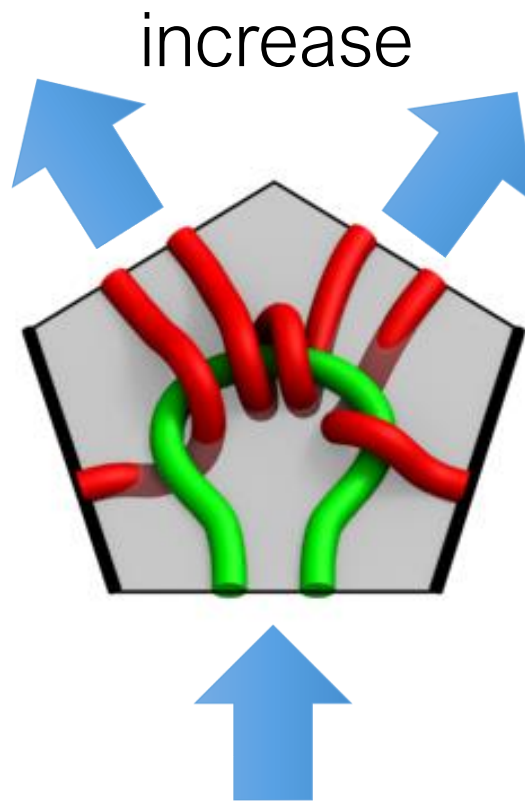
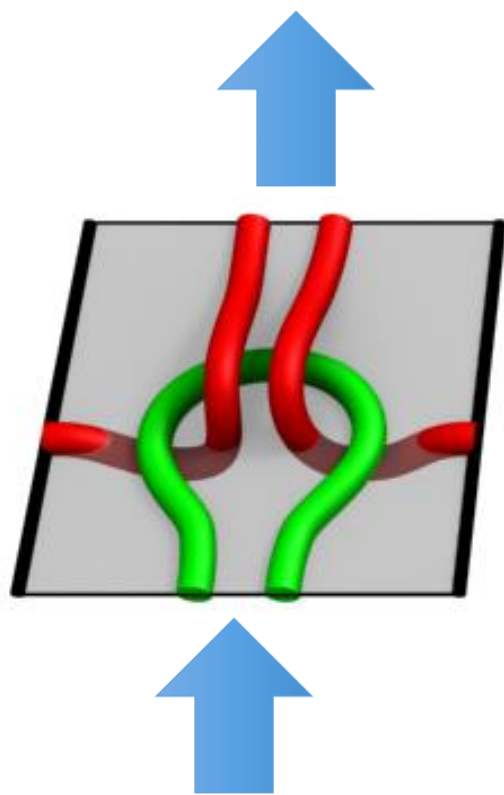
Increases & Decreases [Yuksel et al. 2012]



Increases & Decreases [Yuksel et al. 2012]

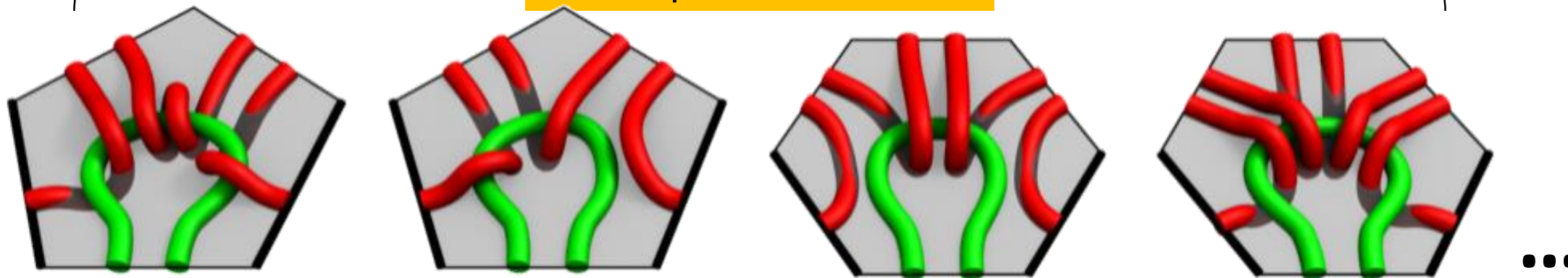


Increases & Decreases [Yuksel et al. 2012]



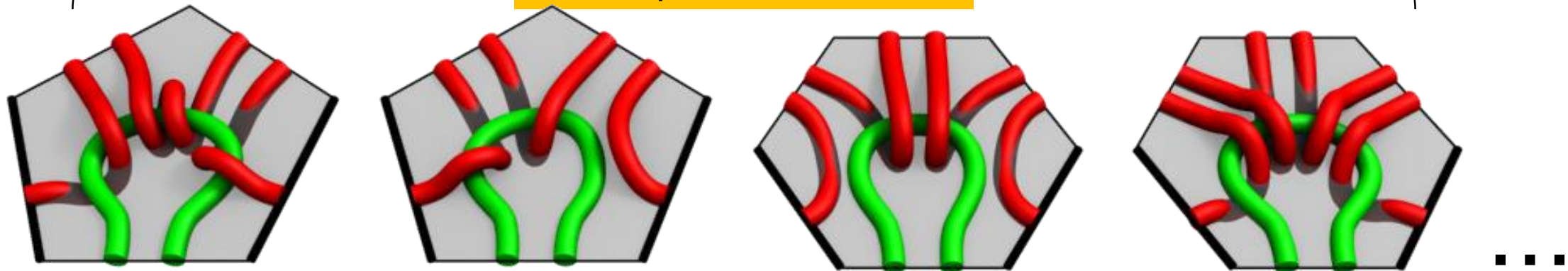
Increases & Decreases [Yuksel et al. 2012]

example increases

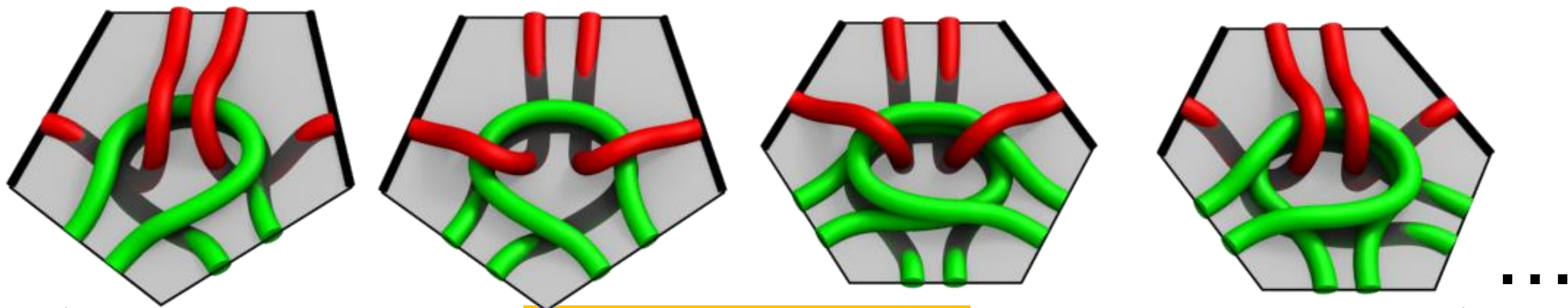


Increases & Decreases [Yuksel et al. 2012]

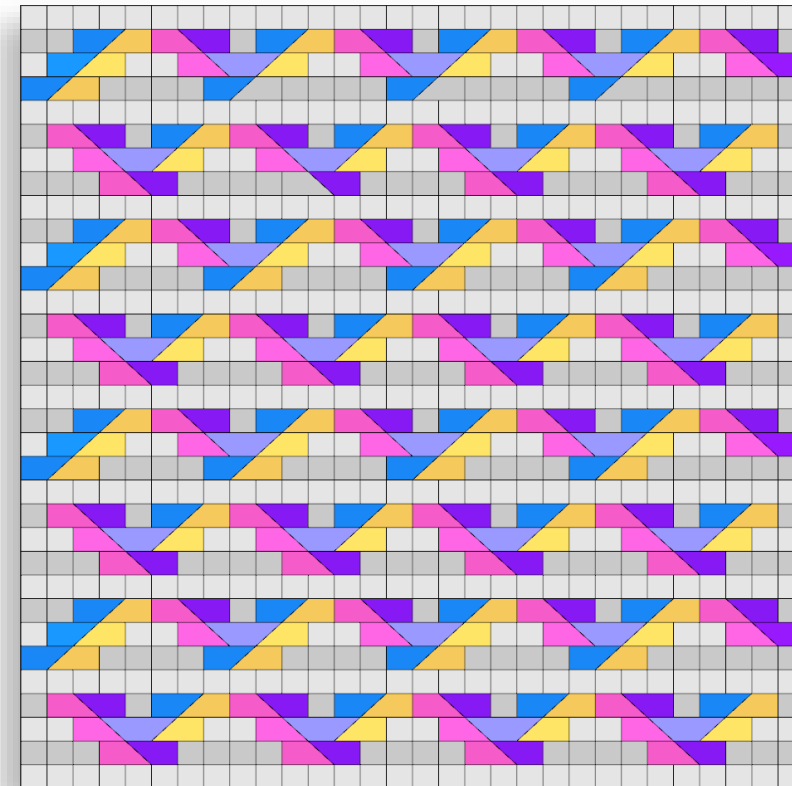
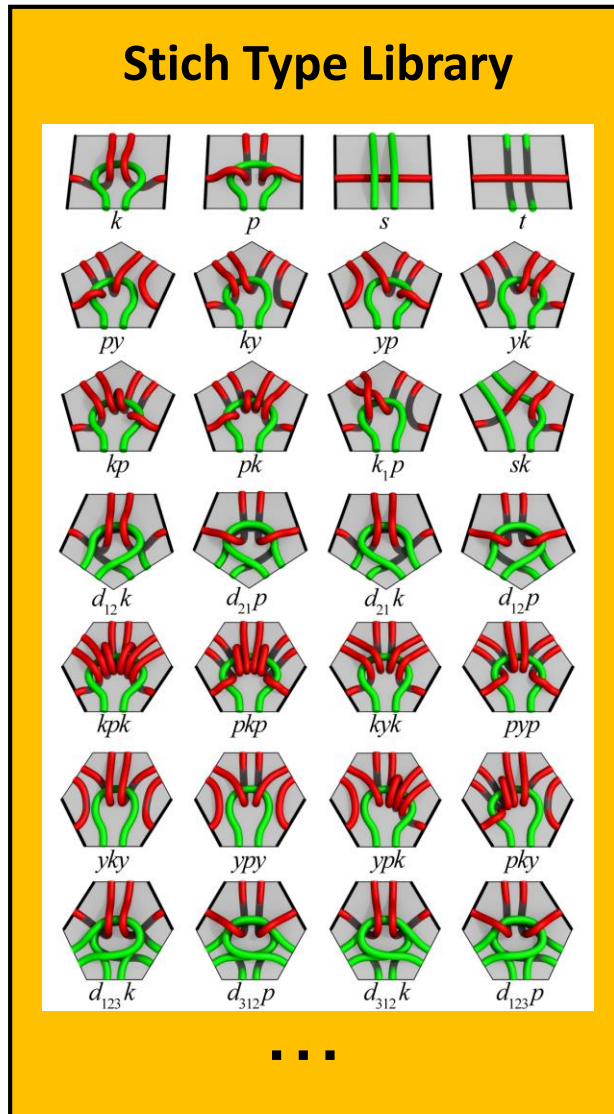
example increases



example decreases

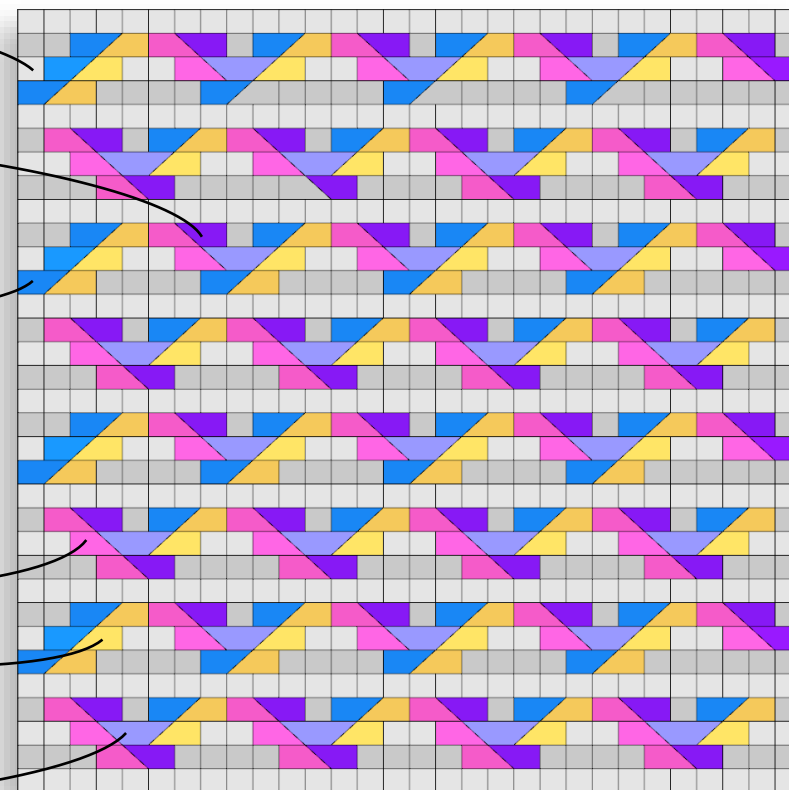
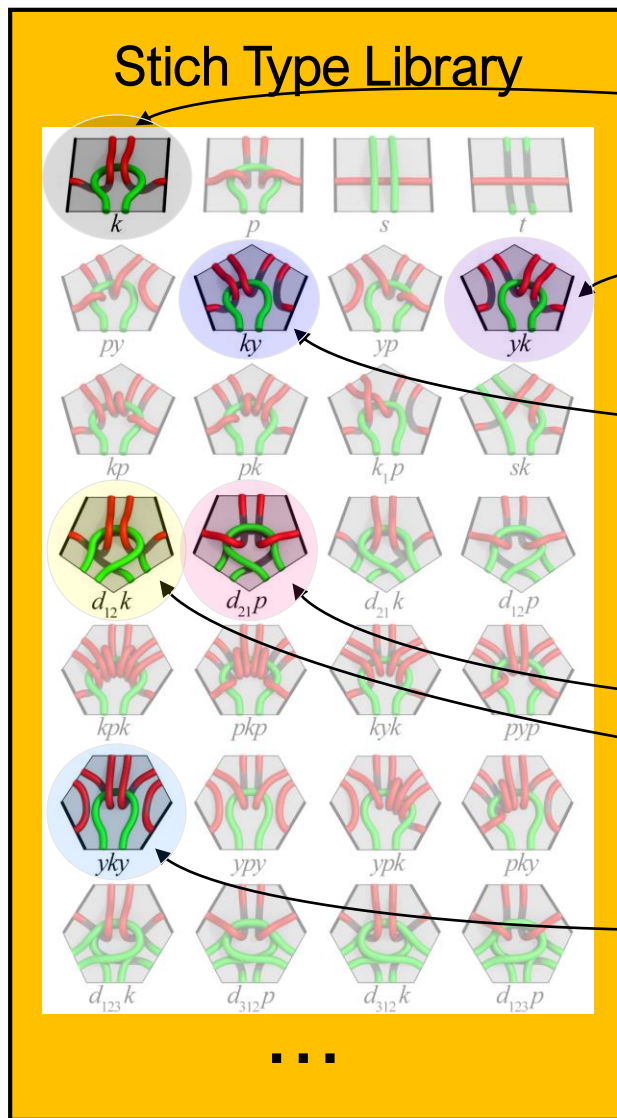


Stitch Type Library [Yuksel et al. 2012]



Stitch Mesh

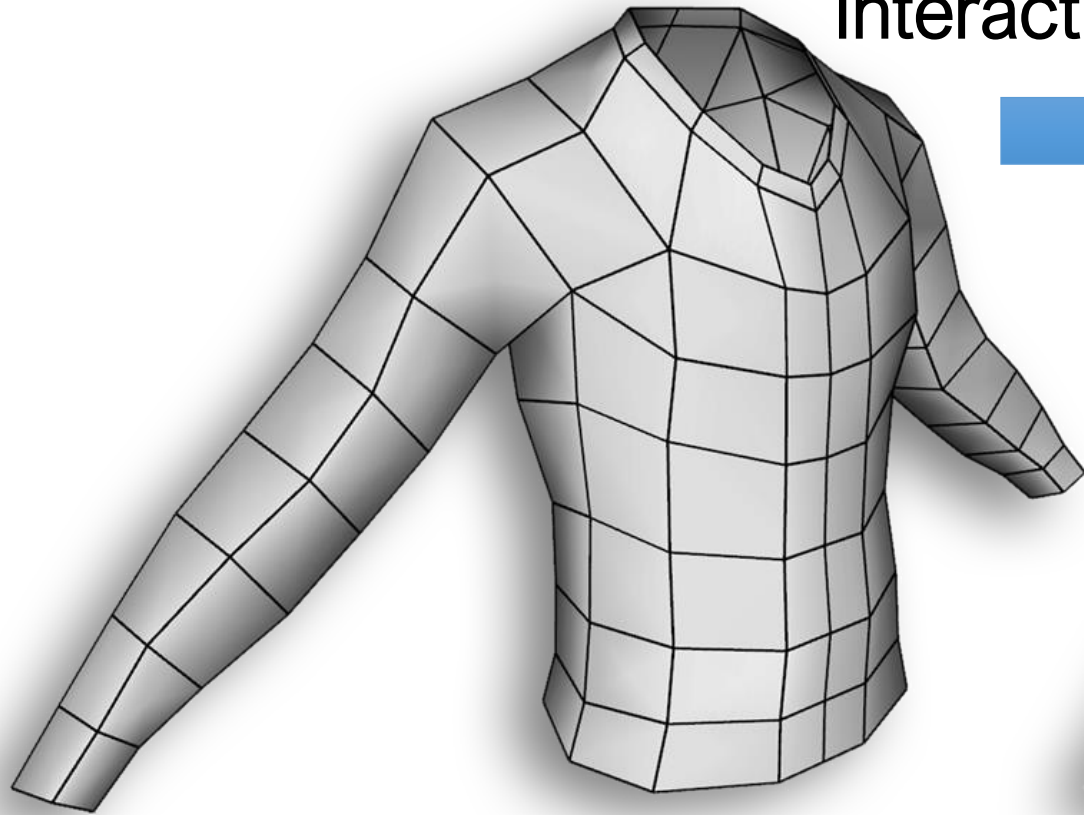
Stitch Type Library [Yuksel et al. 2012]



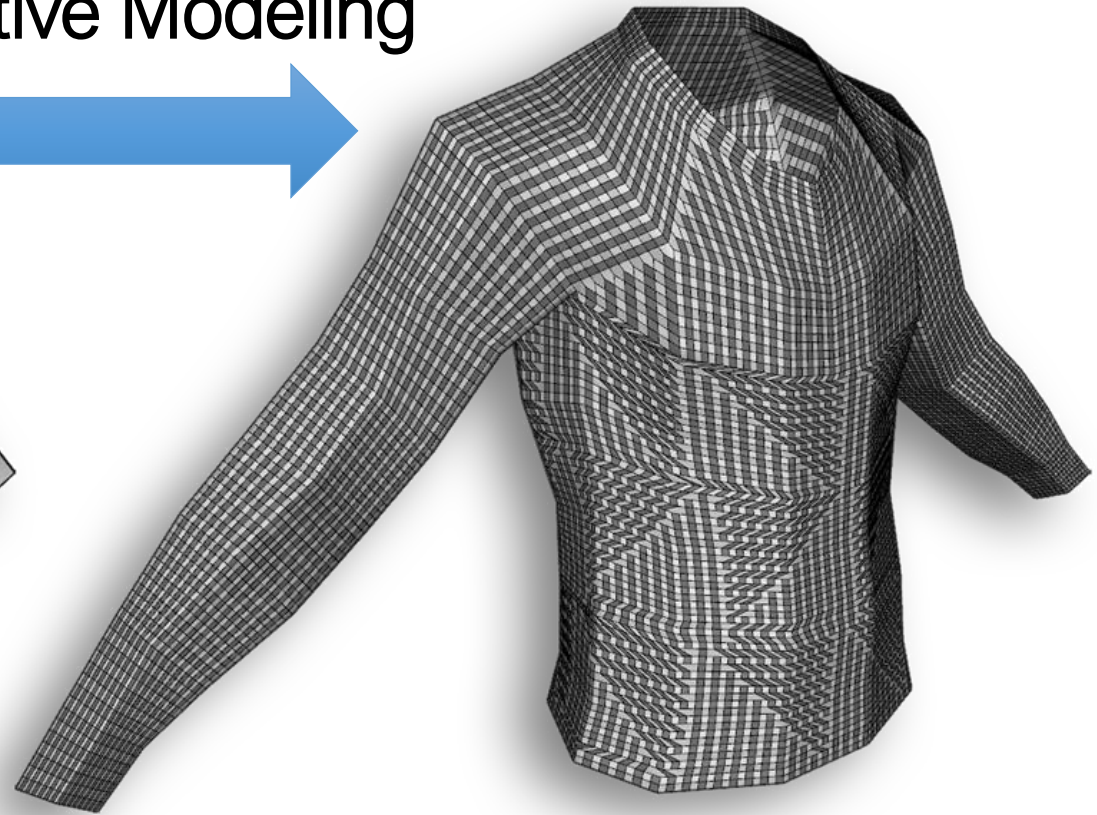
Stitch Mesh

Stitch Mesh [Yuksel et al. 2012]

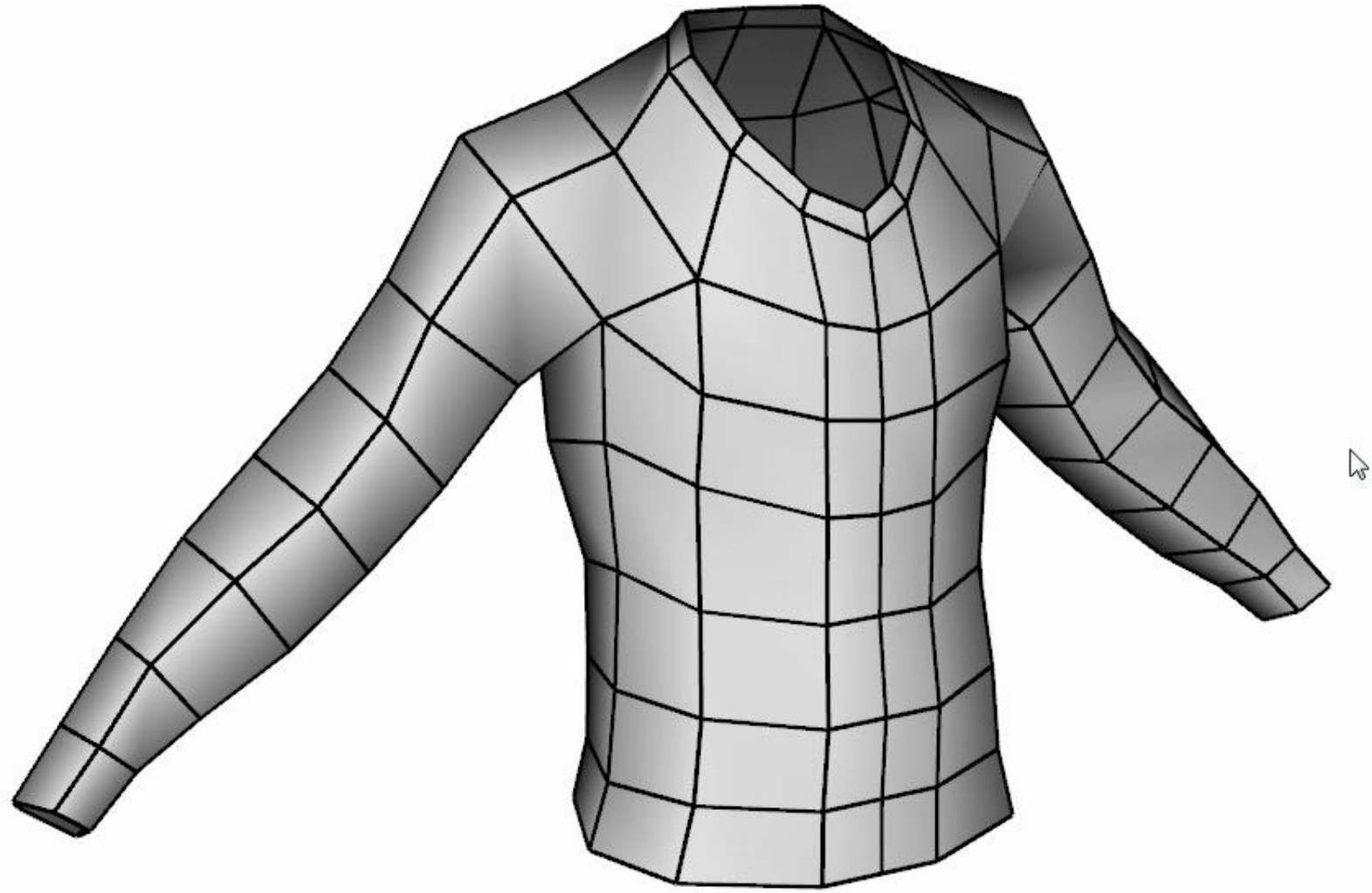
Interactive Modeling



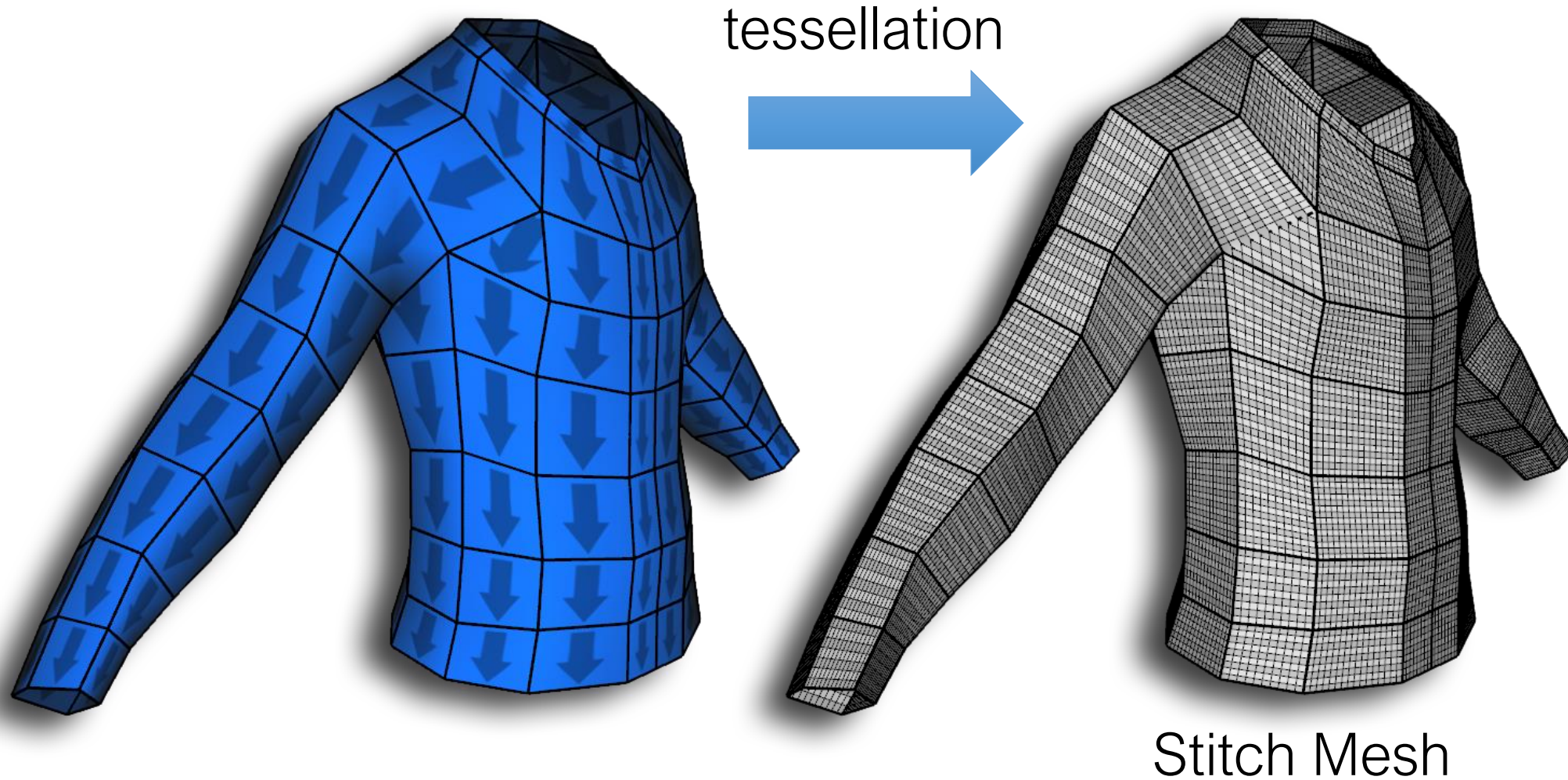
Input Mesh



Stitch Mesh



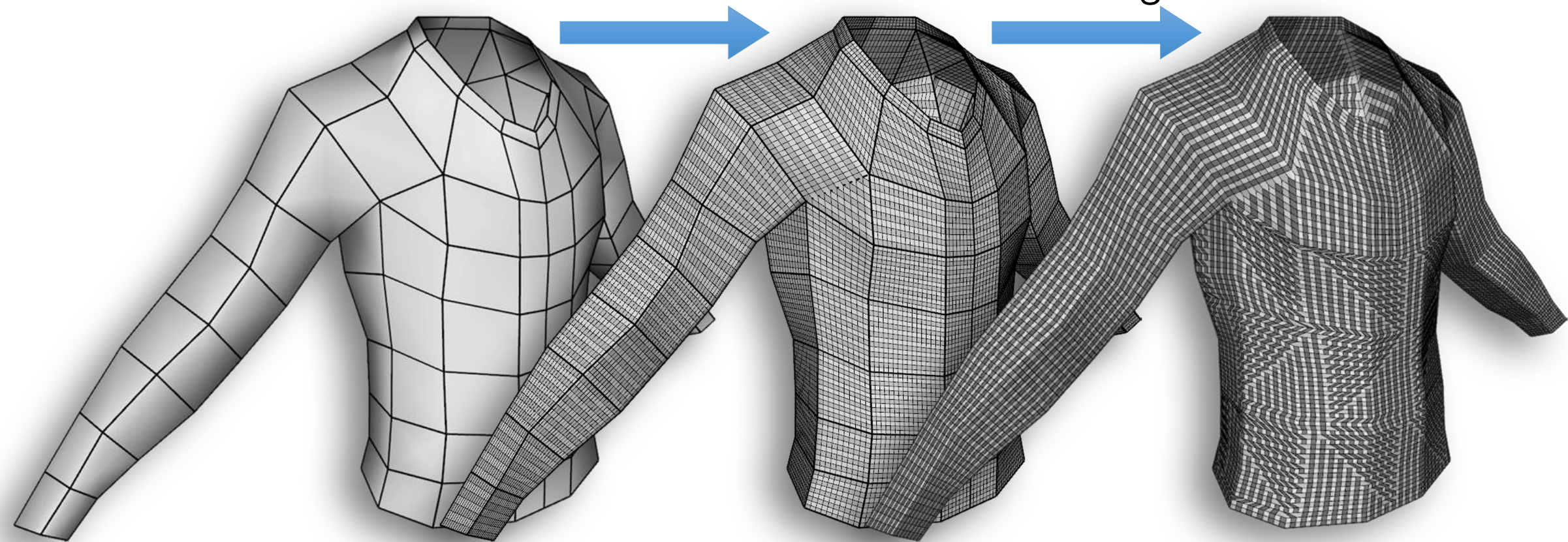
Stitch Mesh Generation [Yüksel et al. 2012]



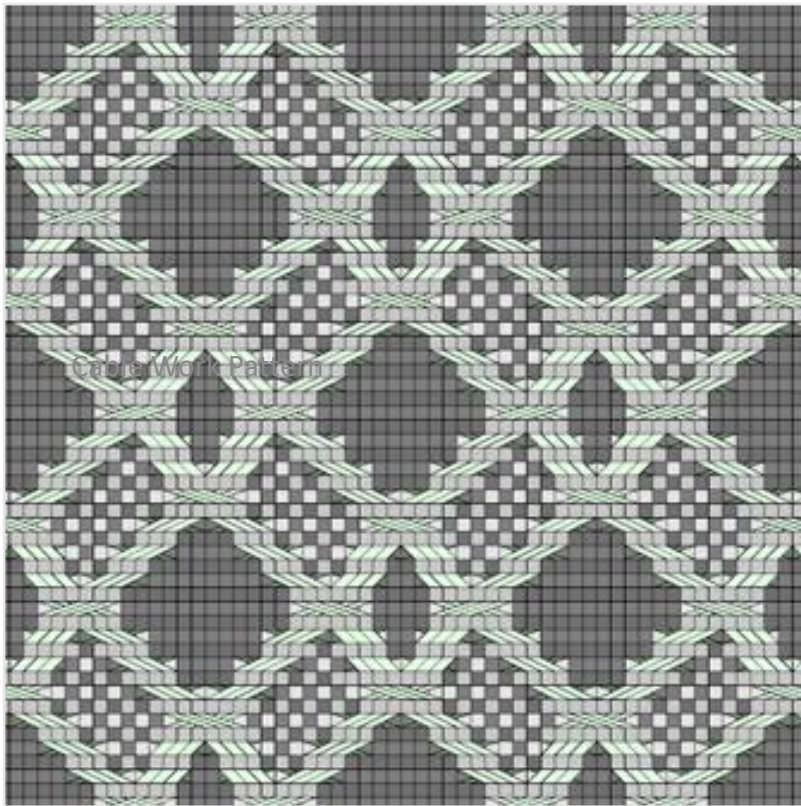
Interactive Modeling [Yuksel et al. 2012]

Stitch Mesh
Generation

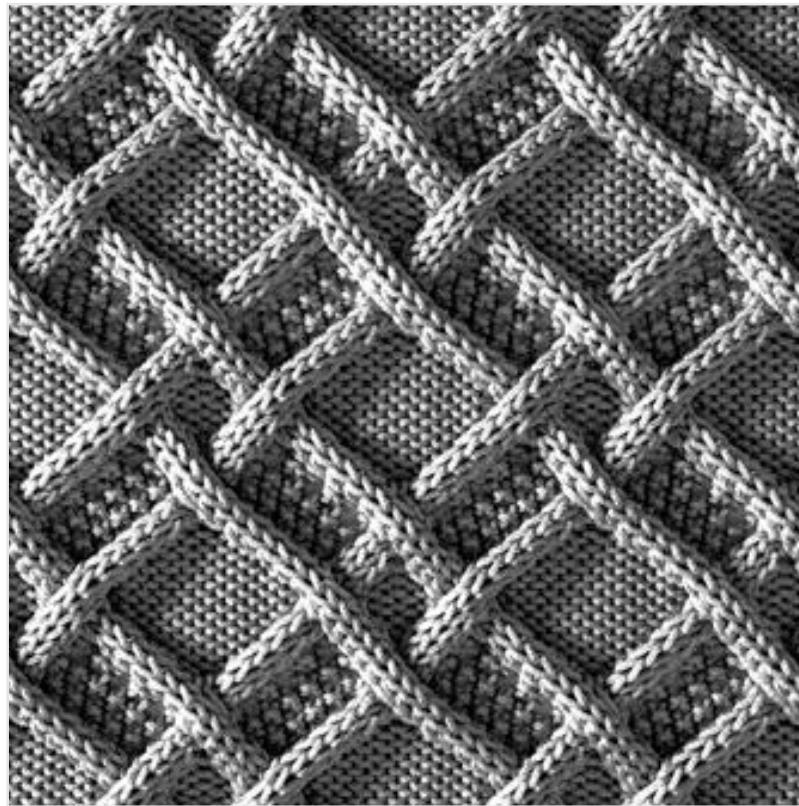
Stitch Mesh
Editing



Example Pattern [Yuksel et al. 2012]



Stitch Mesh



Final Result

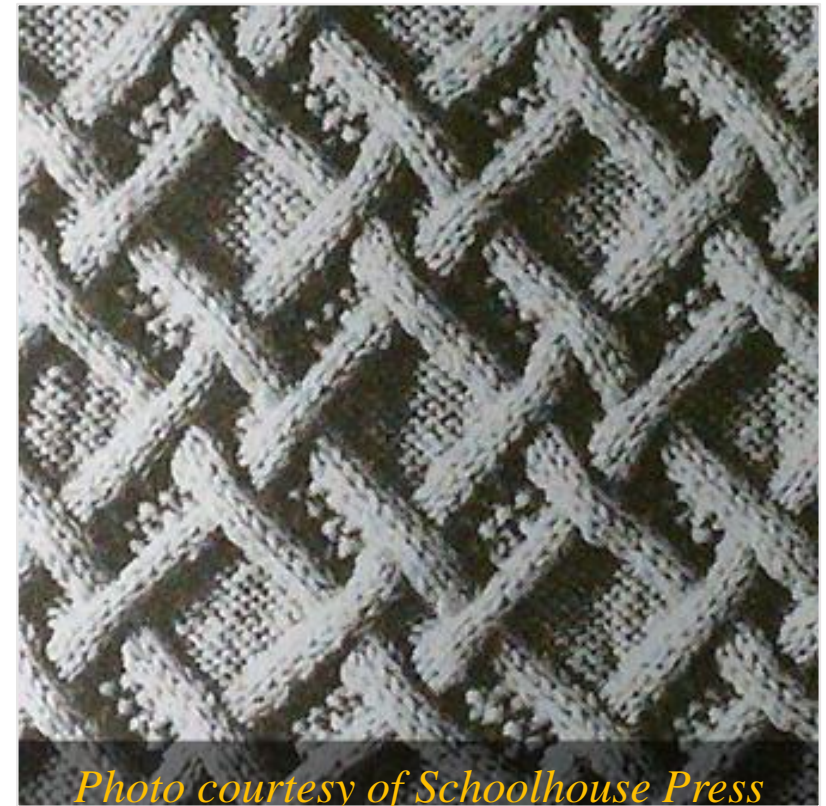
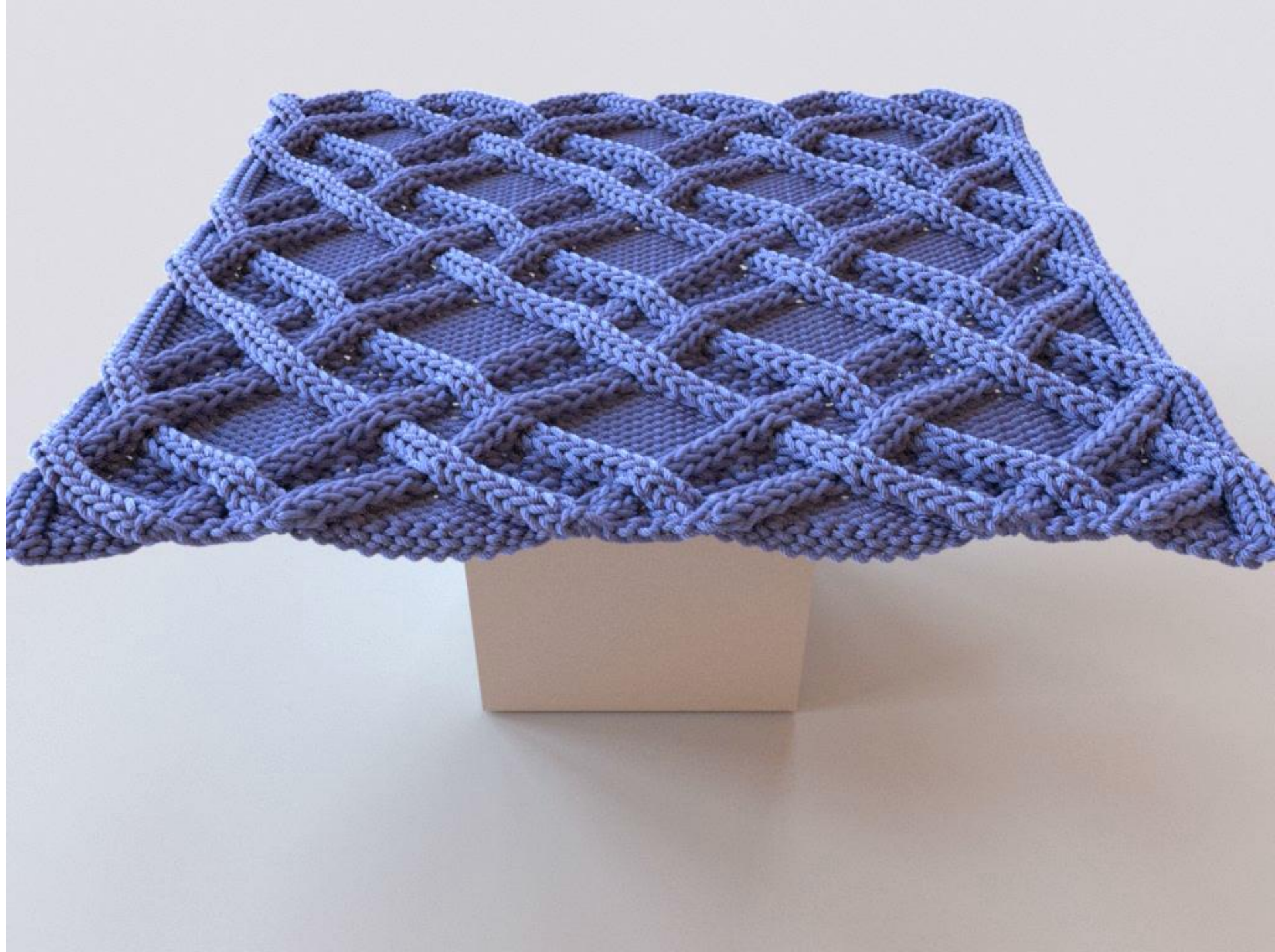


Photo Reference













Labeling the Input Mesh [Yuksel et al. 2012]



Stitch Meshes

Input low polygon mesh must be “labelable”



Input Mesh



Labeled Mesh



Stitch Mesh



Yarn-level Model

Stitch Meshes

Hours of modeling with many iterations



Input Mesh



Labeled Mesh



Stitch Mesh



Yarn-level Model

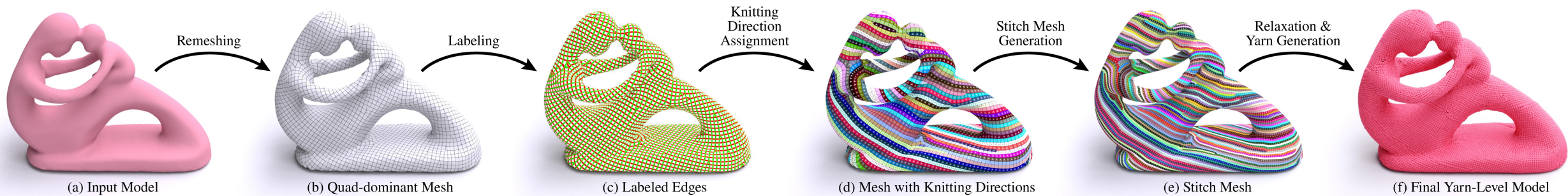
Problem

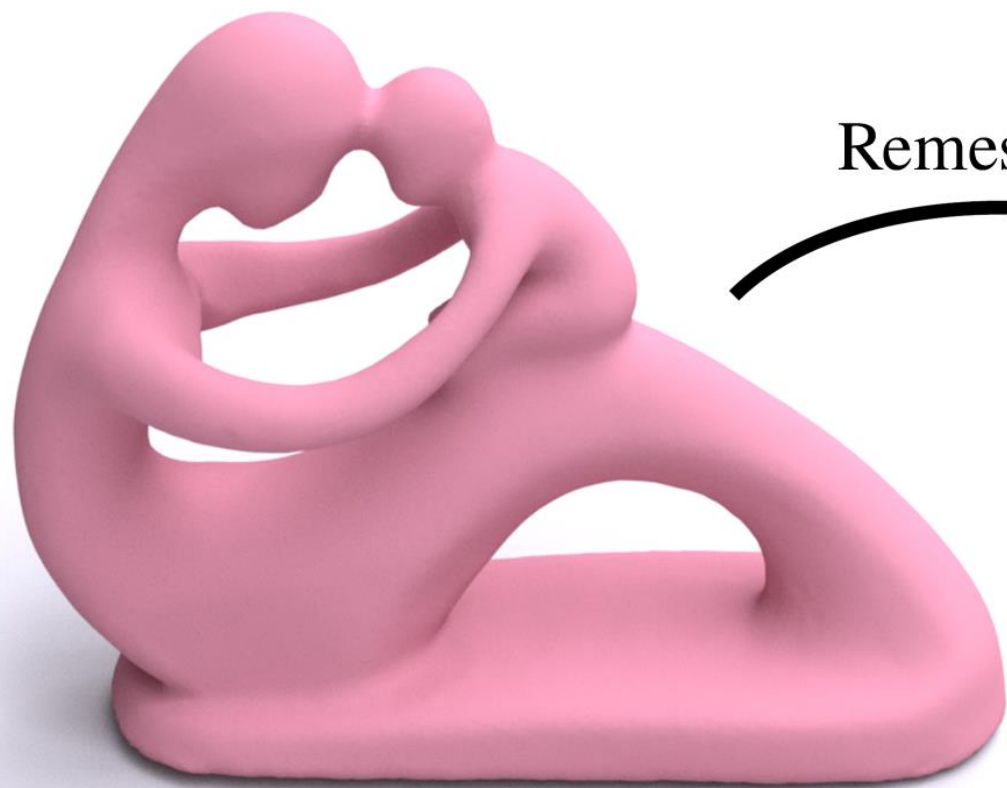
How to convert arbitrary mesh to stitch mesh for yarn-level modeling?



Our Method

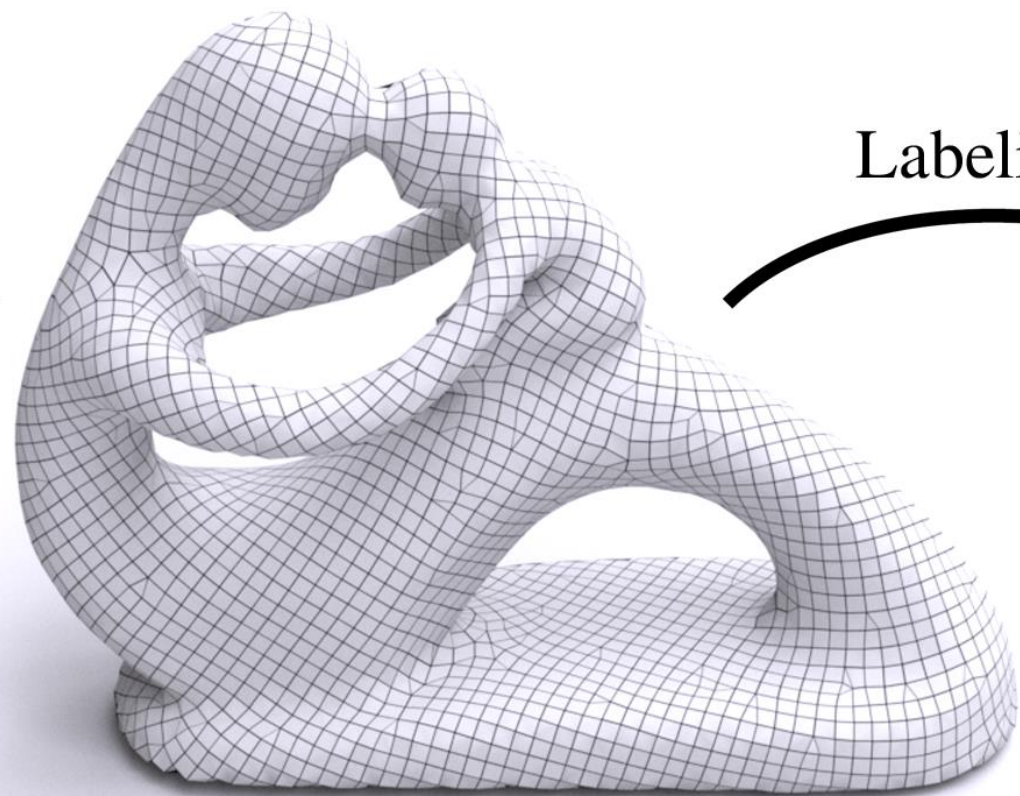
We introduce the first fully automatic pipeline to convert arbitrary 3D shapes into knit models.





(a) Input Model

Remeshing



(b) Quad-dominant Mesh

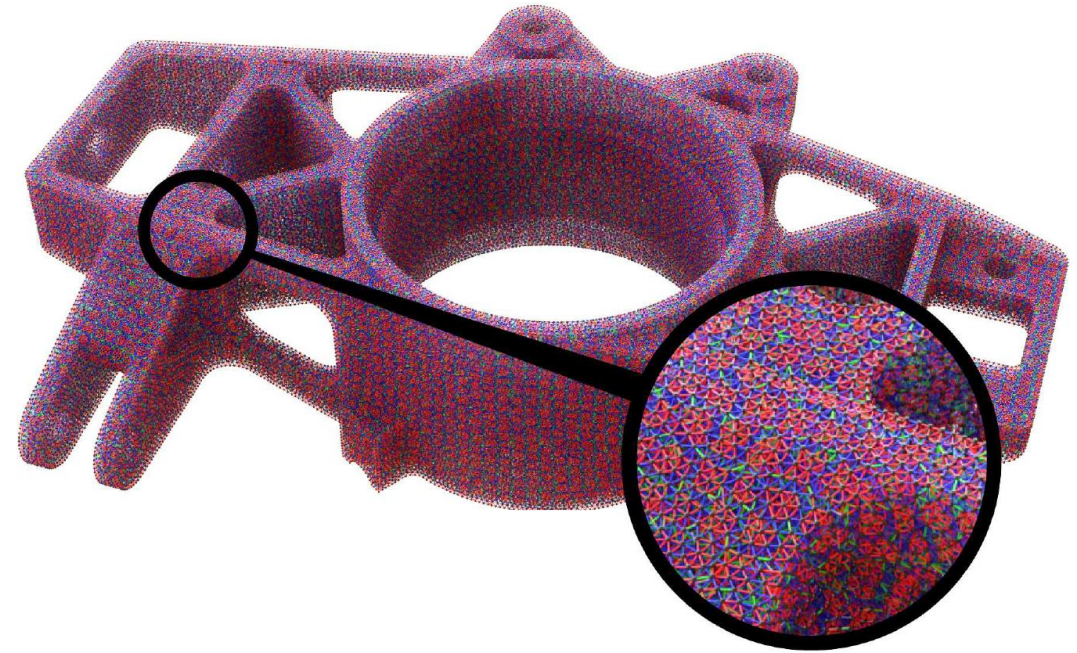
Labeling



Remeshing

We extend the robust quad-dominant meshing pipeline [Gao et al. 2017] to produce meshes

- Robust
- All face are similar size
- All angles are close to 90 degree

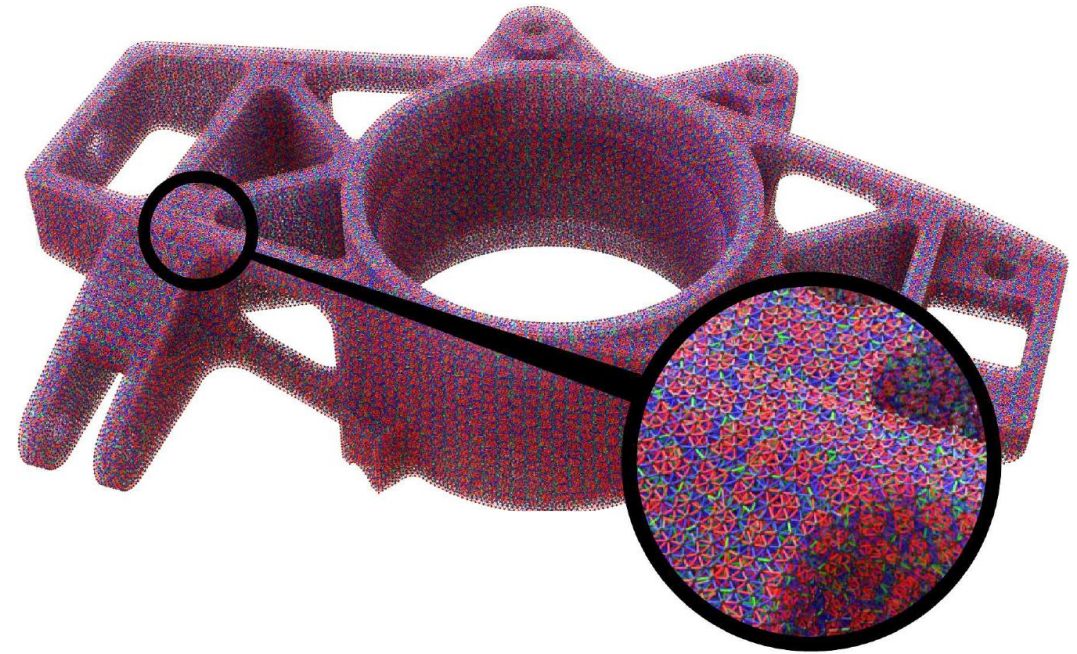


Robust Hex-Dominant Mesh Generation using Field-Guided Polyhedral Agglomeration
Xifeng Gao, Wenzel Jakob, Marco Tarini, Daniele Panozzo
ACM Transactions on Graphics (SIGGRAPH), 2017)

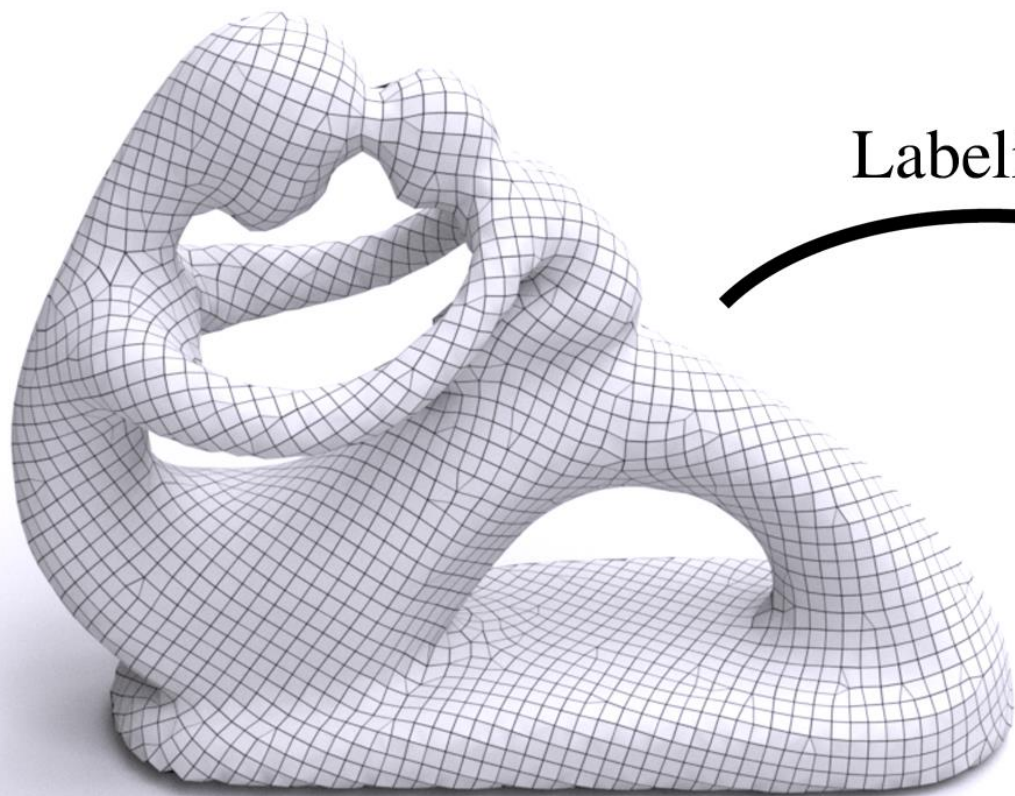
Remeshing

We extend the robust quad-dominant meshing pipeline [Gao et al. 2017] to produce meshes

- Robust
- All face are similar size
- All angles are close to 90 degree
 - Use 2-RoSy (two-fold rotational symmetry) field
 - Cut each polygon with more than 5 sides by adding the edge that is most aligned with the orientation field

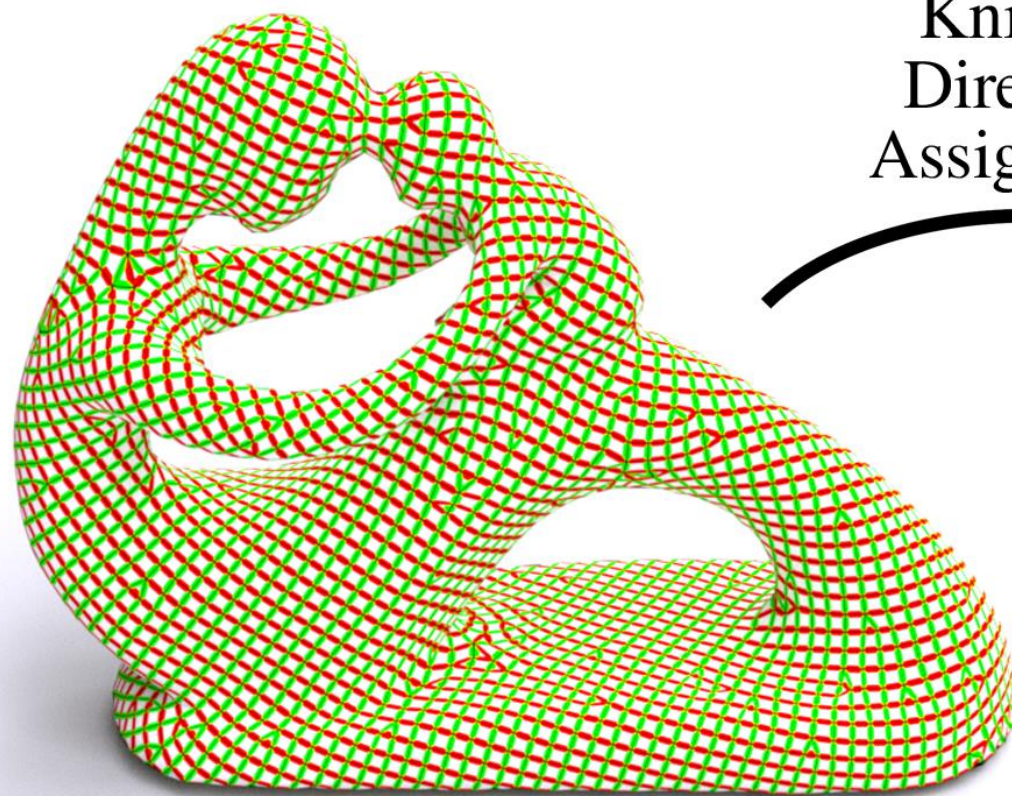


[Gao et al. 2017]



(b) Quad-dominant Mesh

Labeling

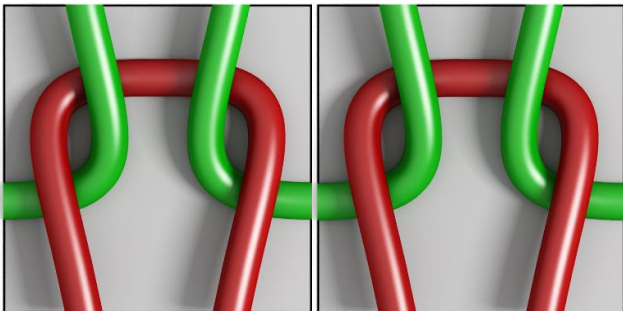
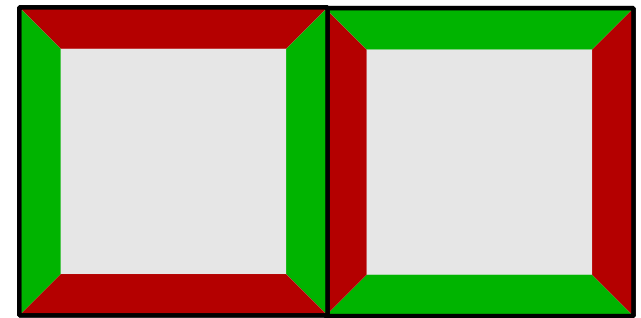
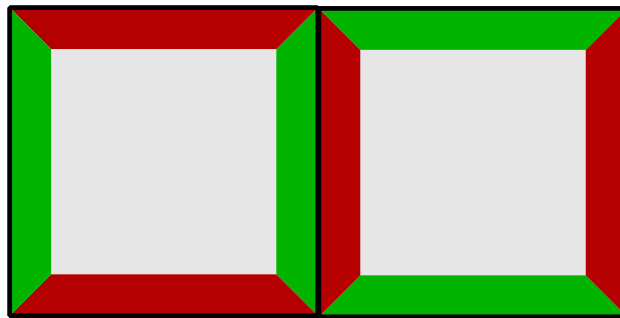
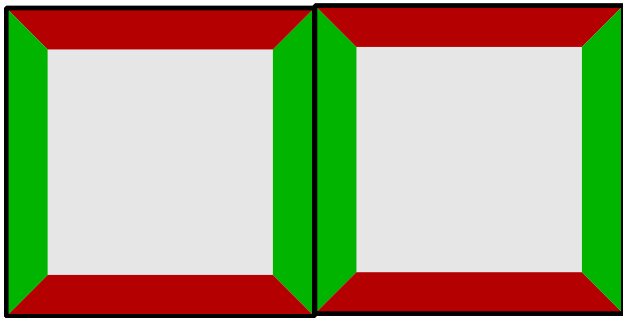


(c) Labeled Edges

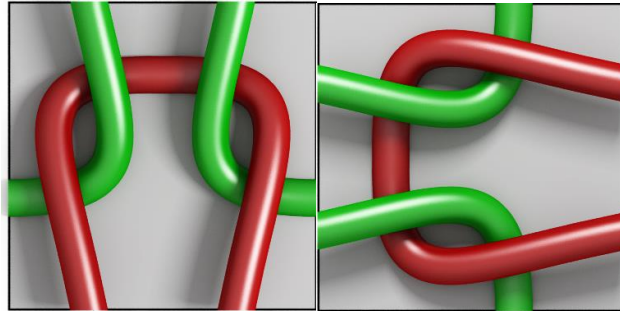
Knitting
Direction
Assignment

Labeling

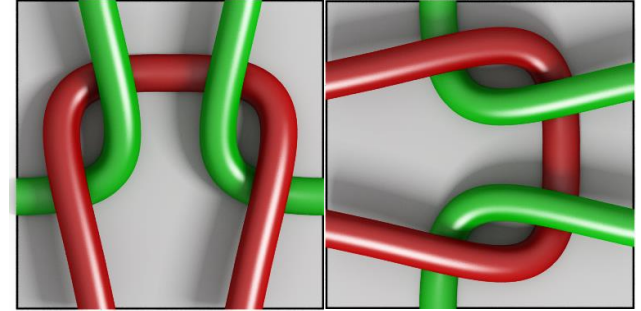
We use half-edge data structure for labeling



no conflicting 😊



conflicting (1) 😞



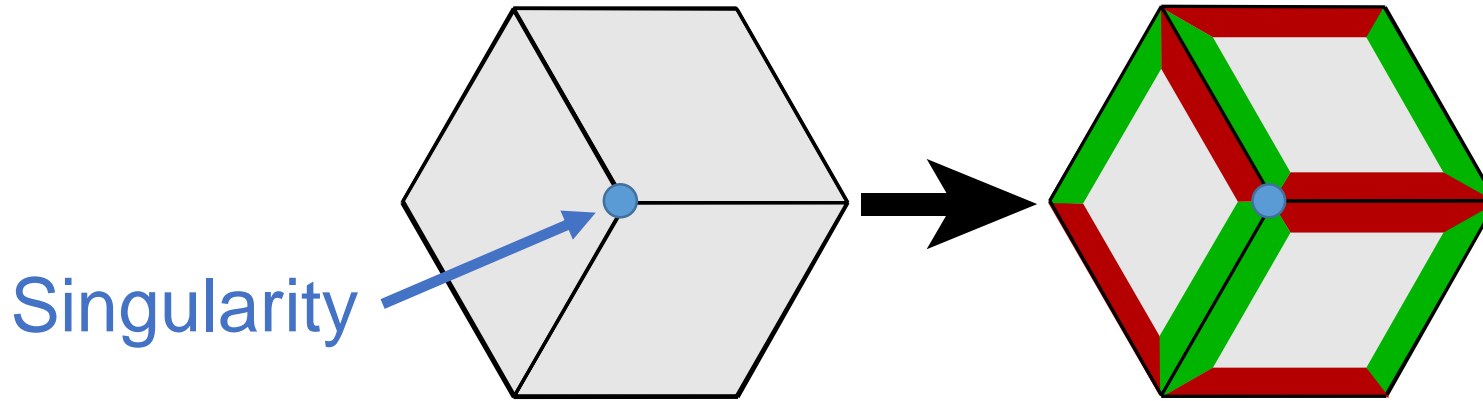
conflicting (2) 😞

Labeling

1. Preprocess
 - Triangulation near singularities
2. Minimize conflicting by solving Mixed-integer Programming (MIP) problem
3. Postprocess
 - solving conflicts
 - merging triangles

Labeling

Preprocess

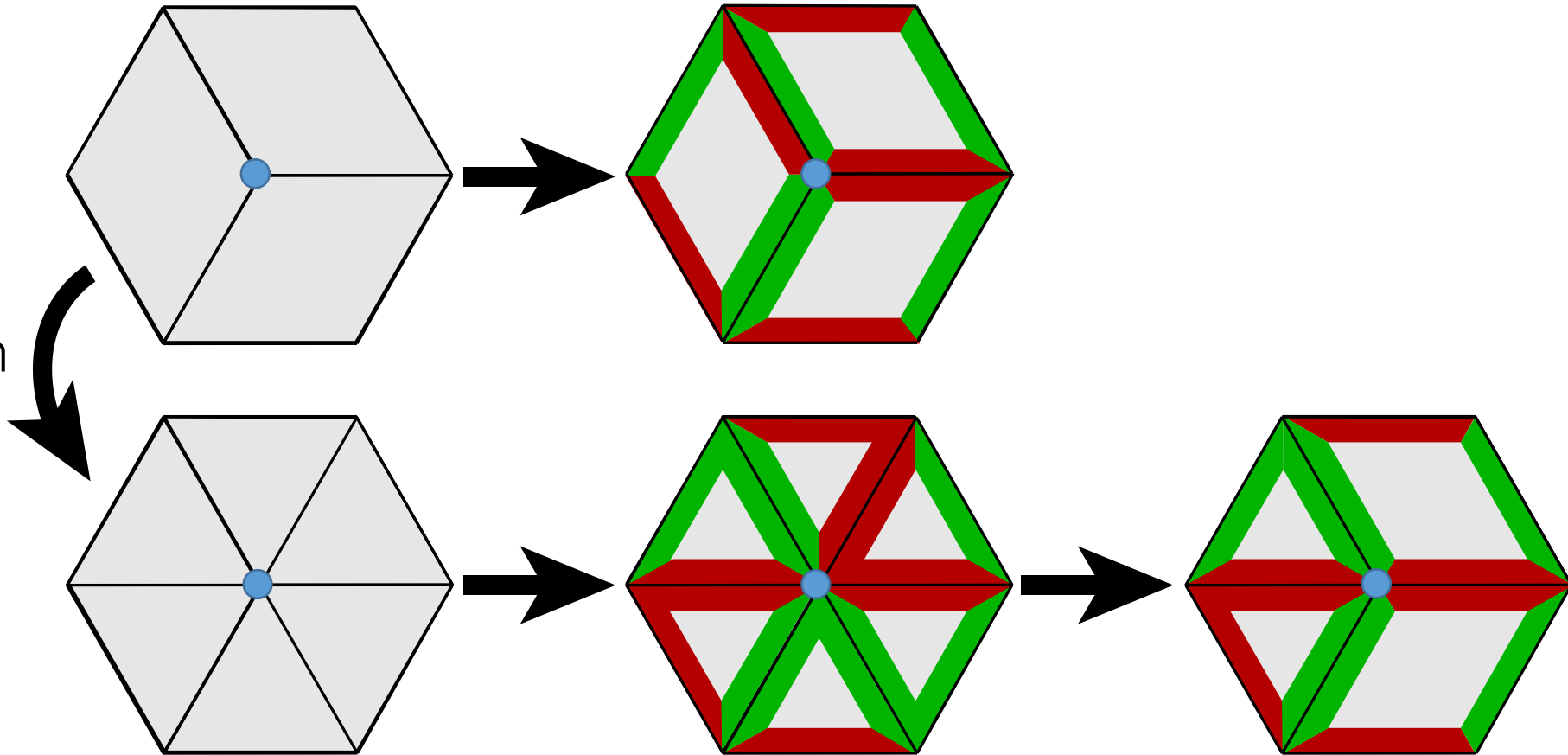


Conflicting is unavoidable

Labeling

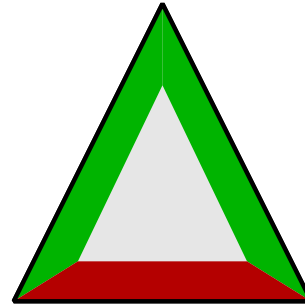
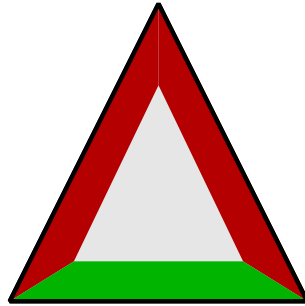
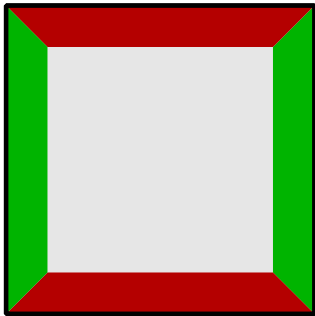
Preprocess

Triangulation



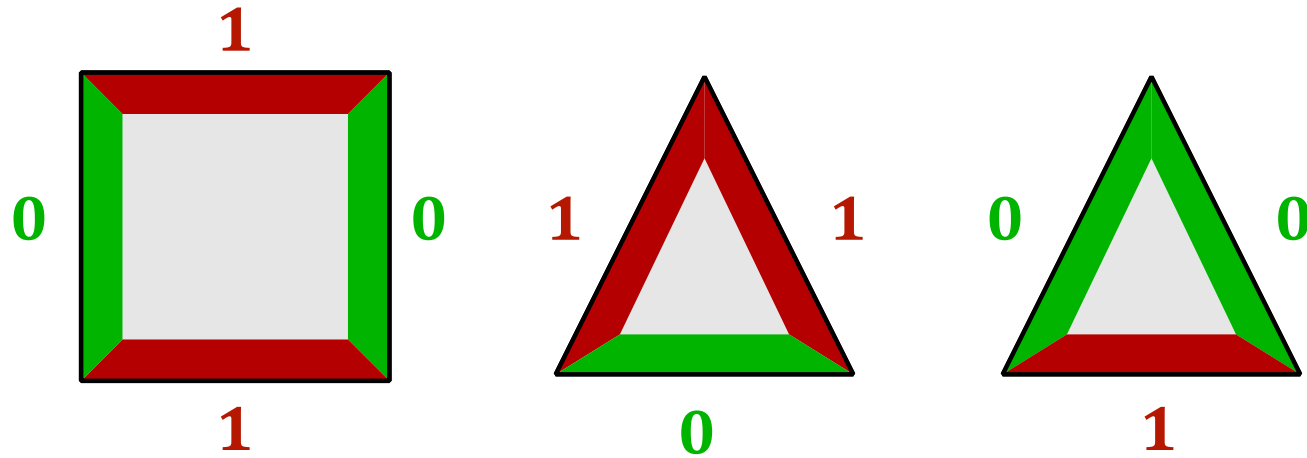
Labeling

Three valid half-edge configurations



Labeling

Three valid half-edge configurations

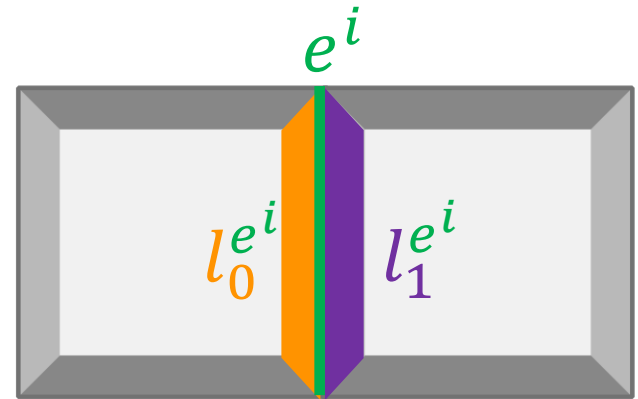


1 - course edge
0 - wale edge

Labeling

Mixed-integer Programming problem

$$\begin{aligned} \text{minimize} \quad & \sum_{i=0}^{n-1} (\ell_0^{e^i} - \ell_1^{e^i})^2 \\ & \ell_0^{e^i}, \ell_1^{e^i} \in \{0, 1\} \end{aligned}$$



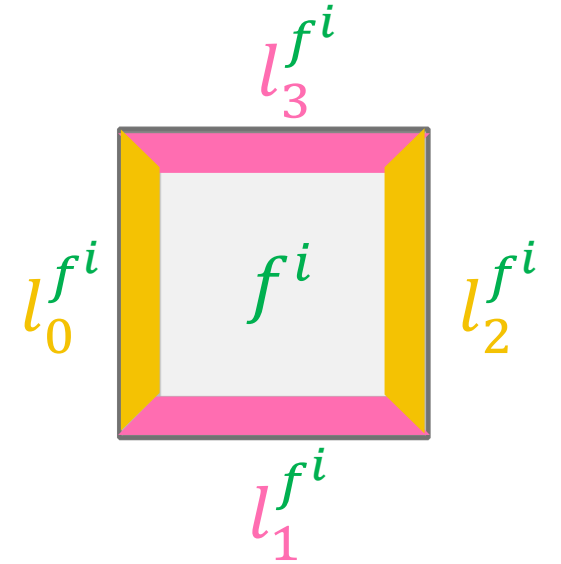
Labeling

Mixed-integer Programming problem

$$\begin{array}{ll} \text{minimize} & \sum_{i=0}^{n-1} (\ell_0^{e_i} - \ell_1^{e_i})^2 \\ \text{subject to} & \end{array}$$

for each quad face f_j ,

$$\ell_0^{f_j} = \ell_2^{f_j}, \quad \ell_1^{f_j} = \ell_3^{f_j}, \quad \ell_0^{f_j} \neq \ell_1^{f_j}$$
$$\ell_k^{f_j} \in \{0, 1\}, \quad k = 0, 1, 2, 3$$



Labeling

Mixed-integer Programming problem

$$\text{minimize } \sum_{i=0}^{n-1} (\ell_0^{e_i} - \ell_1^{e_i})^2$$

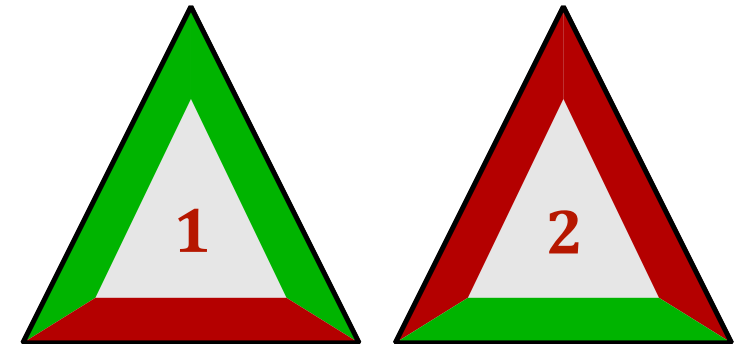
subject to

$$\text{for each quad face } f_j, \quad \ell_0^{f_j} = \ell_2^{f_j}, \quad \ell_1^{f_j} = \ell_3^{f_j}, \quad \ell_0^{f_j} \neq \ell_1^{f_j}$$

$$\ell_k^{f_j} \in \{0, 1\}, \quad k = 0, 1, 2, 3$$

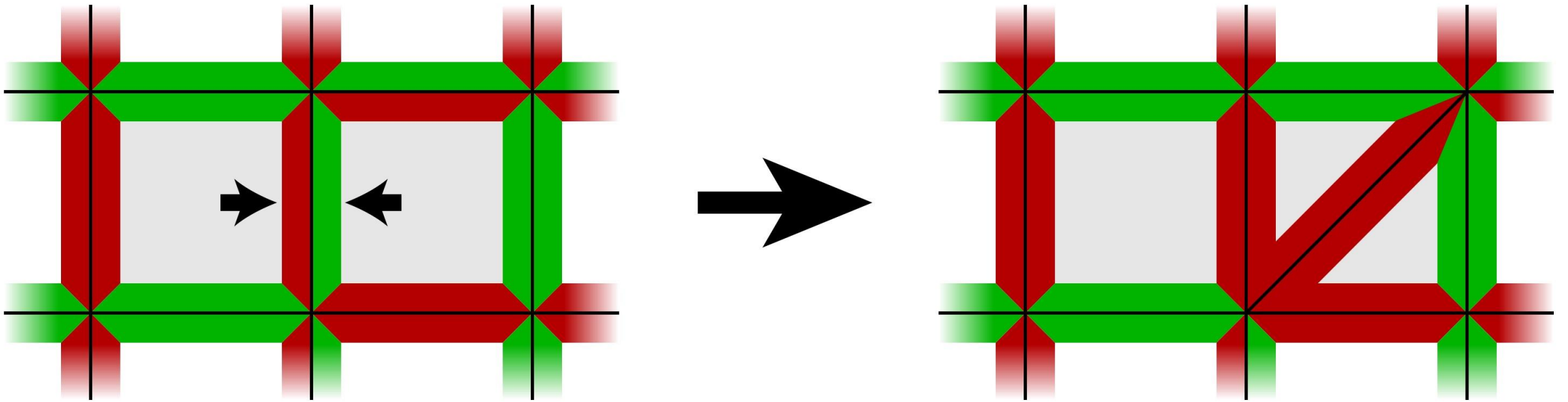
$$\text{for each triangle face } f_j, \quad \mathbf{1} \leq \ell_0^{f_j} + \ell_1^{f_j} + \ell_2^{f_j} \leq \mathbf{2}$$

$$\ell_k^{f_j} \in \{0, 1\}, \quad k = 0, 1, 2$$



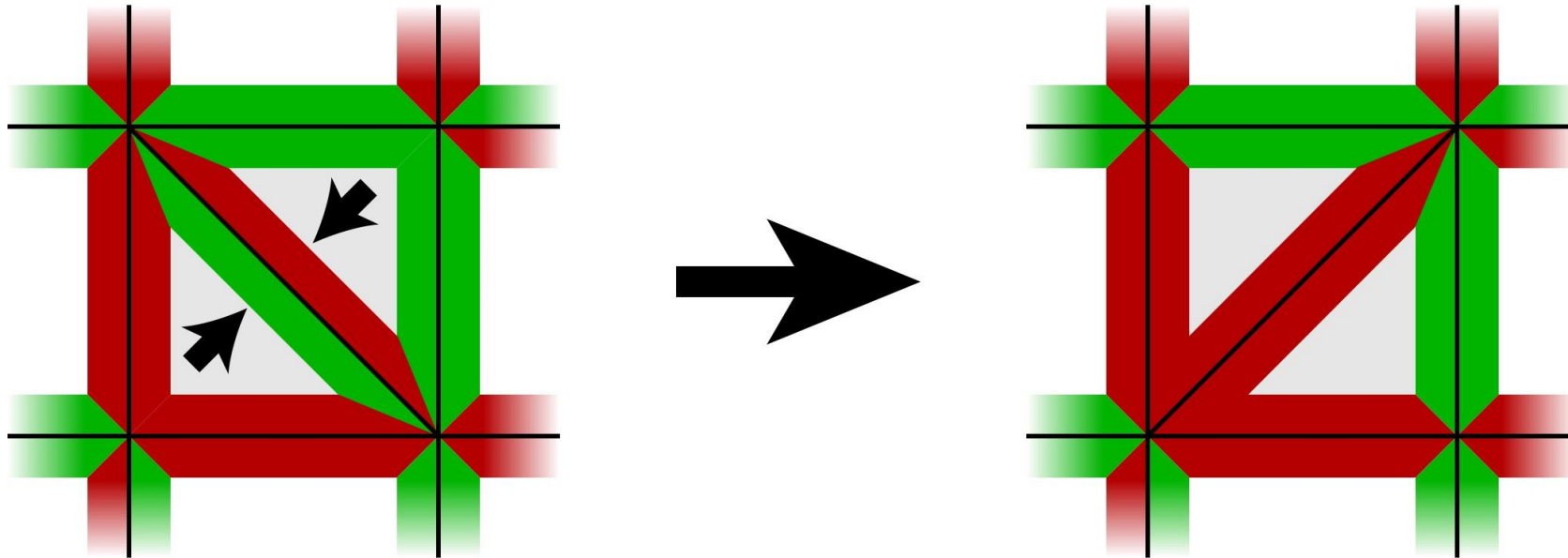
Labeling

Postprocess – face splitting



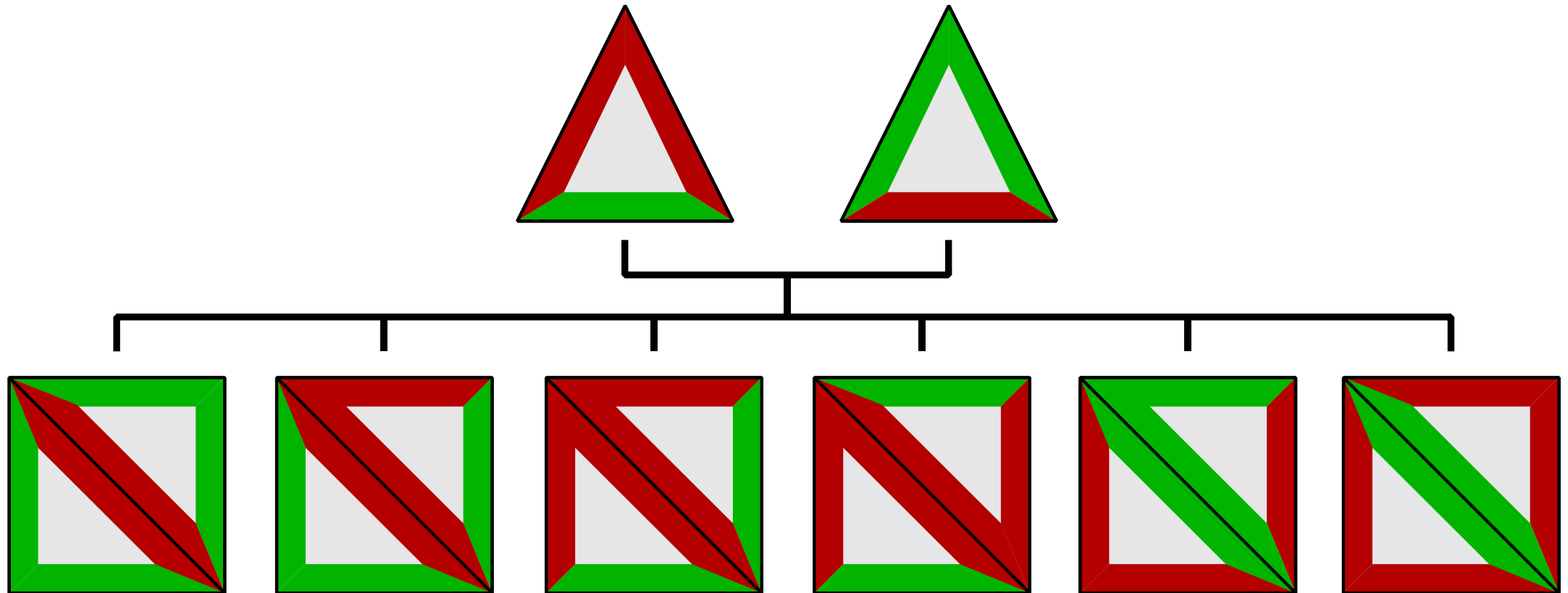
Labeling

Postprocess – edge rotation



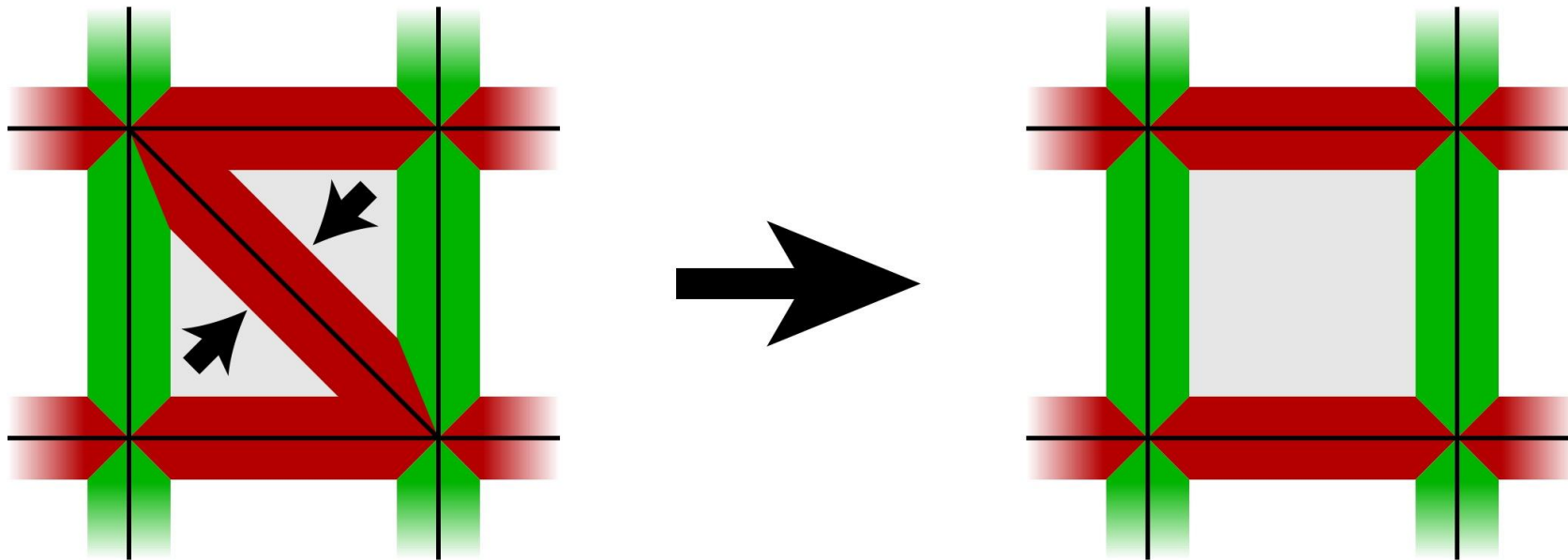
Labeling

Any type of quads can be represented by two triangles



Labeling

Postprocess – triangles merging



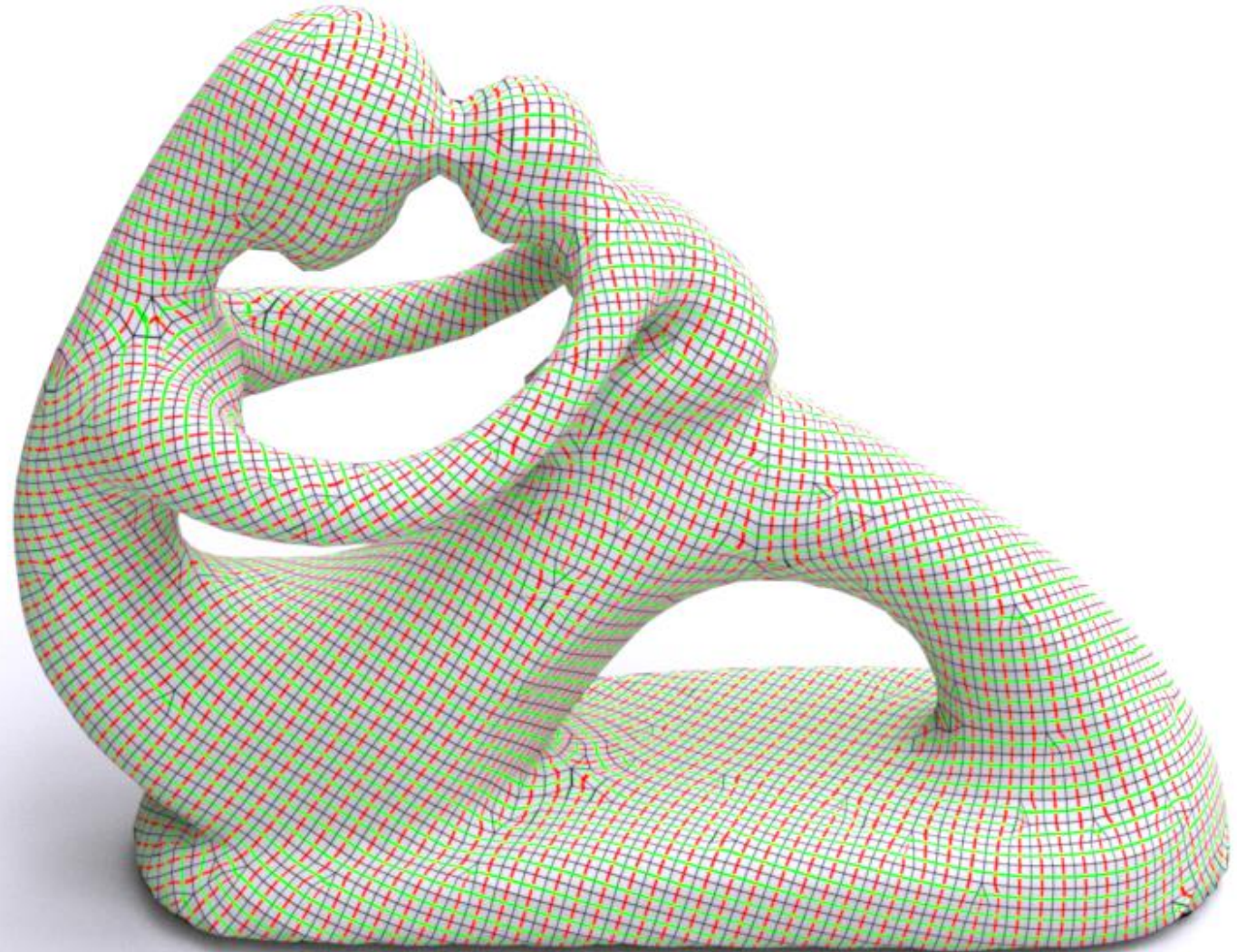
Labeling

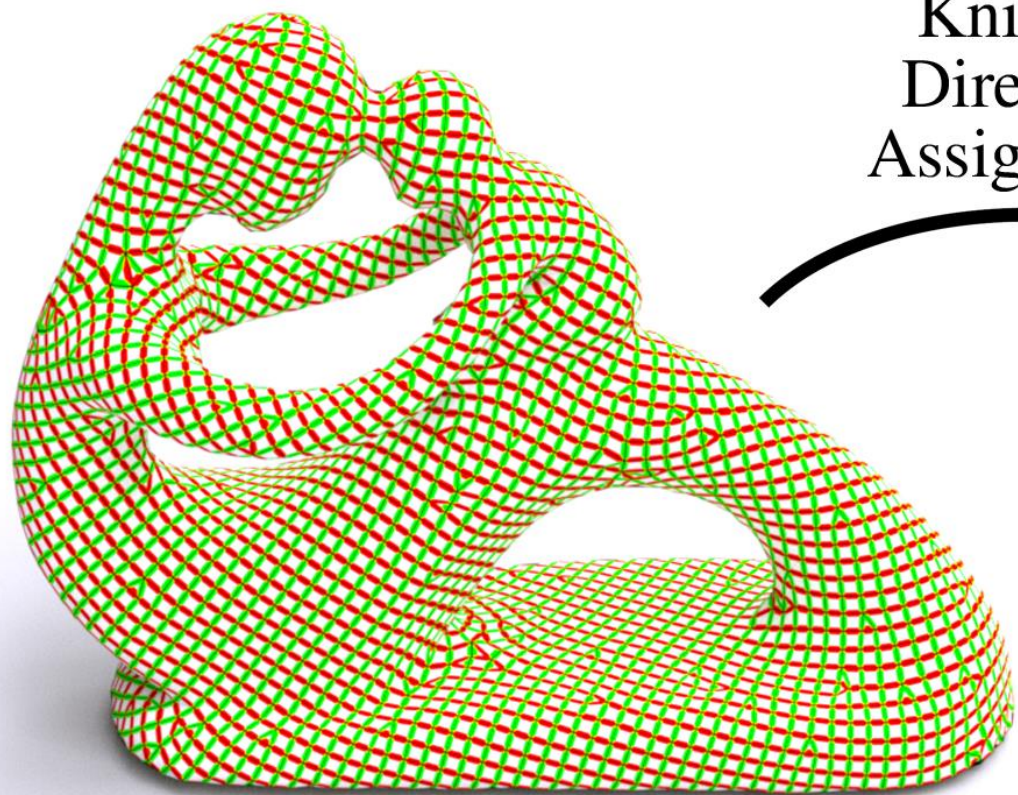
Topology

- No conflicting

Geometry

- All faces have approximately the same size
- All angles are close to 90 degree





(c) Labeled Edges

Knitting
Direction
Assignment

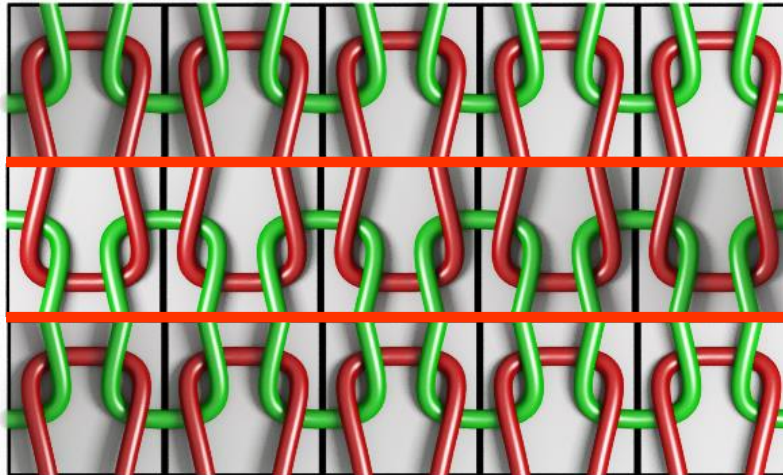
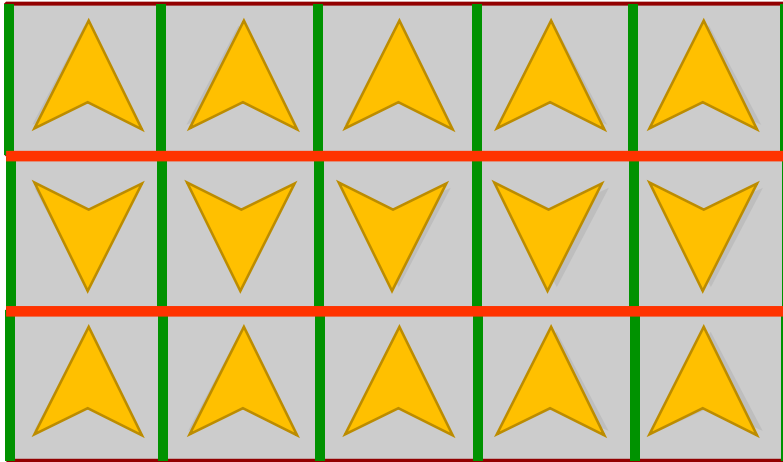


Stitch M
Genera



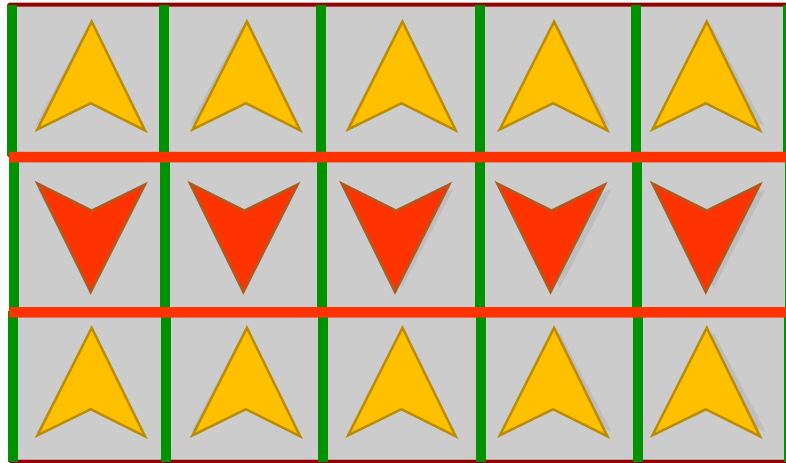
(d) Mesh with Knitting Directions

Knitting Direction Assignment

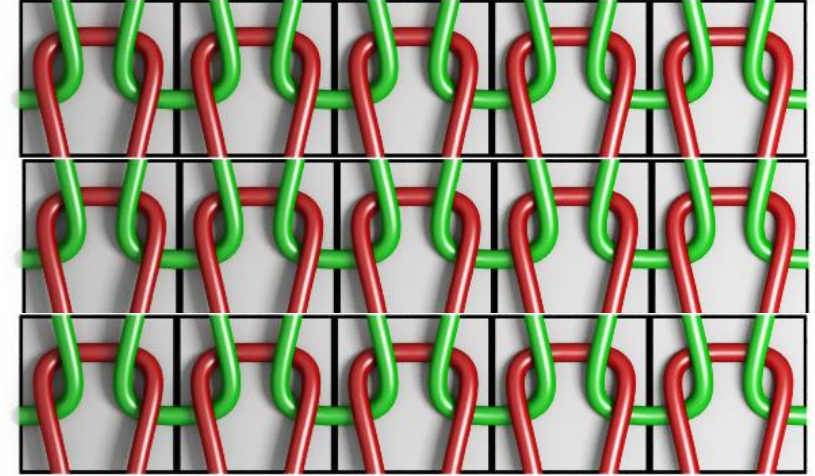
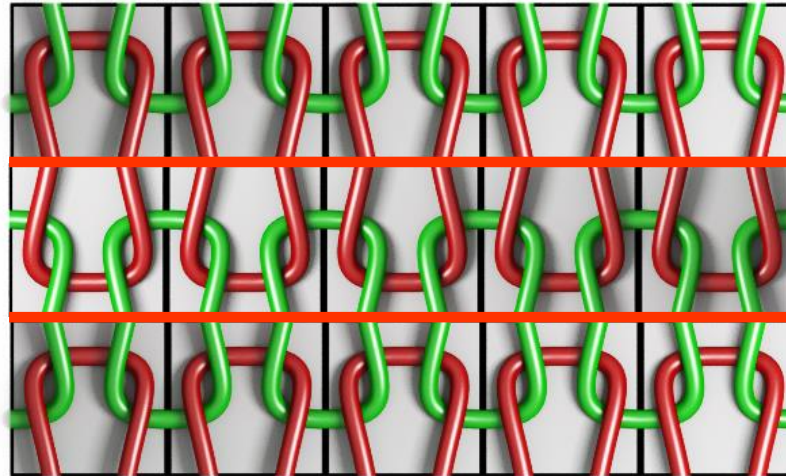
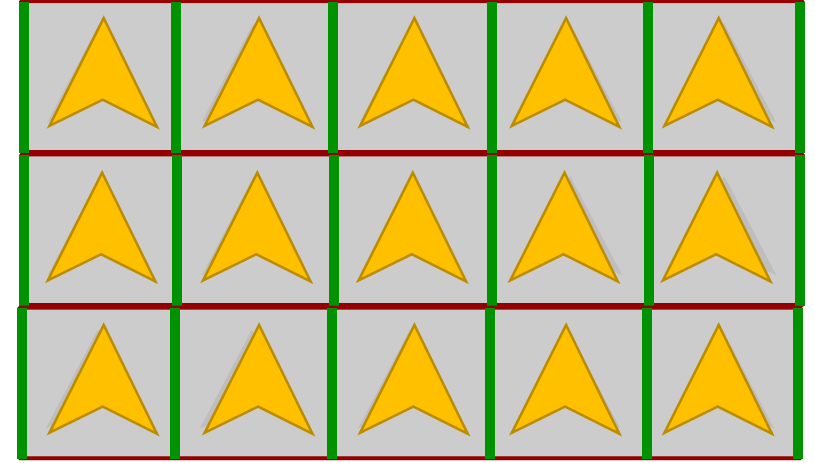


Knitting direction mismatch

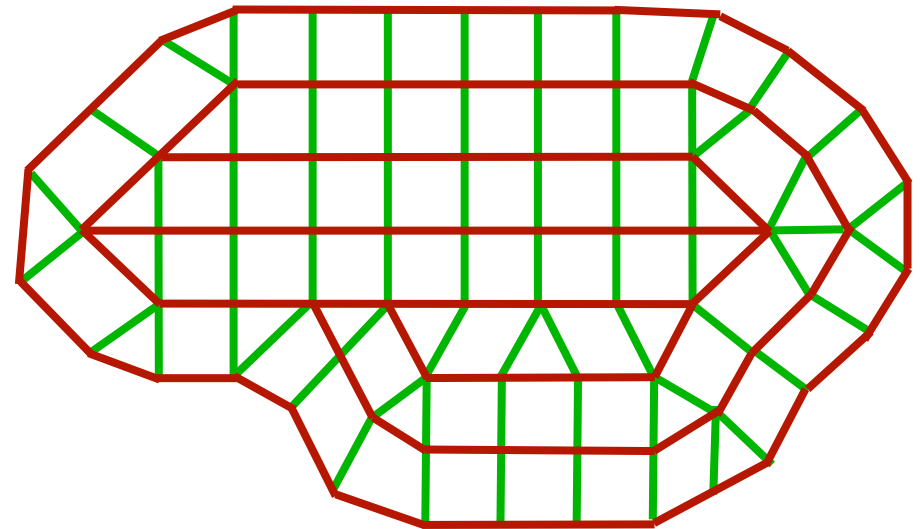
Knitting Direction Assignment



after
assignment

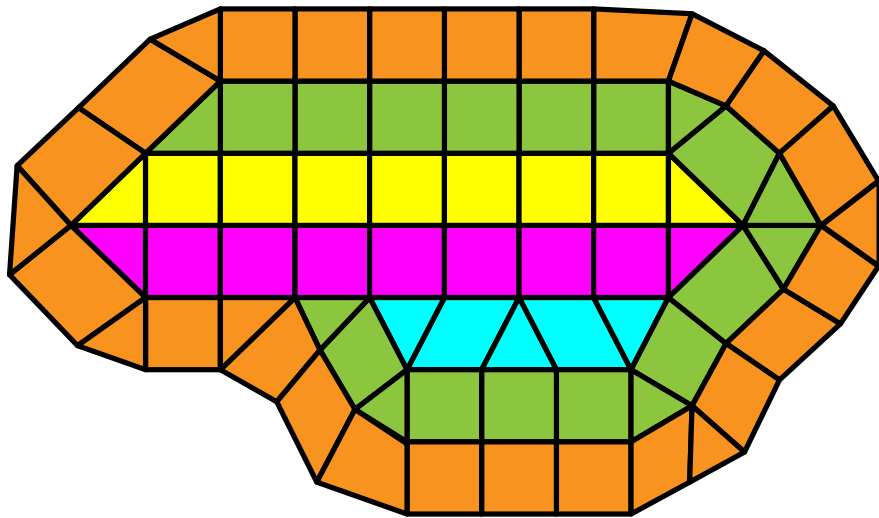


Knitting Direction Assignment

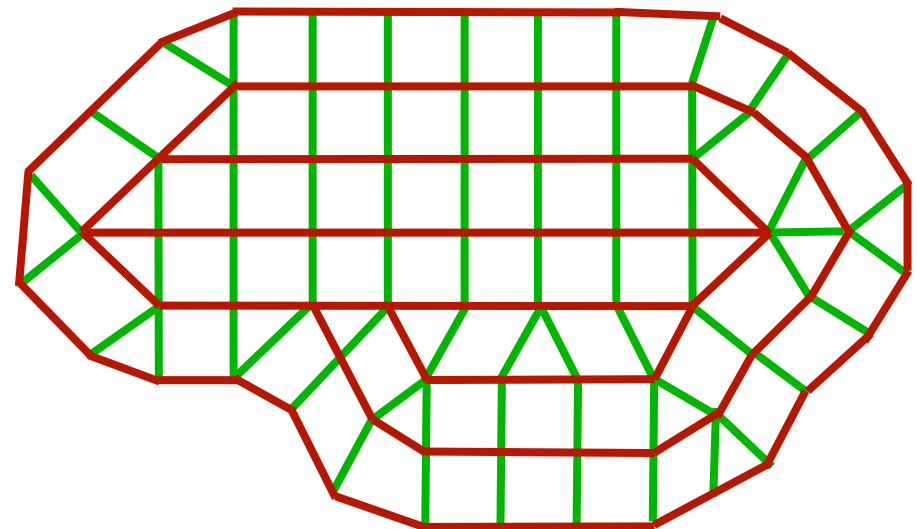


Knitting Direction Assignment

1. group faces by wale edges to form rows
2. build a meta-graph
3. minimizes the number of course edges with mismatched wale directions

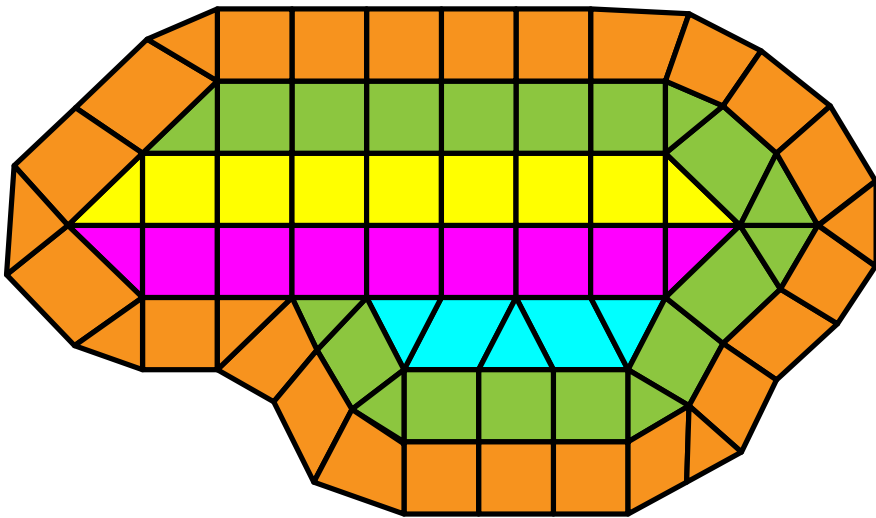


Grouped Stitch Mesh

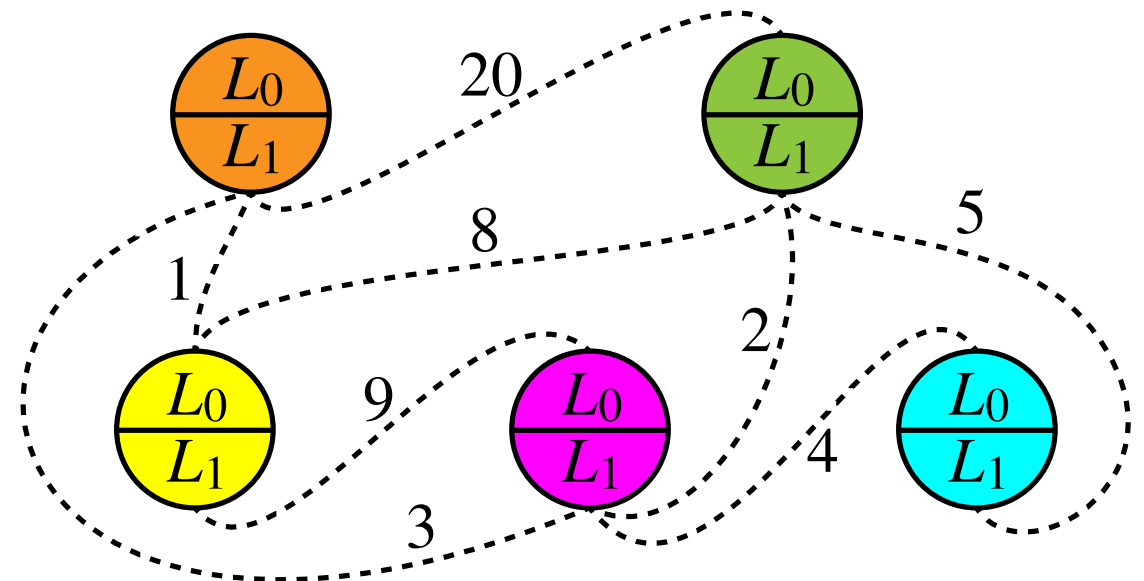


Knitting Direction Assignment

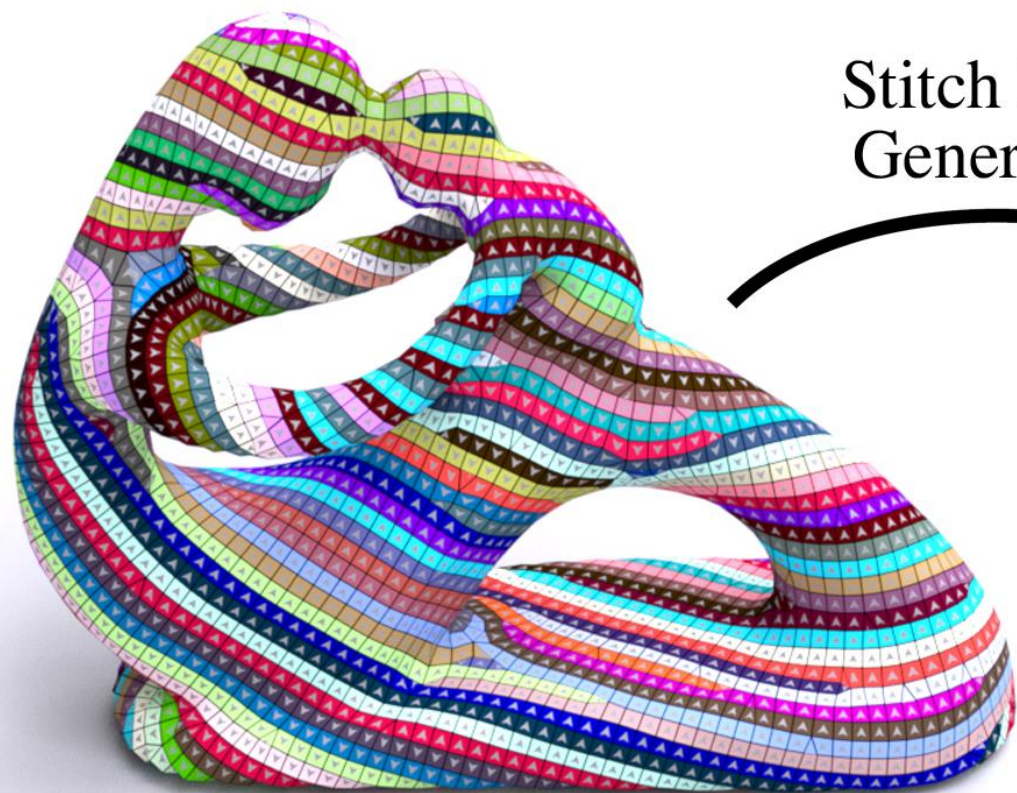
1. group faces by wale edges to form rows
2. build a meta-graph
3. minimizes the number of course edges with mismatched wale directions



Grouped Stitch Mesh

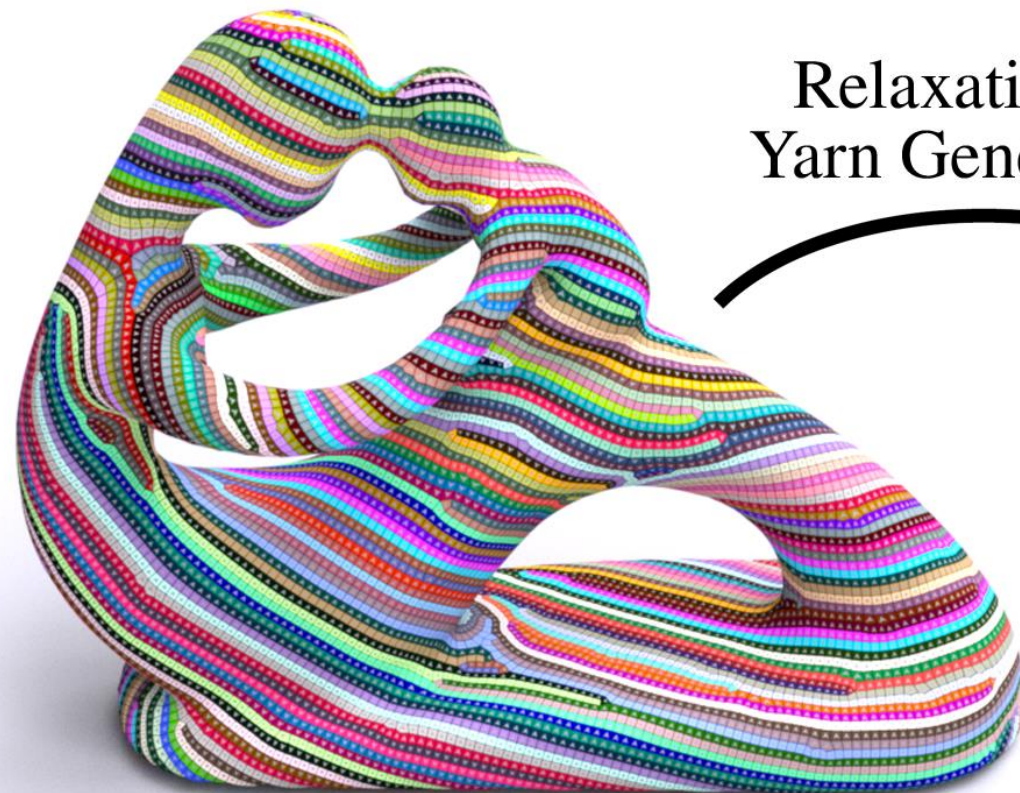


Meta-graph



(d) Mesh with Knitting Directions

Stitch Mesh
Generation



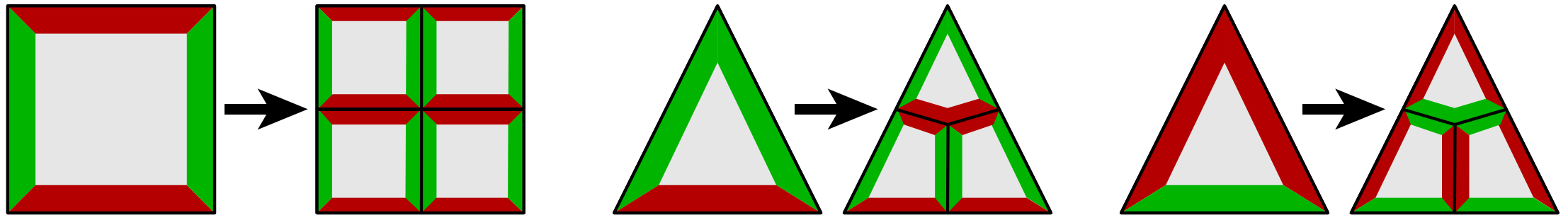
(e) Stitch Mesh

Relaxation &
Yarn Generation



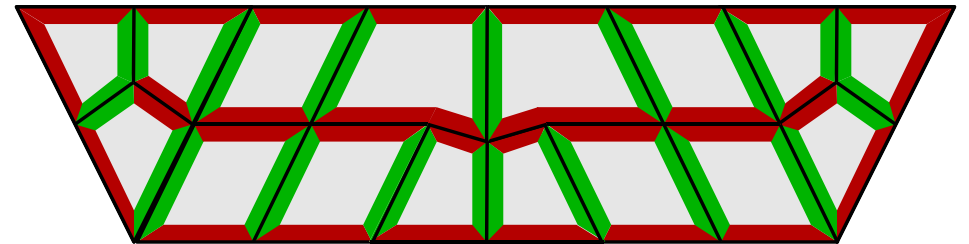
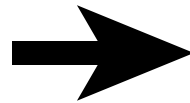
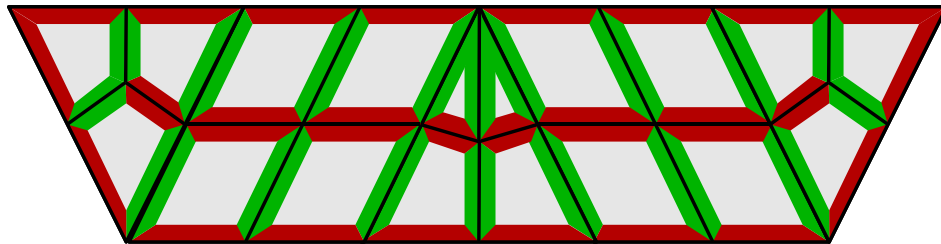
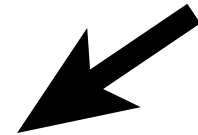
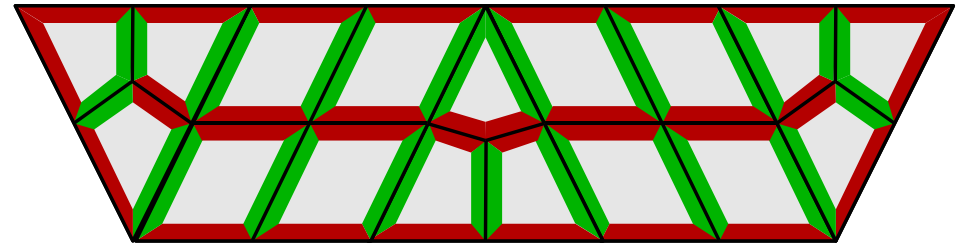
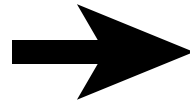
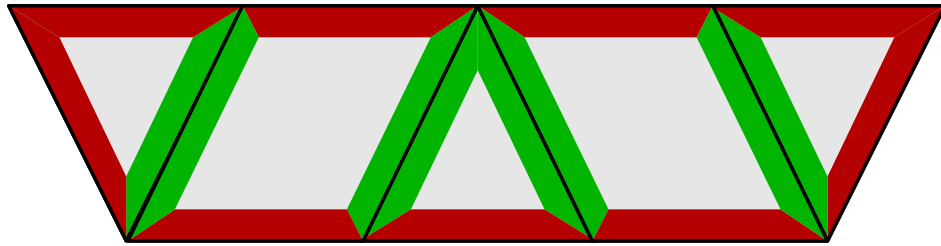
Stitch Mesh Generation

Subdivide mesh to stitch mesh



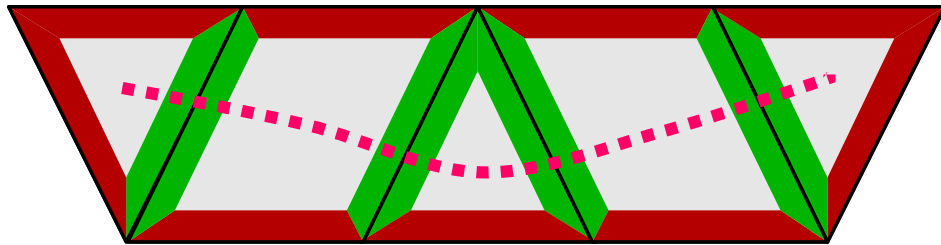
Stitch Mesh Generation

Subdivide mesh to stitch mesh

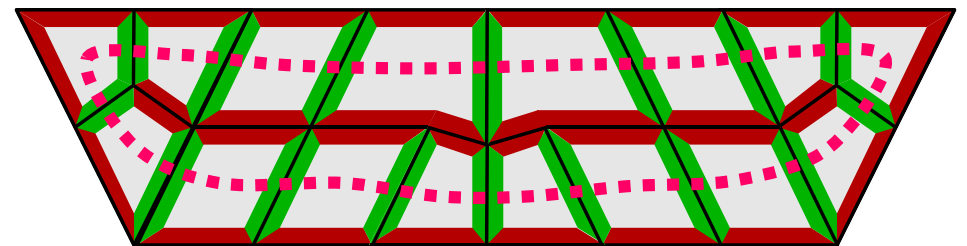
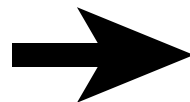
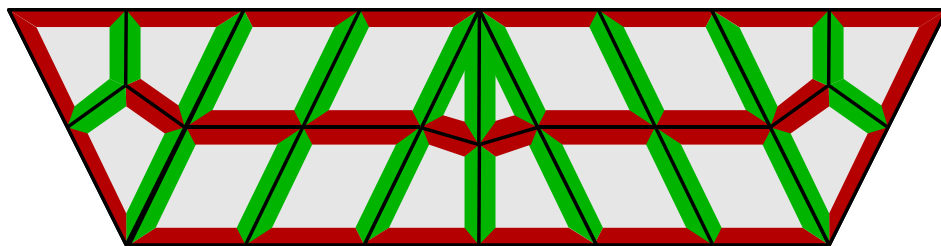
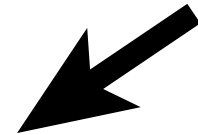
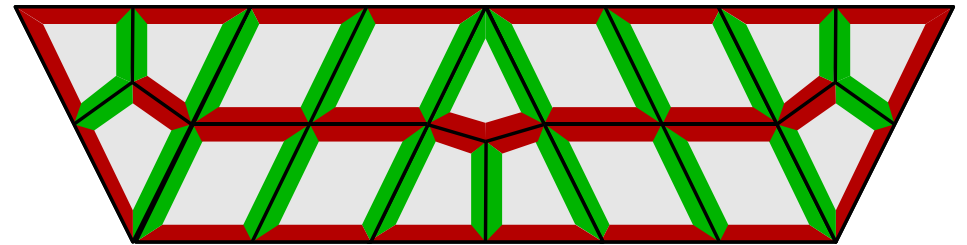
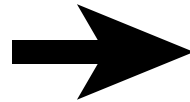


Stitch Mesh Generation

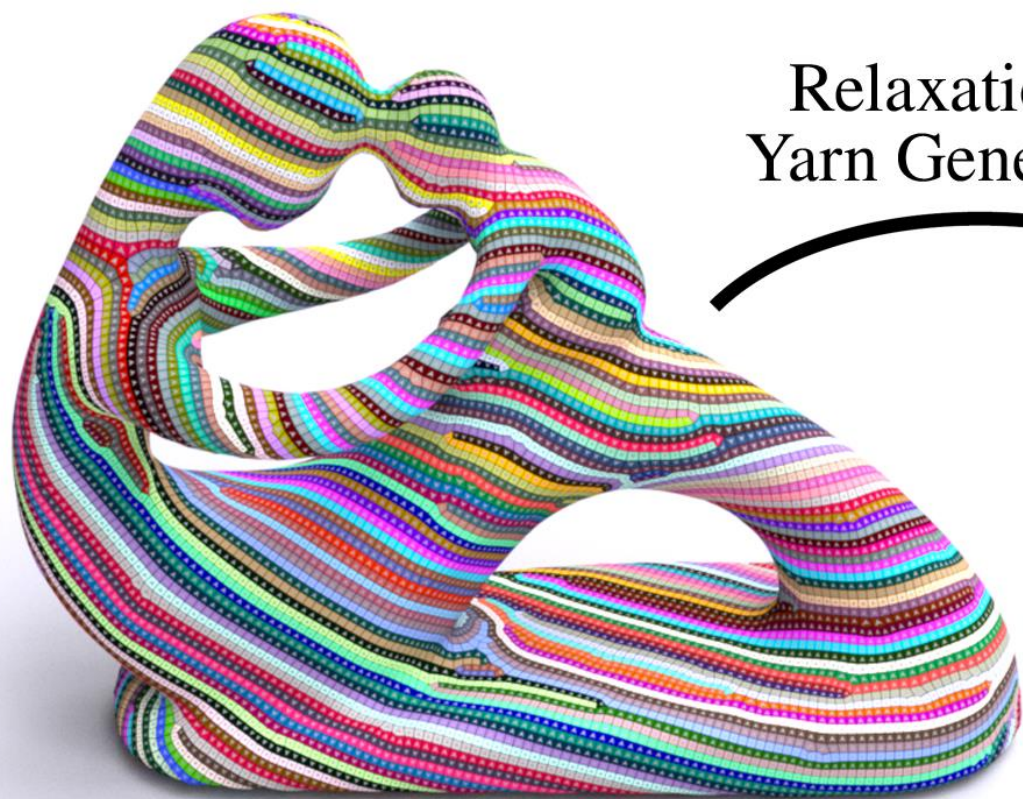
Subdivide mesh to stitch mesh



Open Yarn Loop



Closed Yarn Loop



(e) Stitch Mesh

Relaxation &
Yarn Generation



(f) Final Yarn-Level Model

Yarn Generation

Replace stitch mesh face with corresponding yarn loop topology



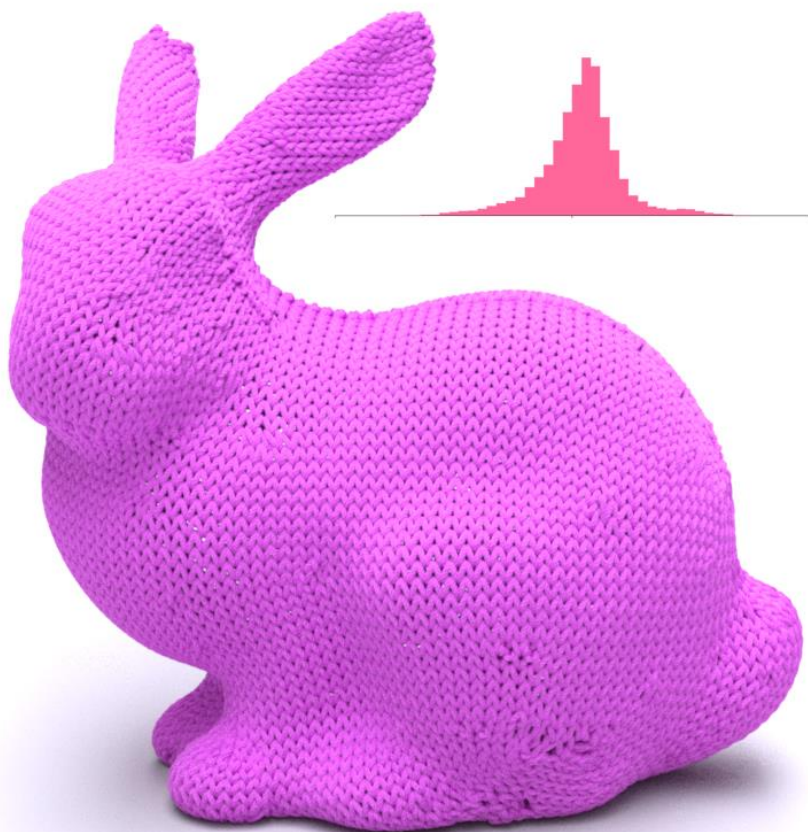
Results

Results



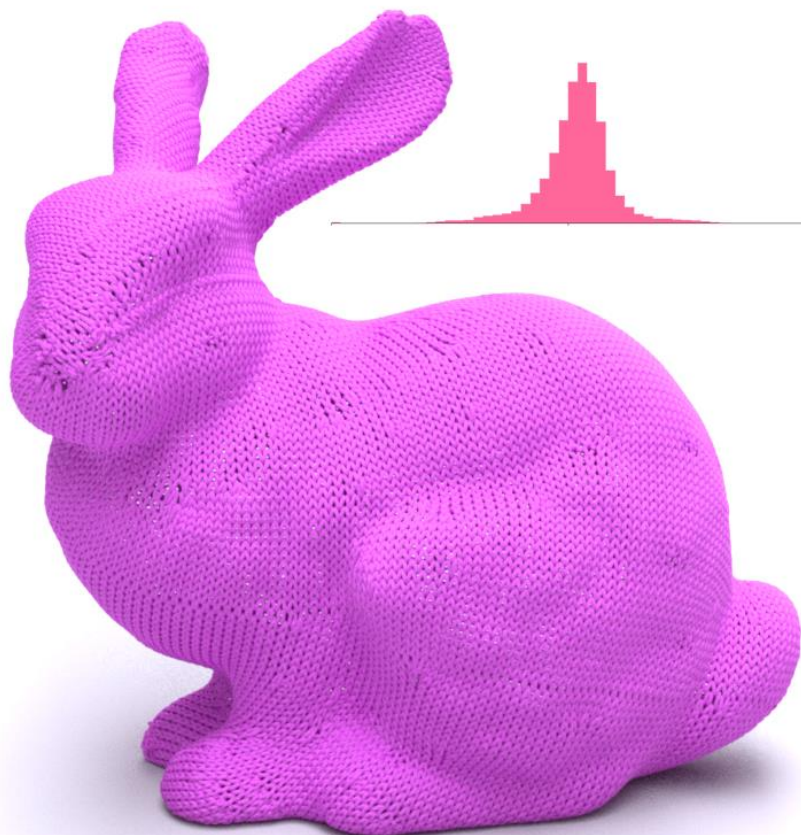
Results

STD 0.22



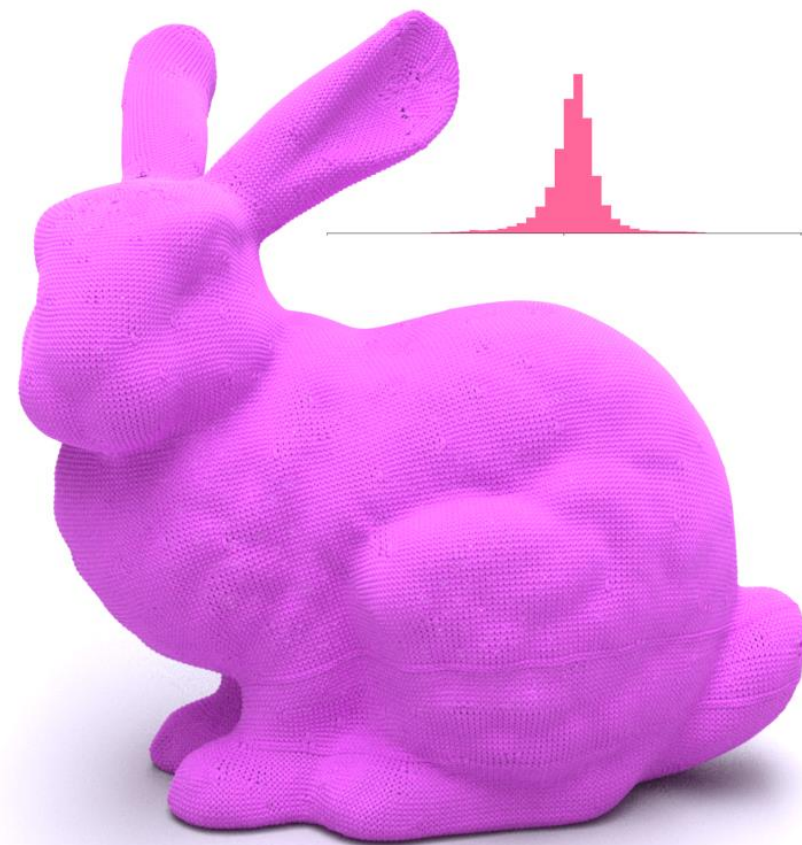
7K

STD 0.13



16K

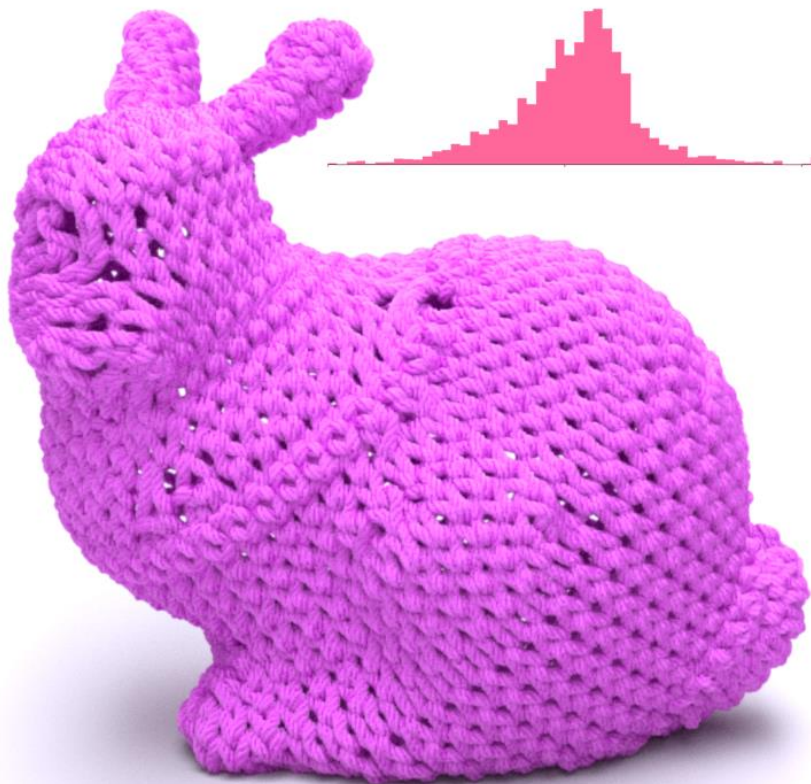
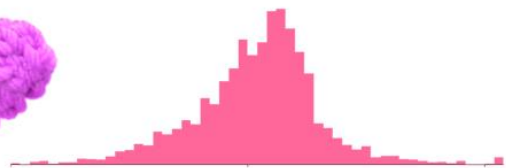
STD 0.06



48K

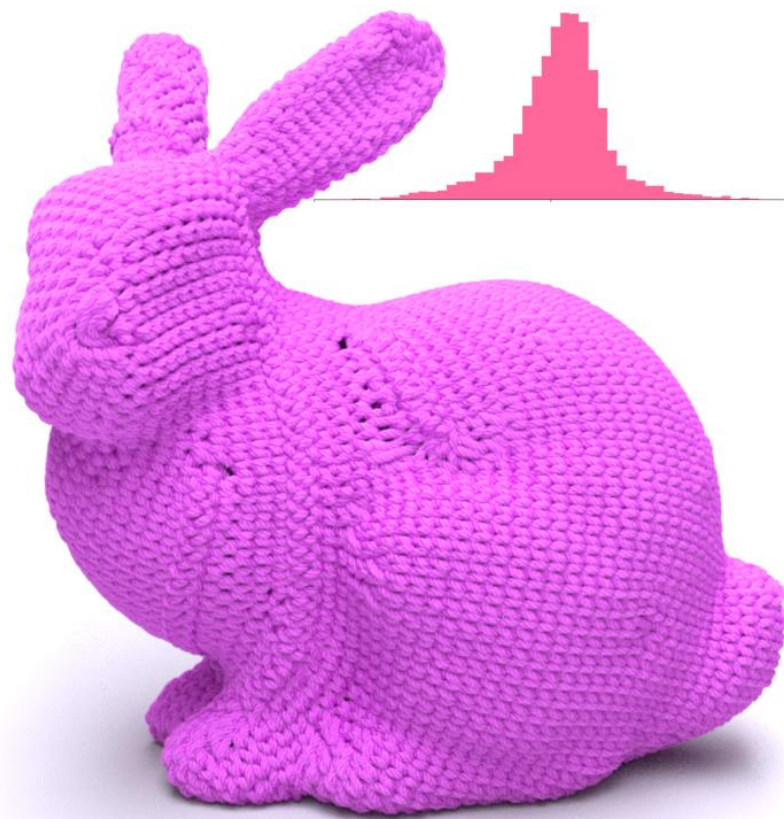
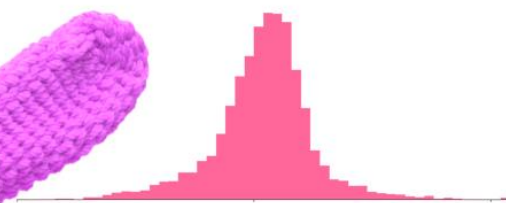
Results

STD 0.77



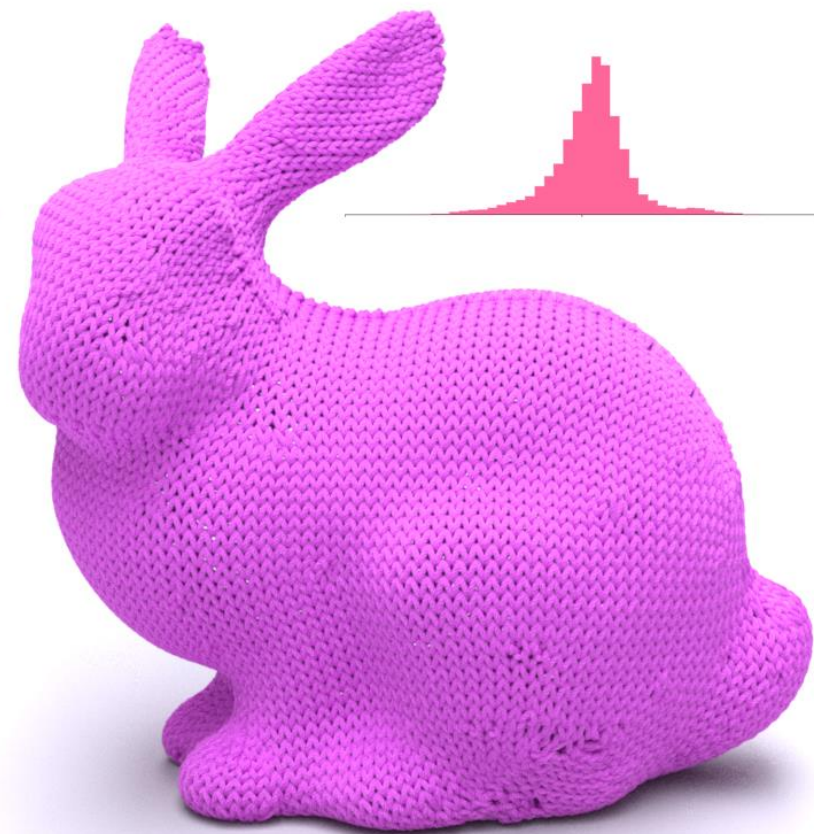
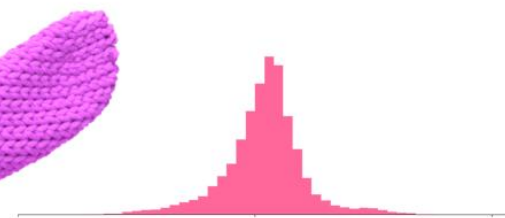
1.3K

STD 0.36



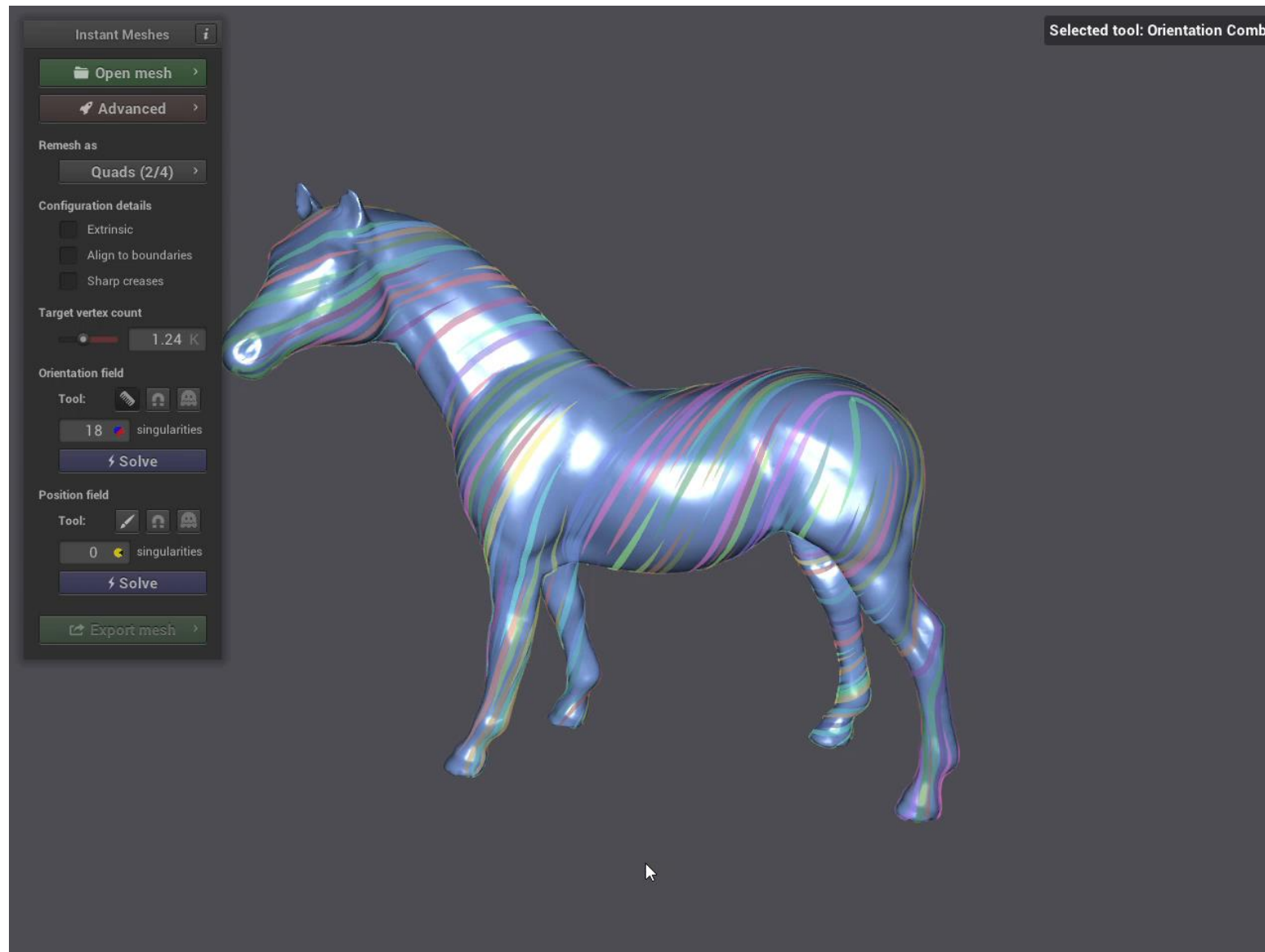
4K

STD 0.22

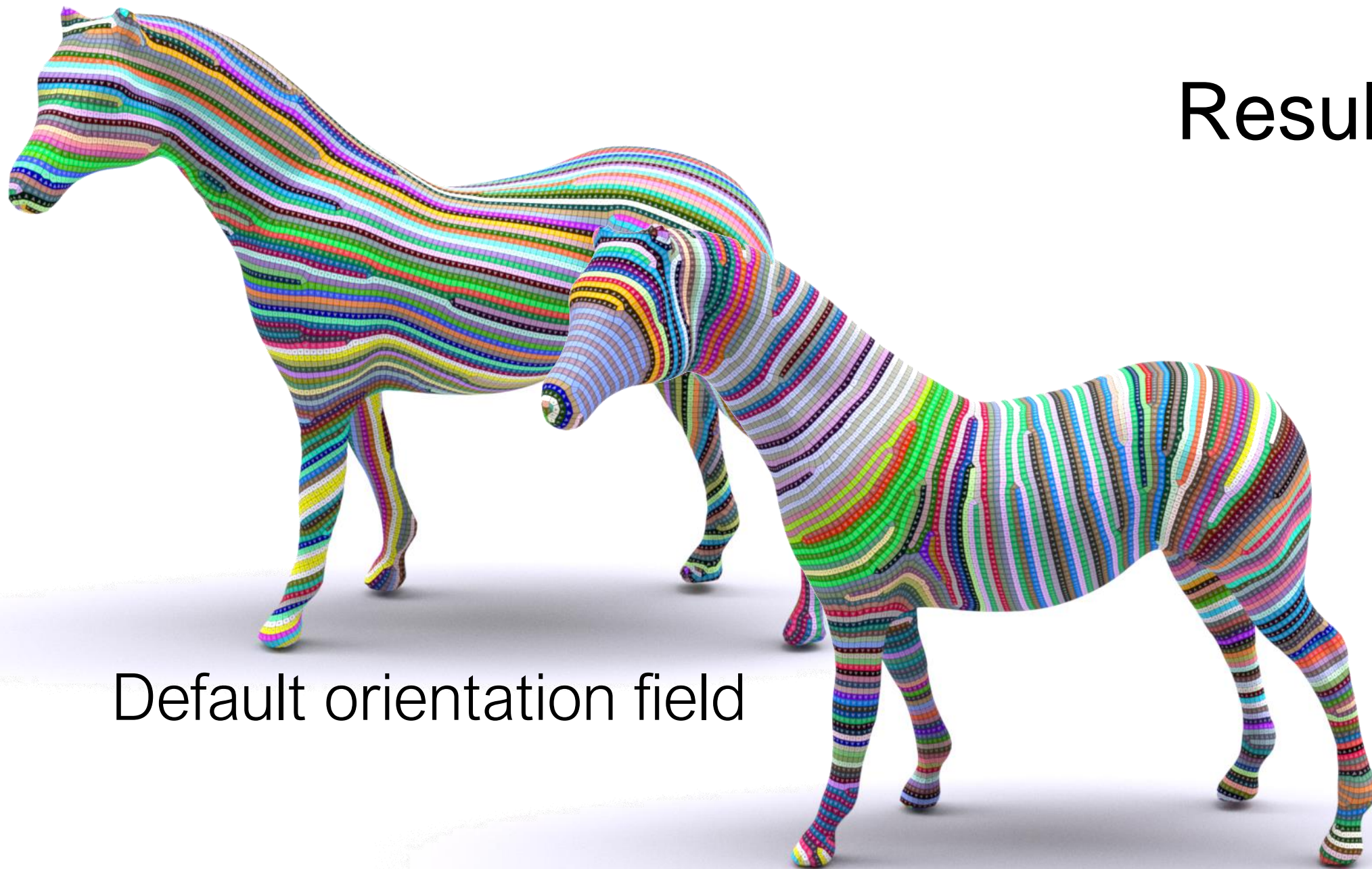


7K

Results



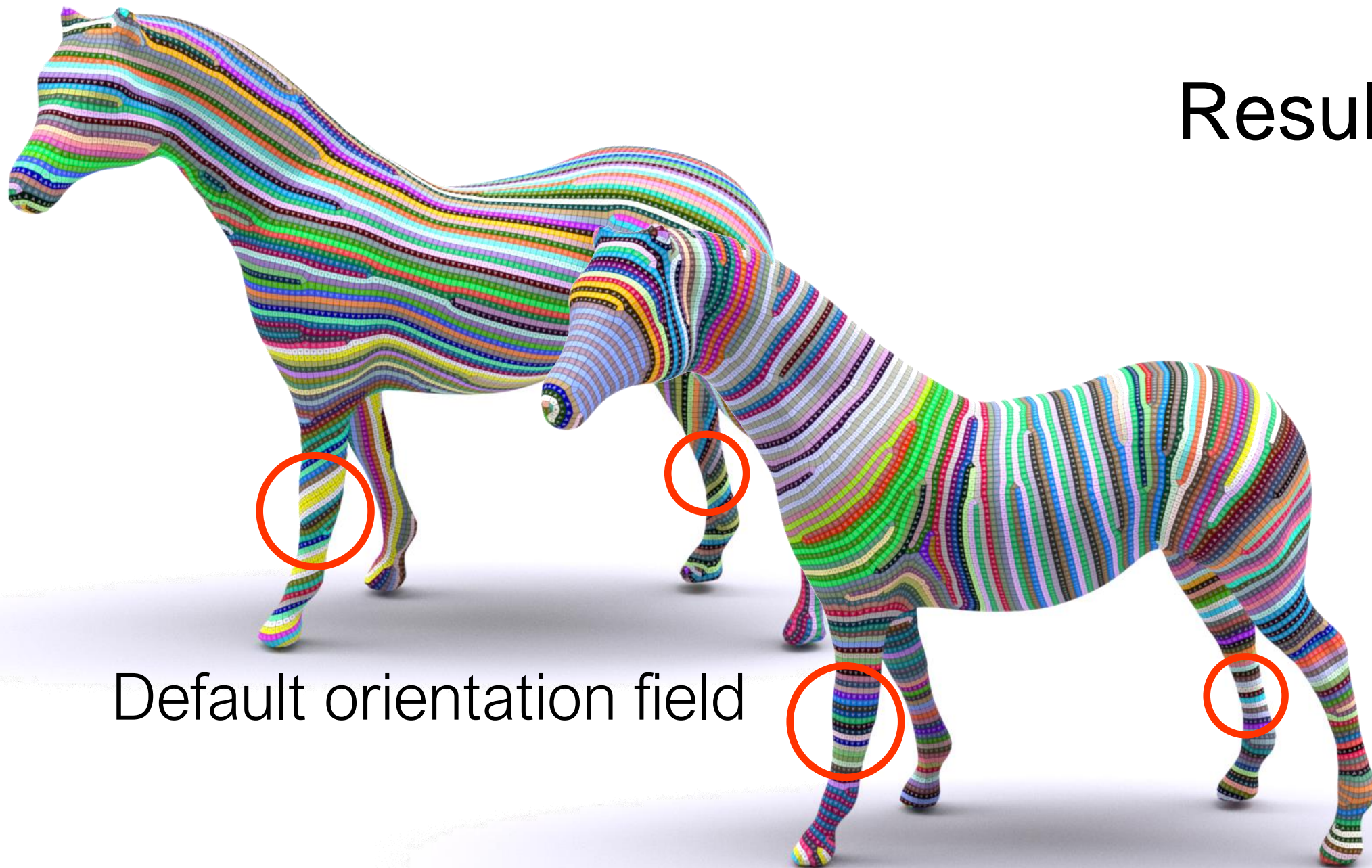
Results



Default orientation field

Custom orientation field

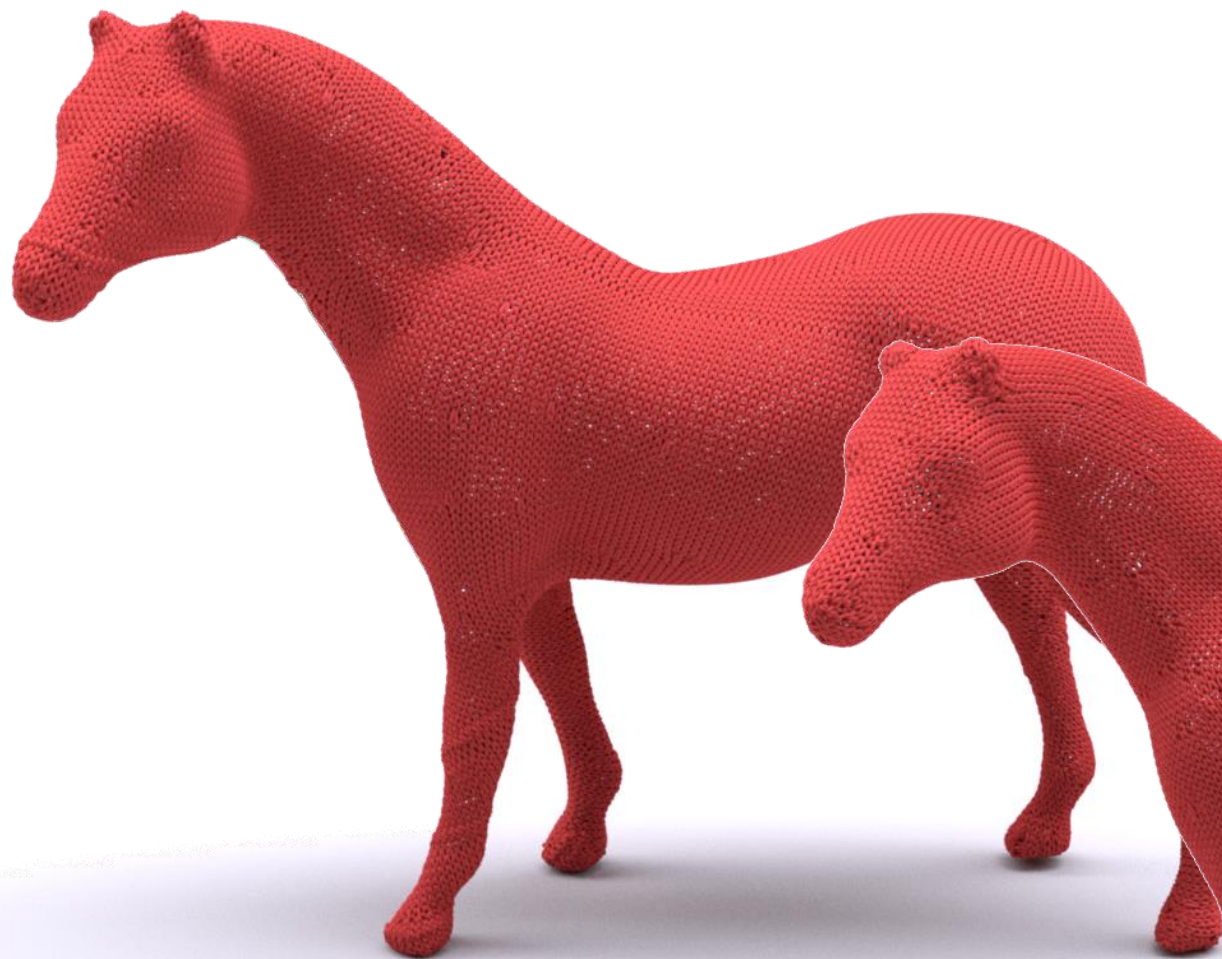
Results



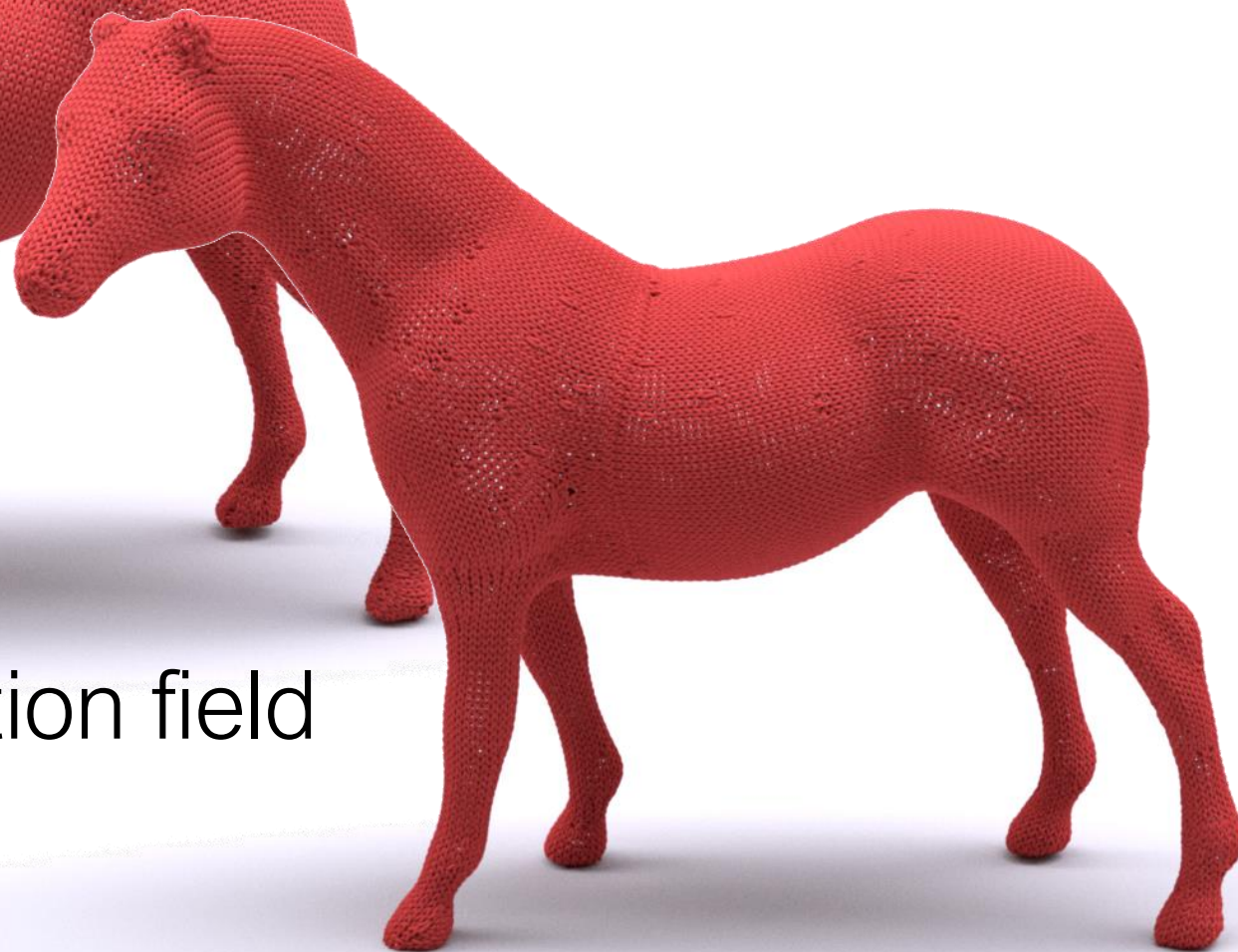
Default orientation field

Custom orientation field

Results



Default orientation field



Custom orientation field

Results

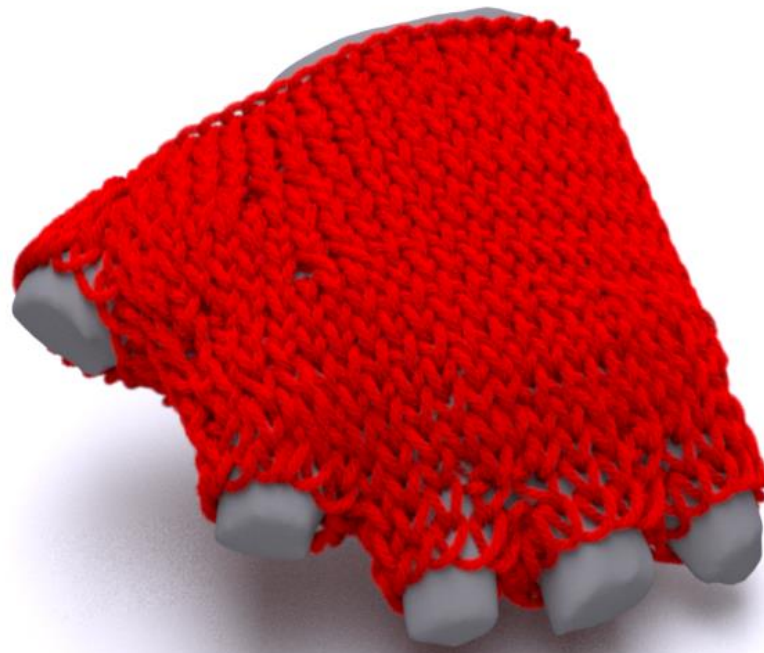
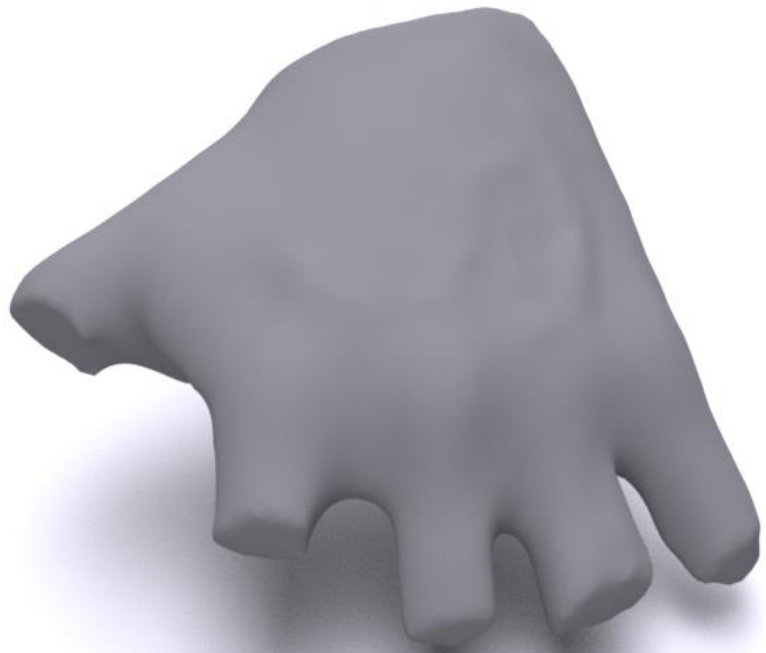
Table 1. *The computation performance measurements for the steps of our pipeline.*

		# Input Faces	# Mesh Faces	# Stitch Faces	Remesh	Labeling	K. Direction Assignment	Stitch Mesh Gen.	Mesh-based Relaxation	Yarn Gen.	Yarn-level Relaxation
Rocker Arm	(Fig.19a)	62K	2,018	7,880	2 s	8 s	99 ms	593 ms	12 s	18 ms	2 hr
Rocker Arm	(Fig.19b)	62K	2,037	7,790	2 s	4 s	127 ms	583 ms	9 s	22 ms	2 hr
Chinese Lion	(Fig.1)	100K	3,495	13,606	4 s	19 s	198 ms	1,049 ms	18 s	39 ms	2 hr*
Kitten	(Fig.1)	100K	3,690	14,460	4 s	16 s	124 ms	1,083 ms	16 s	37 ms	3 hr
Dragon	(Fig.1)	104K	4,218	16,458	4 s	26 s	370 ms	1,234 ms	53 s	35 ms	4 hr*
Horse	(Fig.20a)	134K	4,640	18,172	6 s	17 s	159 ms	1,297 ms	25 s	55 ms	2 hr
Horse	(Fig.20b)	134K	4,655	18,160	6 s	18 s	306 ms	1,311 ms	45 s	52 ms	2 hr
Elephant	(Fig.1)	299K	4,791	18,686	13 s	26 s	237 ms	1,421 ms	28 s	51 ms	2 hr
Fertility	(Fig.3)	167K	4,979	19,490	8 s	32 s	192 ms	1,495 ms	46 s	54 ms	1 hr*
Armadillo	(Fig.17)	280K	6,591	25,734	13 s	58 s	567 ms	1,963 ms	88 s	77 ms	2 hr*
Bunny (1.3K)	(Fig.16)	111K	353	1392	4 s	2 s	45 ms	119 ms	6 s	4 ms	<1 hr
Bunny (4K)	(Fig.16)	111K	1059	4124	4 s	2 s	66 ms	315 ms	8 s	12 ms	<1 hr
Bunny (7K)	(Fig.16)	111K	1,821	7,090	4 s	2 s	131 ms	550 ms	10 s	19 ms	1 hr*
Bunny (16K)	(Fig.16)	111K	4,003	15,704	5 s	16 s	147 ms	1101 ms	12 s	45 ms	2 hr
Bunny (48K)	(Fig.16)	406K	12,195	48,096	37 s	84 s	399 ms	3526 ms	130 s	159 ms	3 hr*

The computation times are generated using a computer with Intel Core i7 6700HQ CPU @ 2.60 GHz with 16 GB RAM.

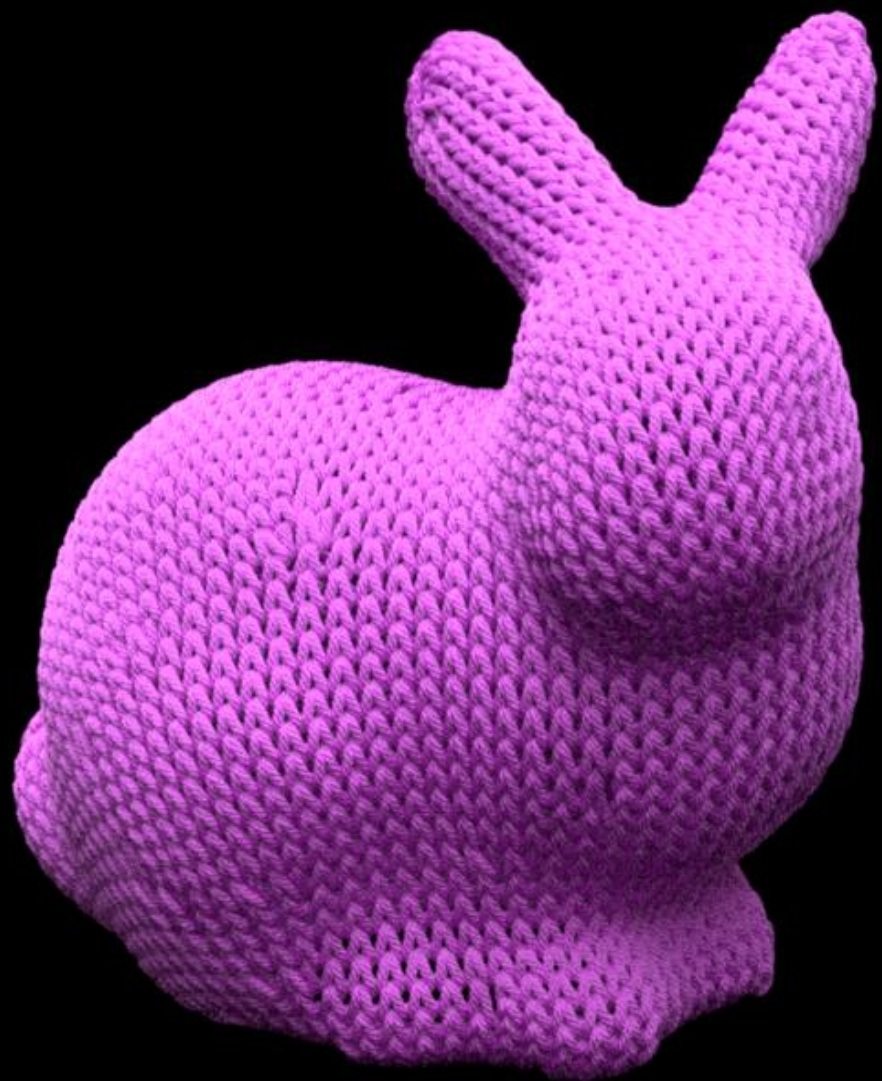
** Yarn-level relaxation timings are generated using a computer with Intel Core i7 3930K CPU @ 3.20 GHz with 32 GB RAM.*

Customized 3D Print Glove



3D Print Octopus Sweater





Results



Results



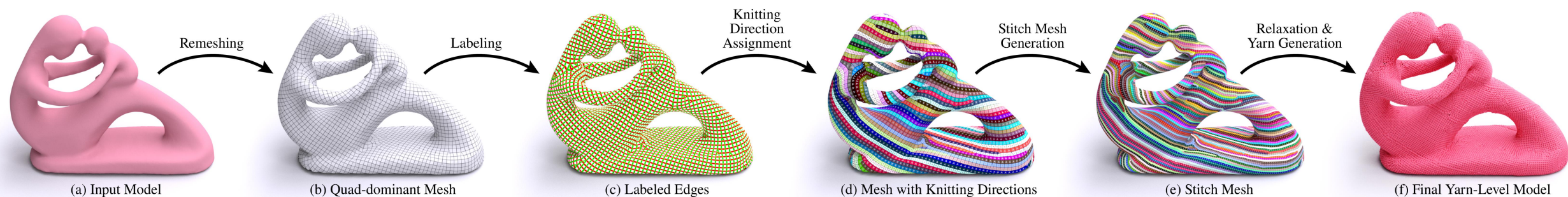
Results



Tests with 106 models

Conclusion

We introduce the first **fully automatic** pipeline to convert arbitrary 3D shapes into knit models.

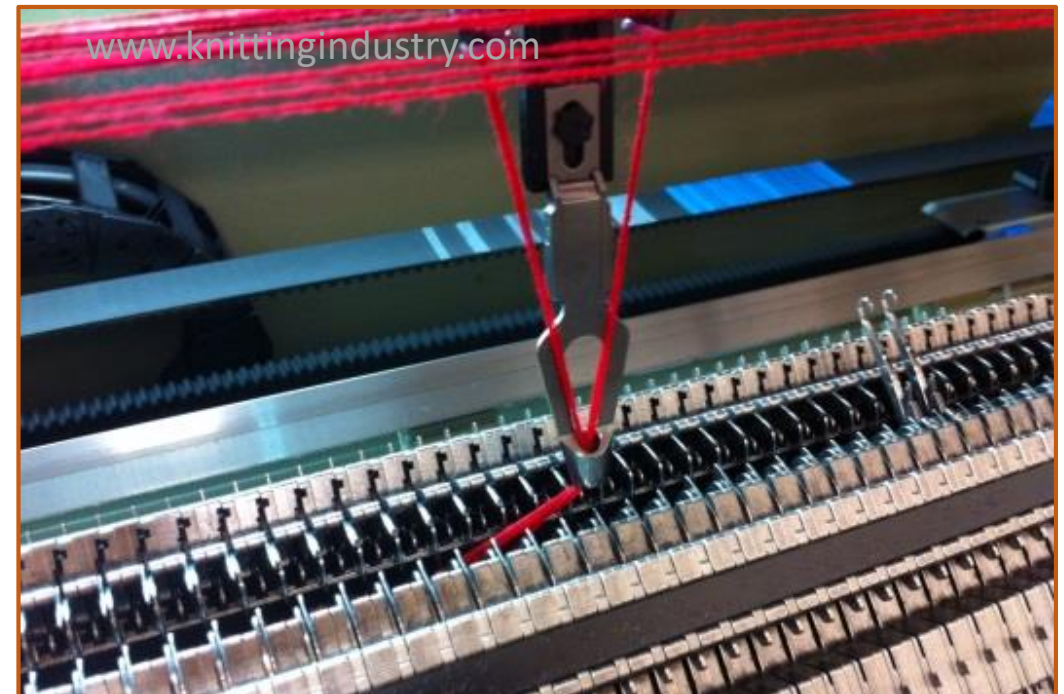


Future Work

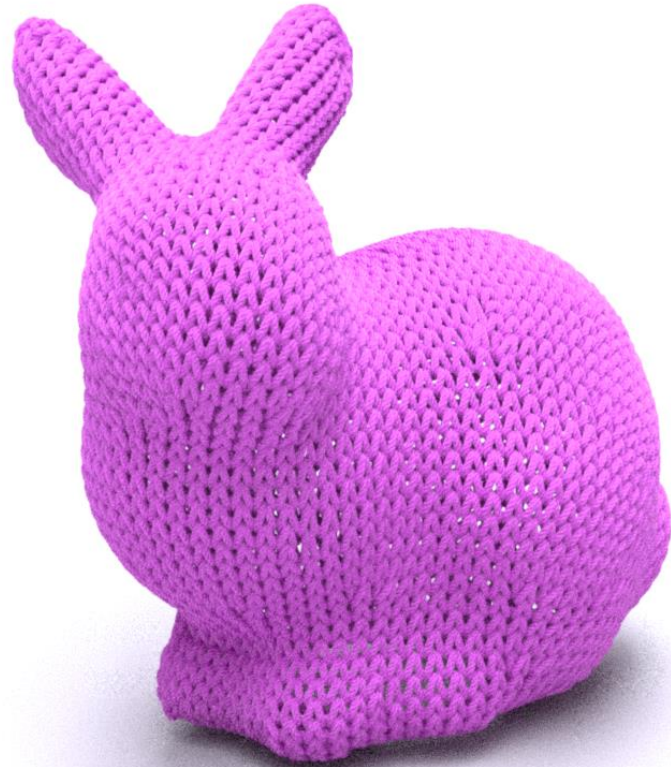
Convert knitted structure to **knittable** structure



Hand Knitting



Machine Knitting



Thanks!

Website: <http://www.cs.utah.edu/~kwu>

Email: kwu@cs.utah.edu

