

Differentiable Rendering for Mesh and Implicit Surface

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Tencent America

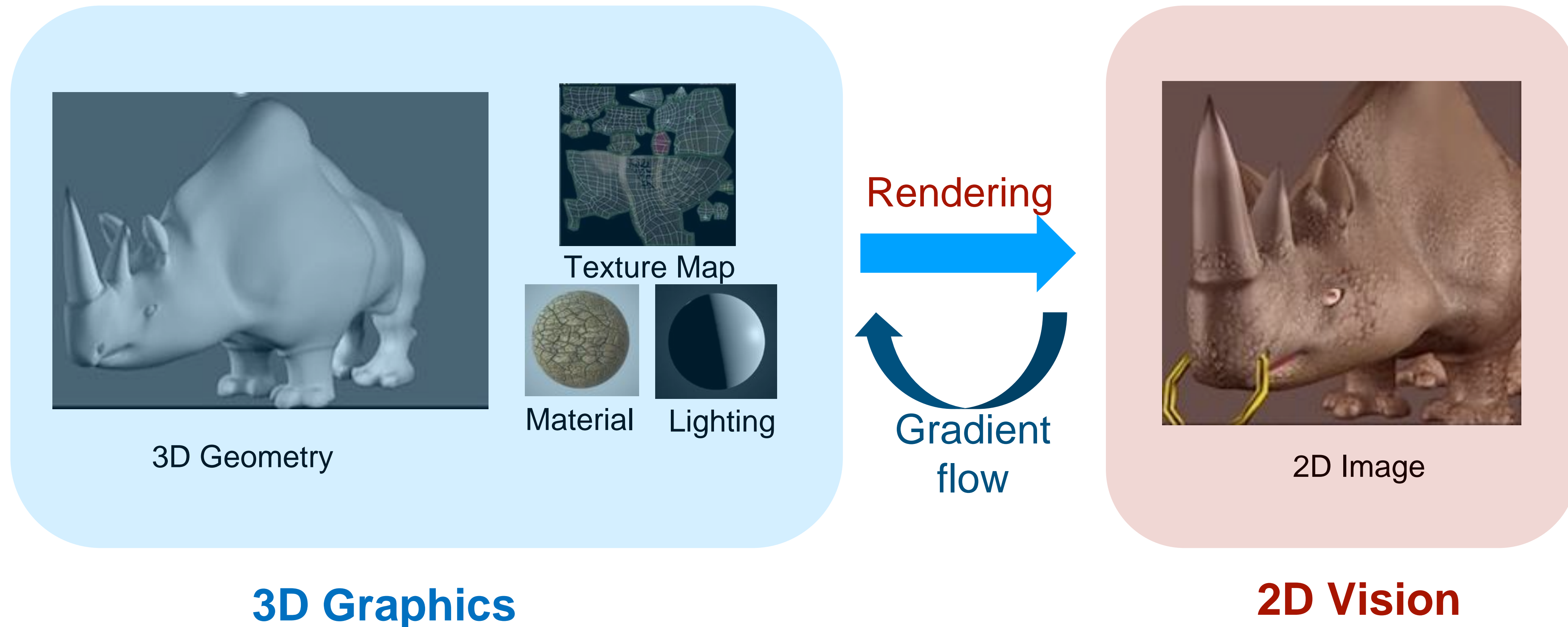
Outline

- Motivation
- SoftRas: A Differentiable Renderer for Triangular Mesh (ICCV'19)
- Learning to Infer Implicit Surfaces without 3D Supervision (NeurIPS'19)
- Conclusions

Motivation

Why Differentiable Rendering?

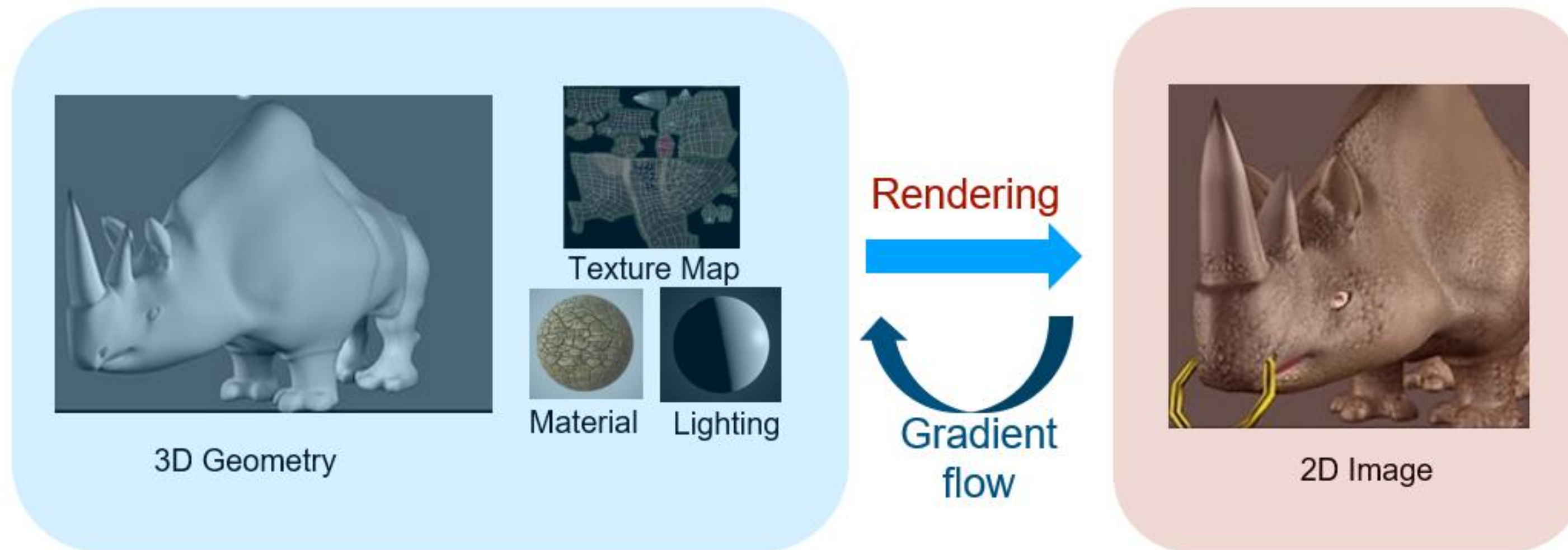
Rendering can be viewed as the “*bridge*” connecting 3D graphics and 2D vision



Differentiable rendering enables direct optimization of 3D properties based on **image-based supervision** -- gradients flowing from image pixels to 3D!

Motivation

Why Differentiable Rendering?



3D Graphics

2D Vision

Applications

Pose estimation
3D reconstruction
Material Inference
Lighting Estimation

....

ALL Image-based 3D Reasoning Tasks!

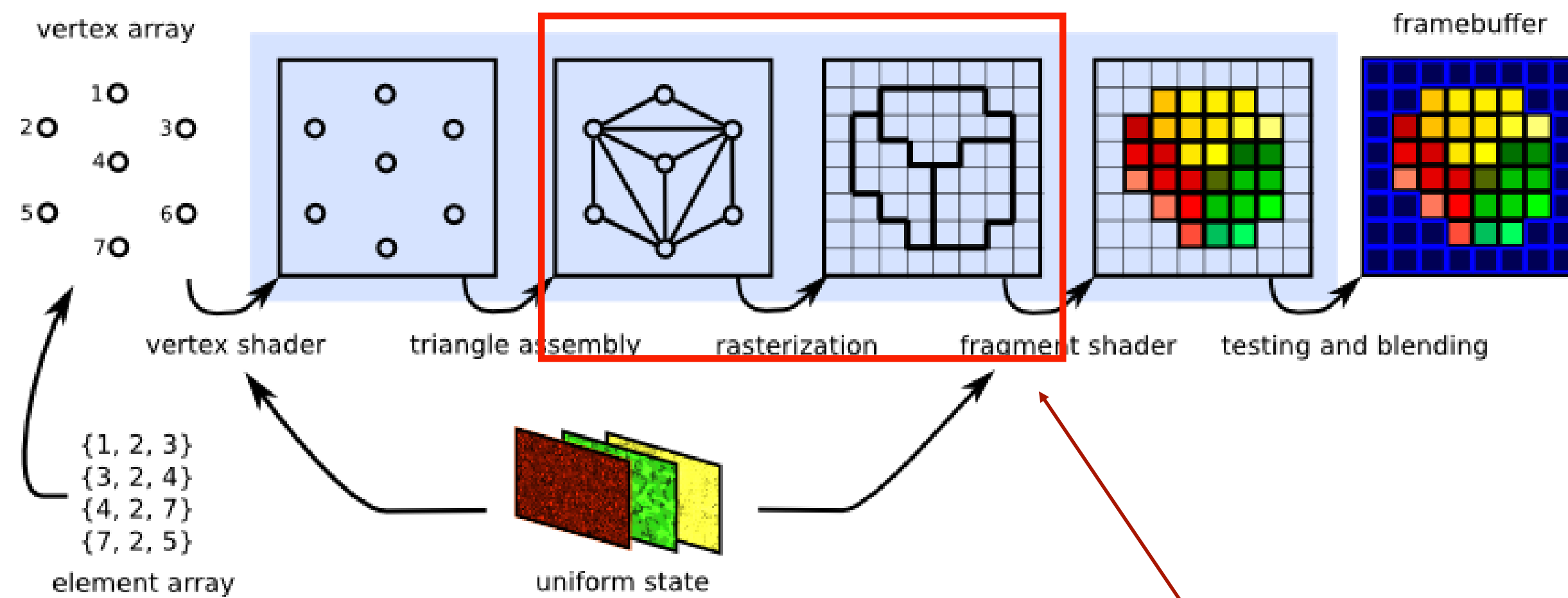
3D Unsupervised Learning!

Differentiable Rendering for Meshes

Soft Rasterizer: A Differentiable Renderer for Image-based 3D Reasoning, ICCV'19 (Oral)

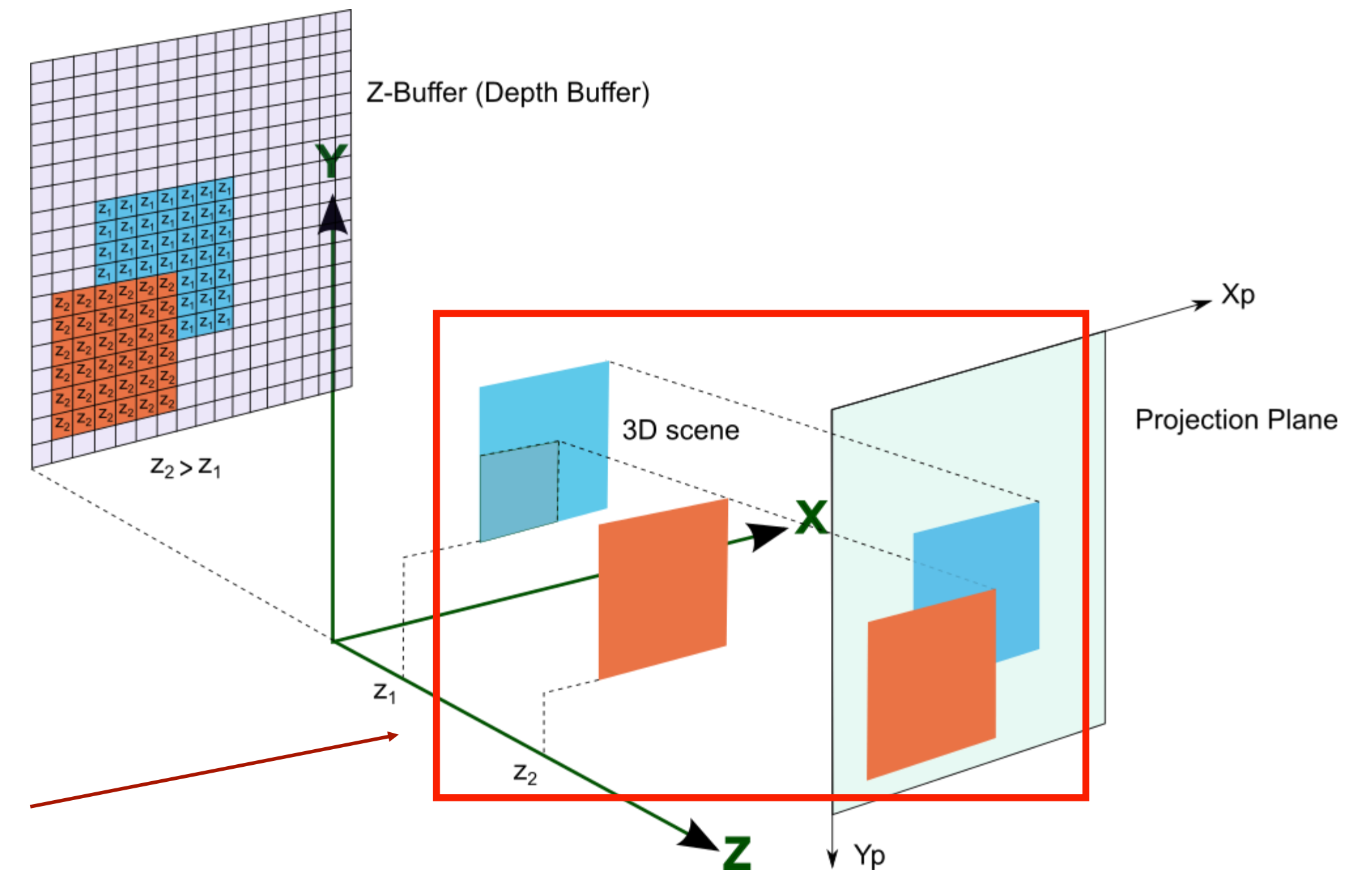
Challenges

Standard Graphics Rendering is NOT Differentiable



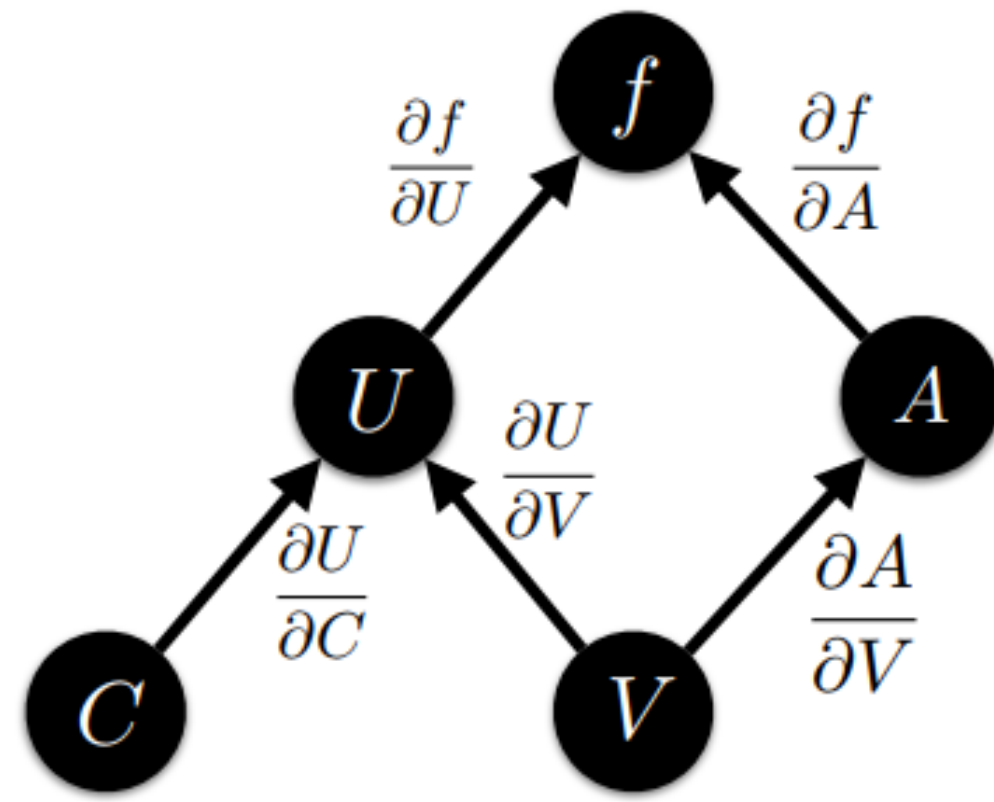
Rasterization
(XY plane)

Discrete sampling

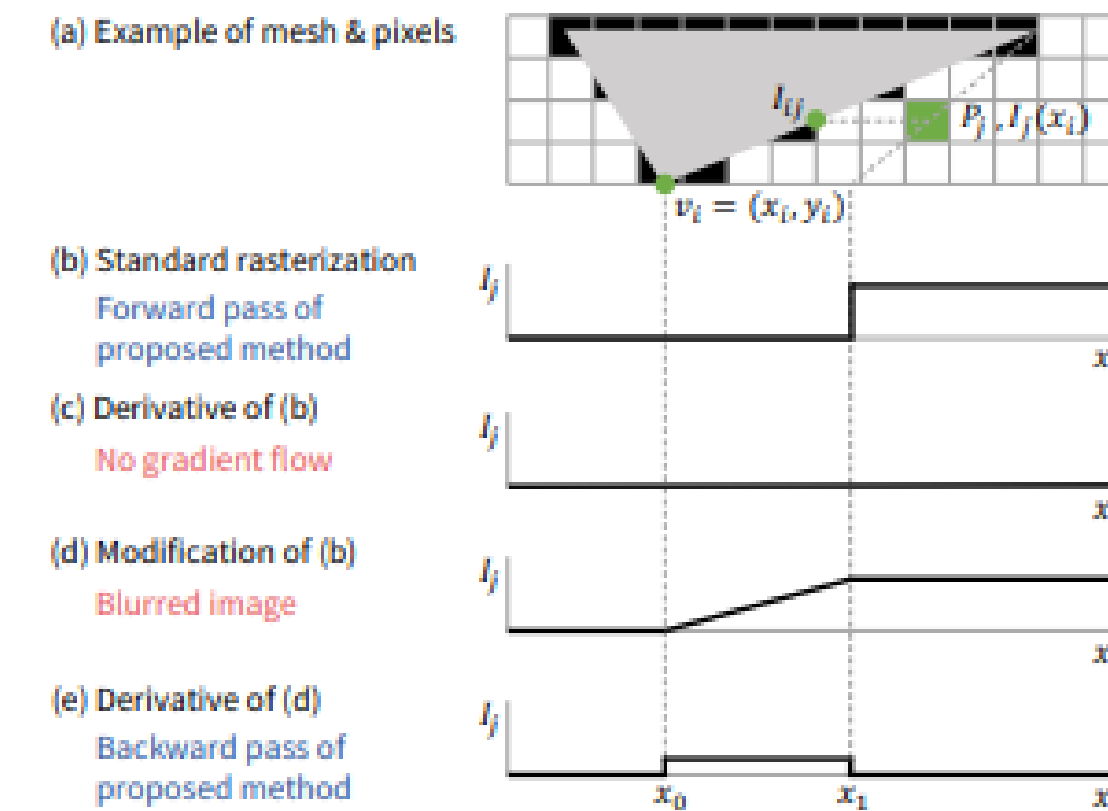


Z-Buffering
(Z/depth direction)

Previous Works



OpenDR [Loper et al. 14]

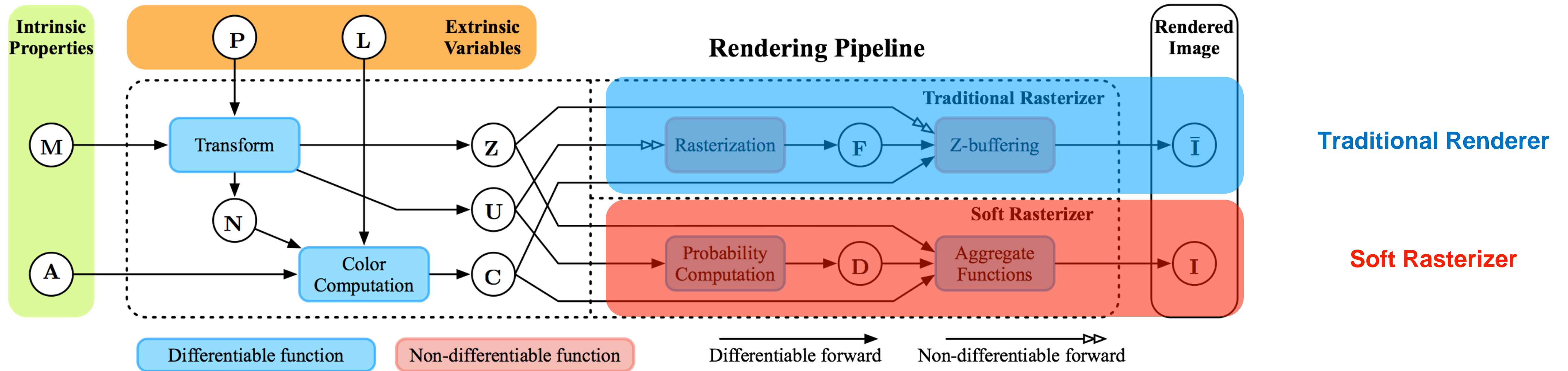


Neural 3D Mesh Renderer [Kato et al. 18]

Both directly use OpenGL in the forward rendering and approximate the rendering gradient using hand-crafted functions.

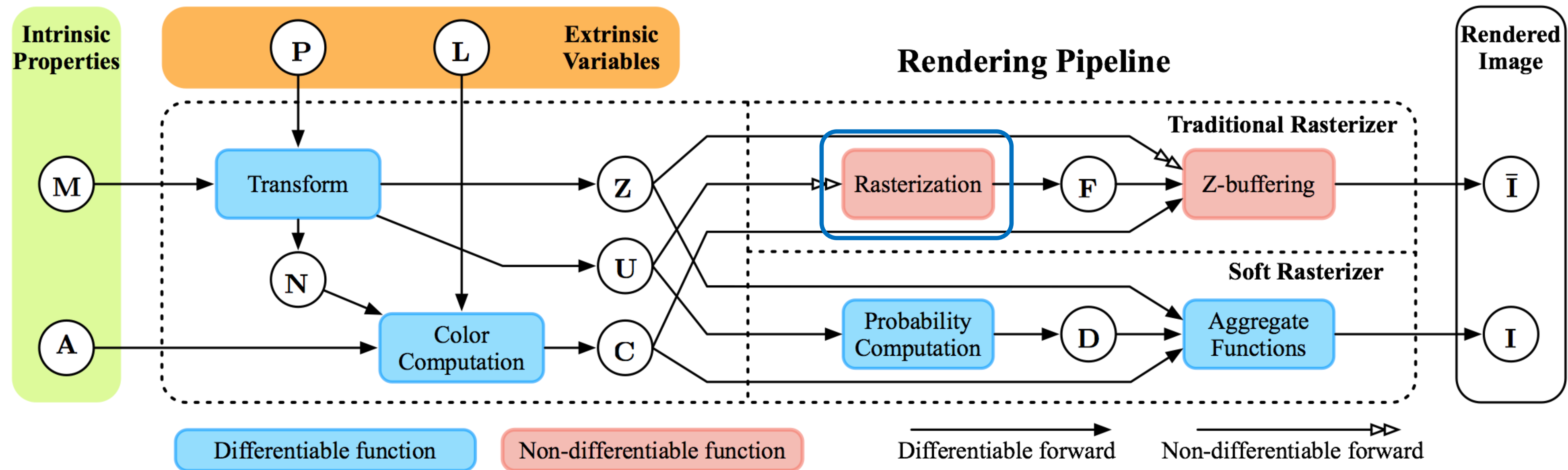
Problem: the gradient is not consistent with the forward rendering

Proposed Rendering Pipeline

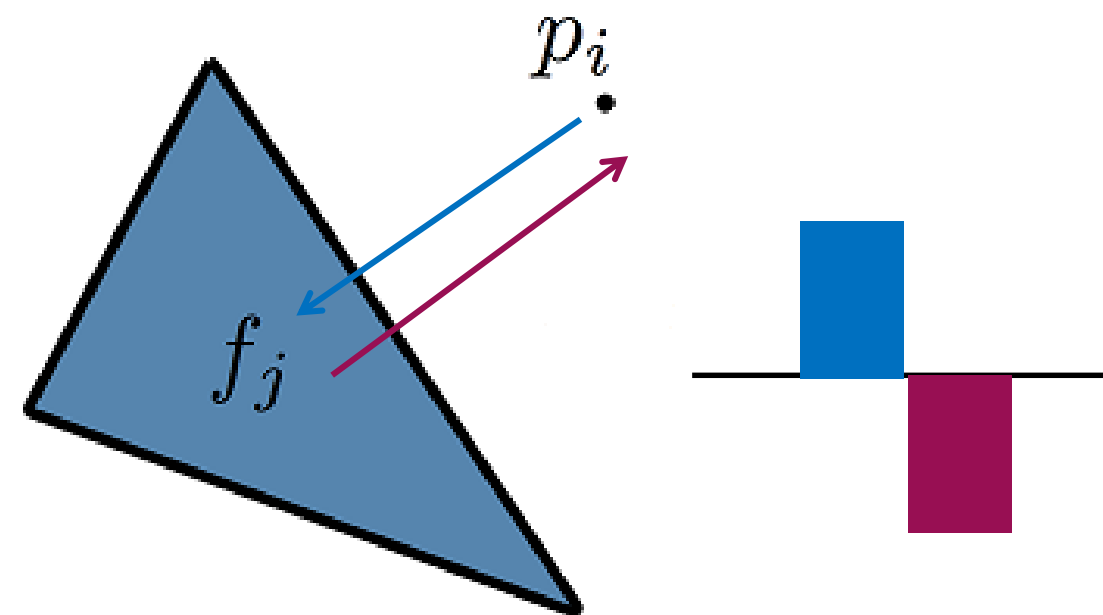


Rasterization and z-buffering are **non-differentiable** functions

Differentiable Rasterization



Traditional Rasterization

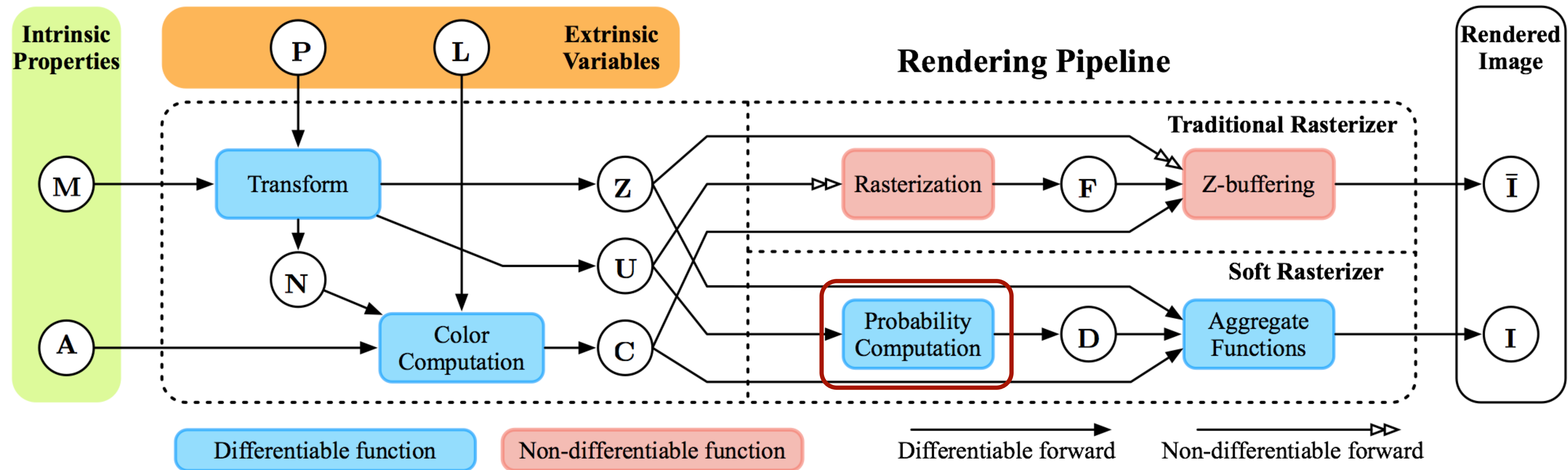


Color of p_i suffers from a sudden change when cross the edge of the triangle f_j

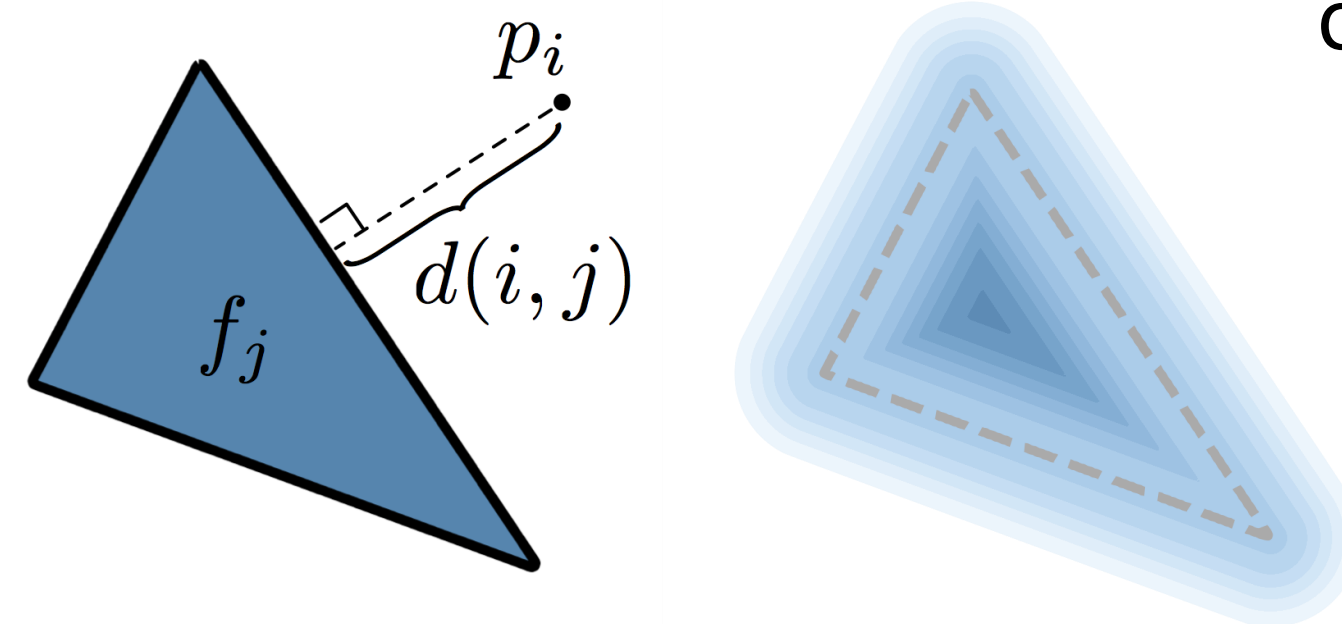


zero gradient in almost everywhere in the space

Differentiable Rasterization

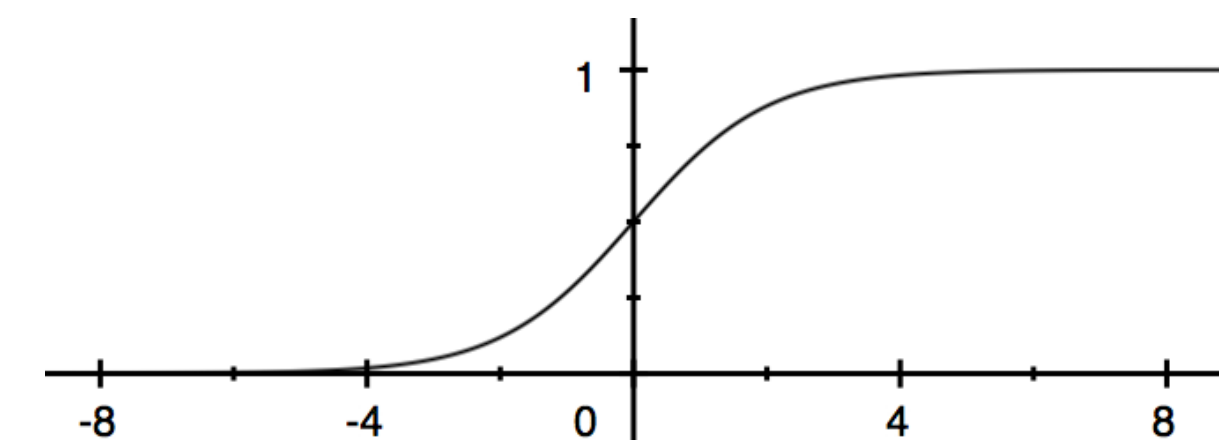


Soft Rasterization

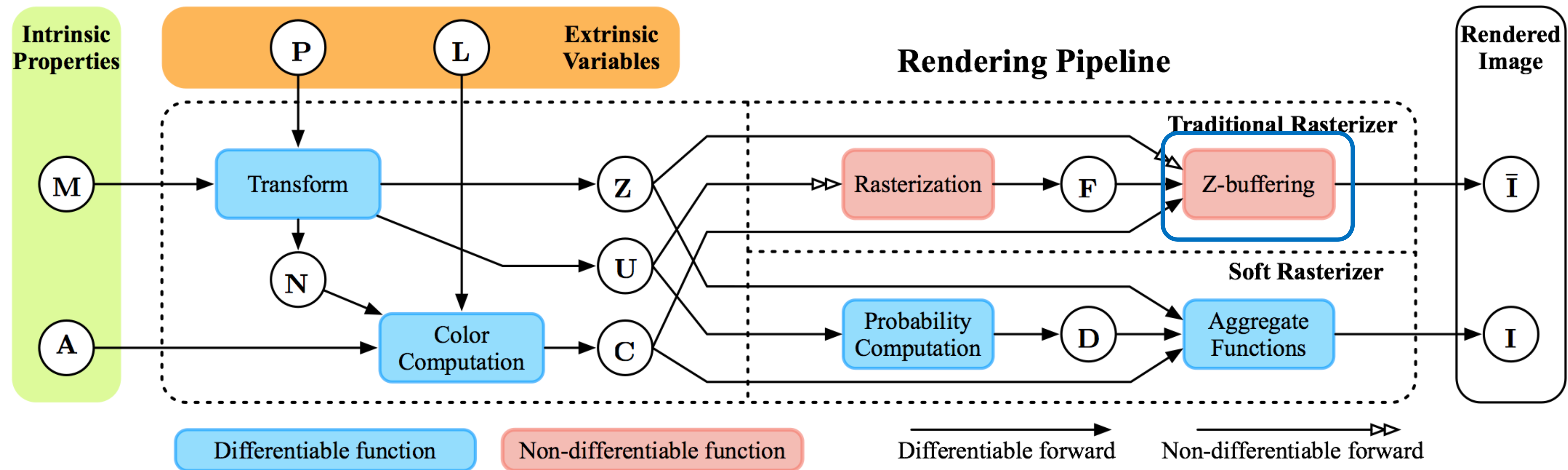


Change of color is formulated in a **probabilistic** way depending on *the distance between the pixel and triangle edge*.

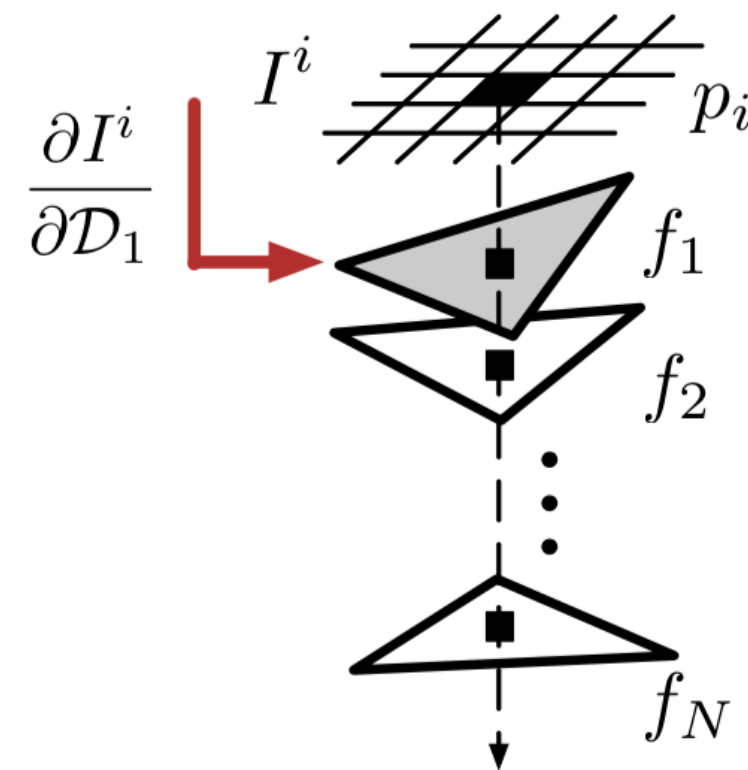
$$\mathcal{D}_j^i = \text{sigmoid}(\delta_j^i \cdot \frac{d^2(i, j)}{\sigma})$$



Differentiable Z-Buffering



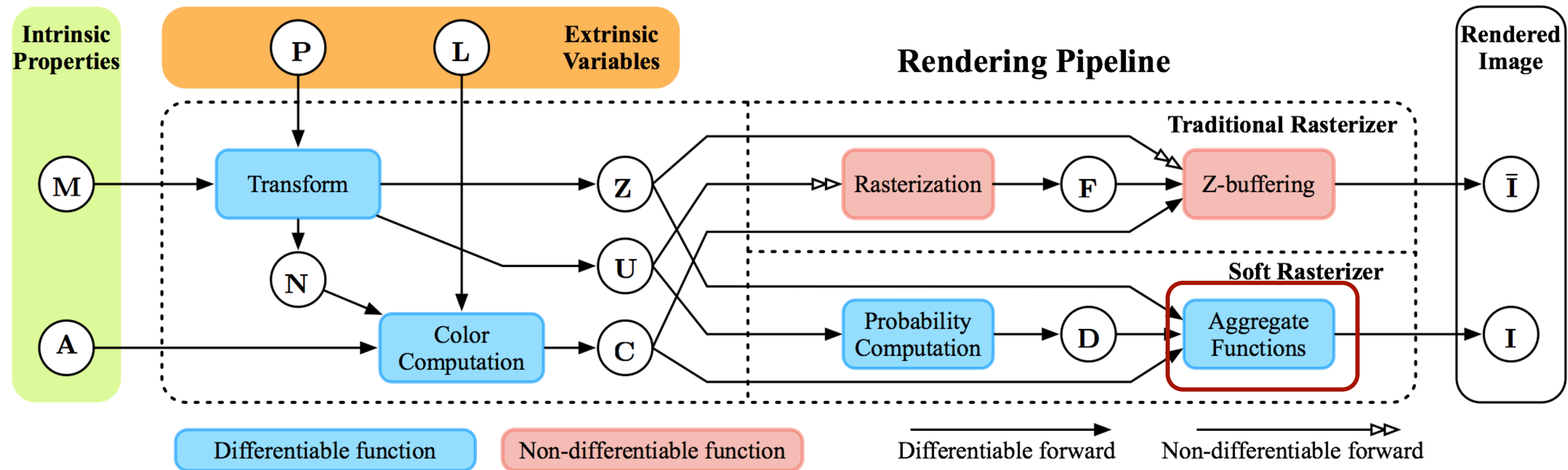
Traditional Z-Buffering



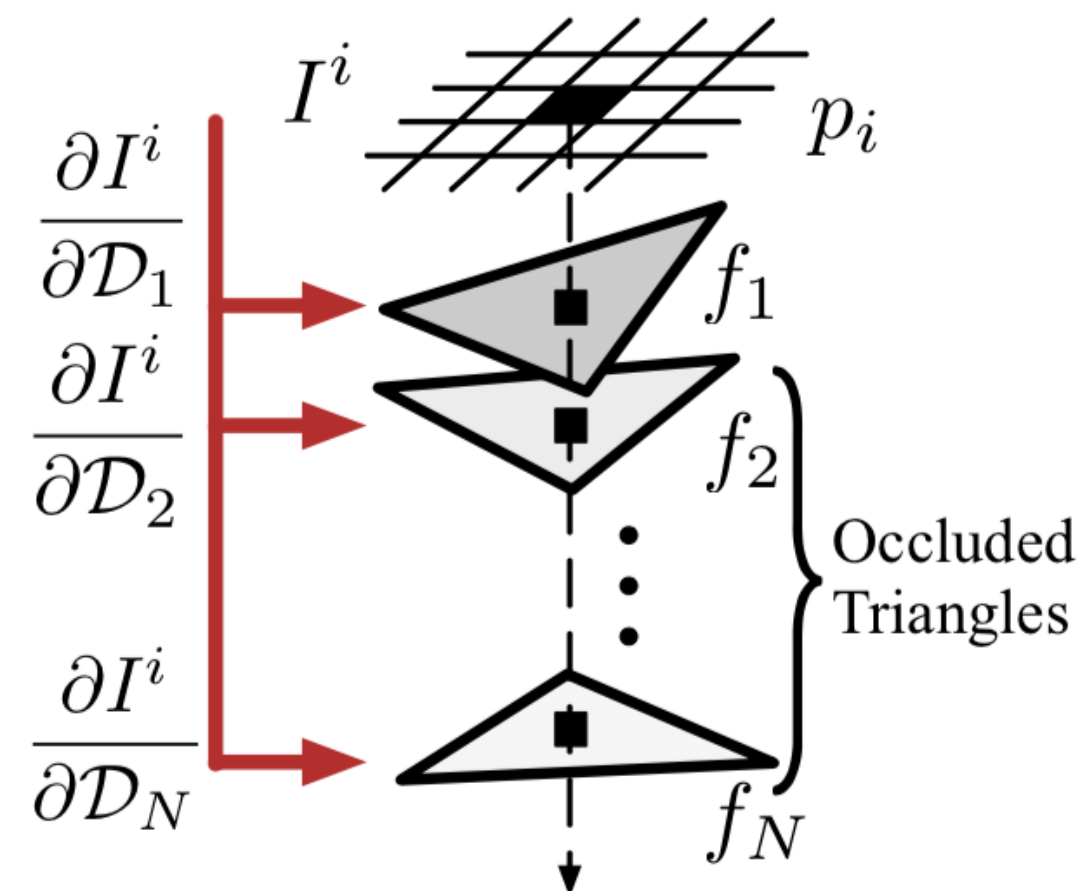
Color is determined by the nearest triangle

Non-differentiable **One-hot Voting!**

Differentiable Z-Buffering



Soft Z-Buffering



The final color is the **probabilistic aggregation** of **all possible triangles along the Z/depth direction** depending on their relative depth.

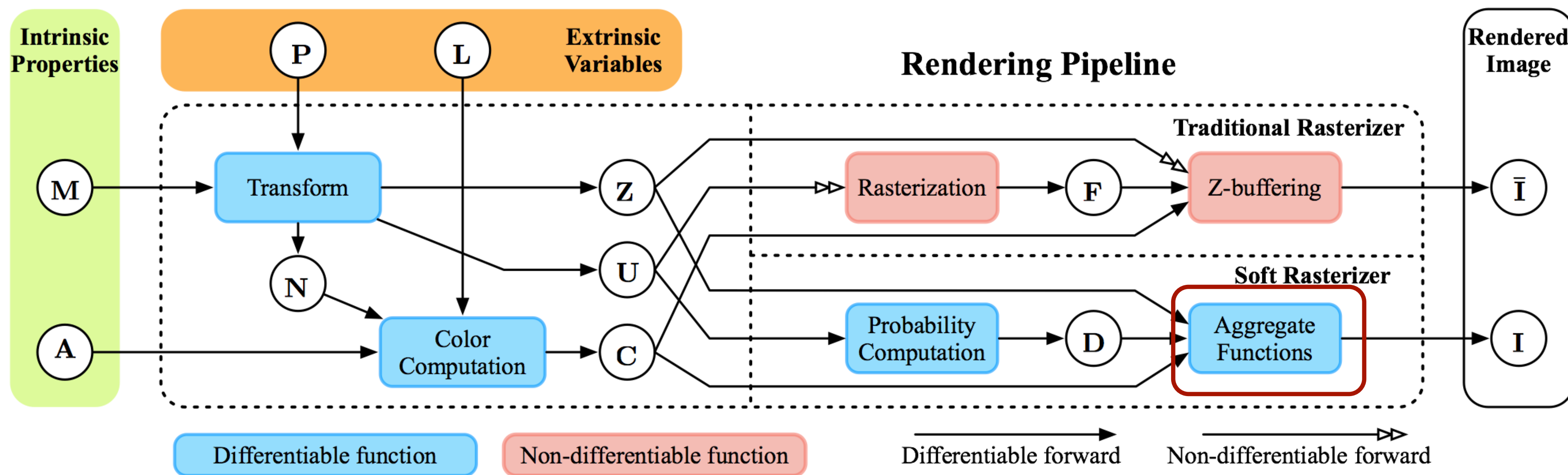
Aggregation Function

$$I^i = \mathcal{A}_S(\{C_j\}) = \sum_j w_j^i C_j^i + w_b^i C_b$$

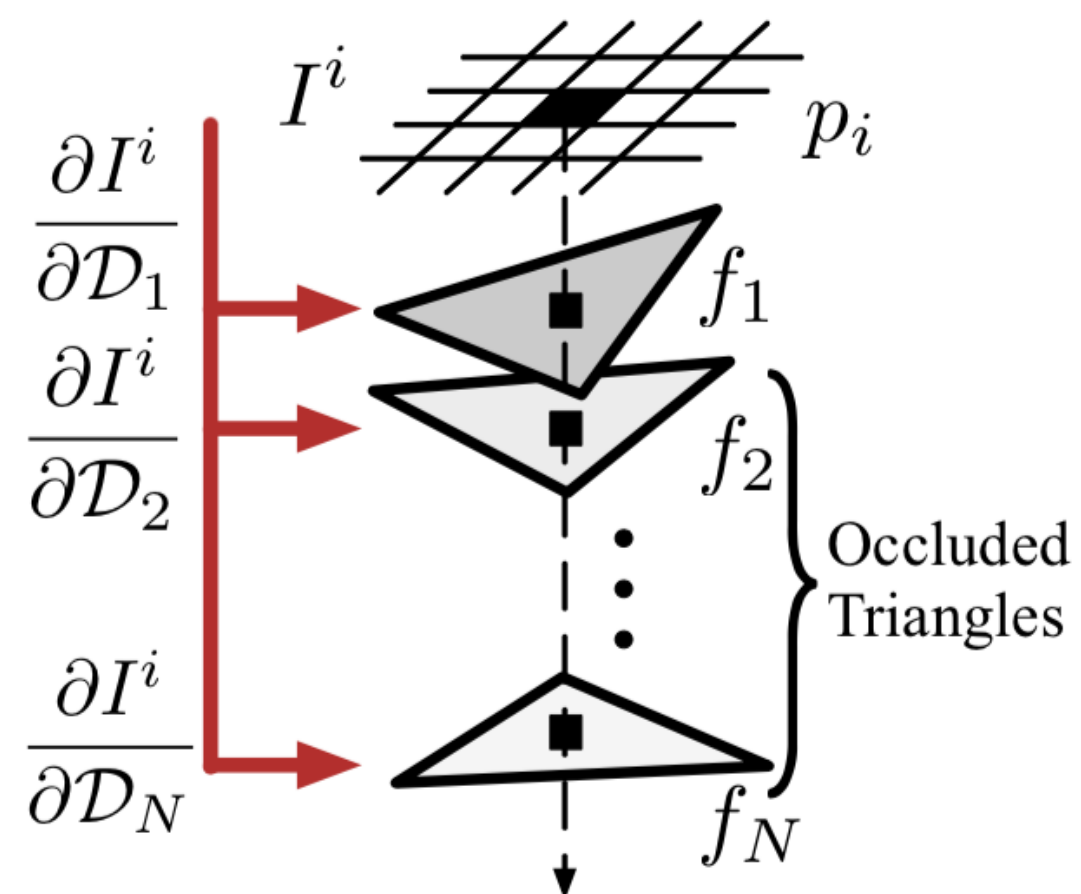
$$w_j^i = \frac{\mathcal{D}_j^i \exp(z_j^i / \gamma)}{\sum_k \mathcal{D}_k^i \exp(z_k^i / \gamma) + \exp(\epsilon / \gamma)}$$

- 1) Triangles closer to the image plane has higher contribution/gradient during optimization.
- 2) Enable gradient to flow into occluded triangles.

Differentiable Z-Buffering



Soft Z-Buffering



Aggregation Function can have different forms!

$$I^i = \mathcal{A}_S(\{C_j\}) = \sum_j w_j^i C_j^i + w_b^i C_b$$

Color

$$I_s^i = \mathcal{A}_O(\{D_j\}) = 1 - \prod_j (1 - D_j^i)$$

Silhouette

$$\mathcal{A}_N = \text{Neural Network}$$

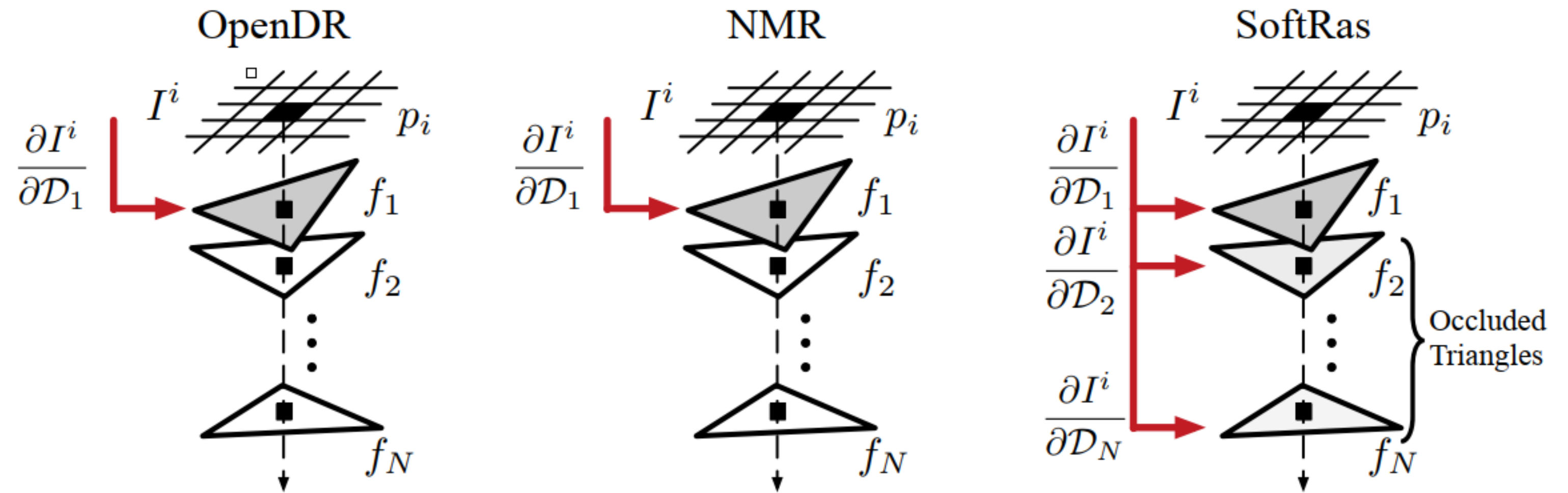
Color

Silhouette

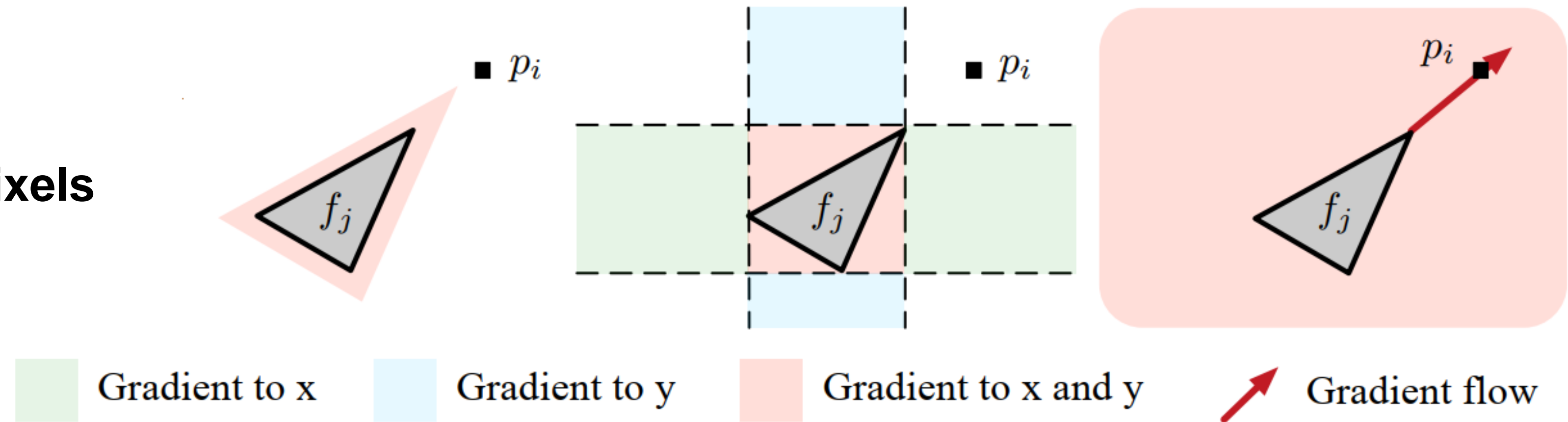
\vdots

Comparisons of Different DRs

Gradient from pixels to triangles

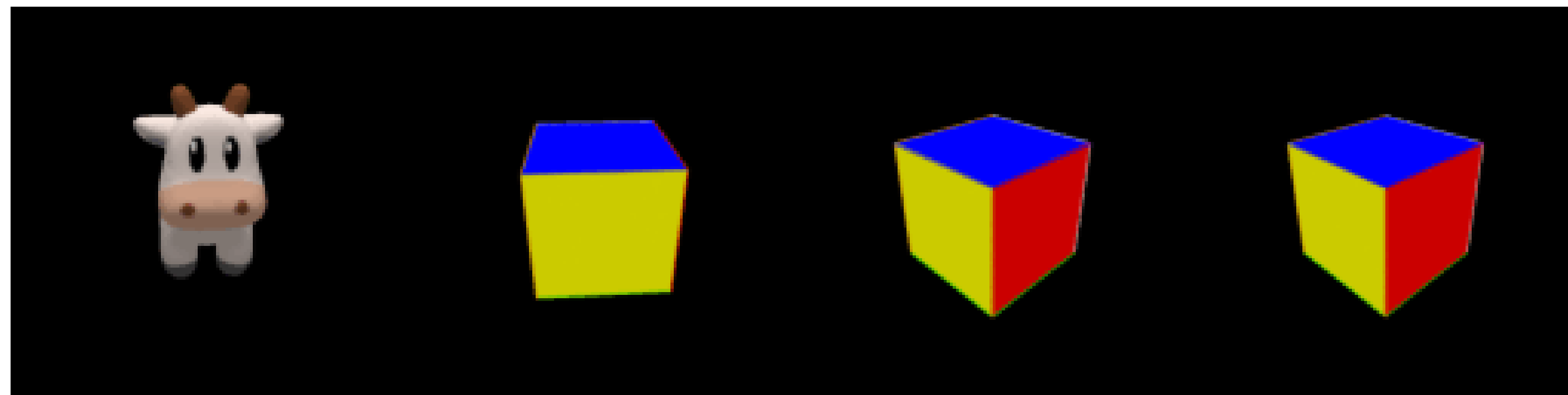
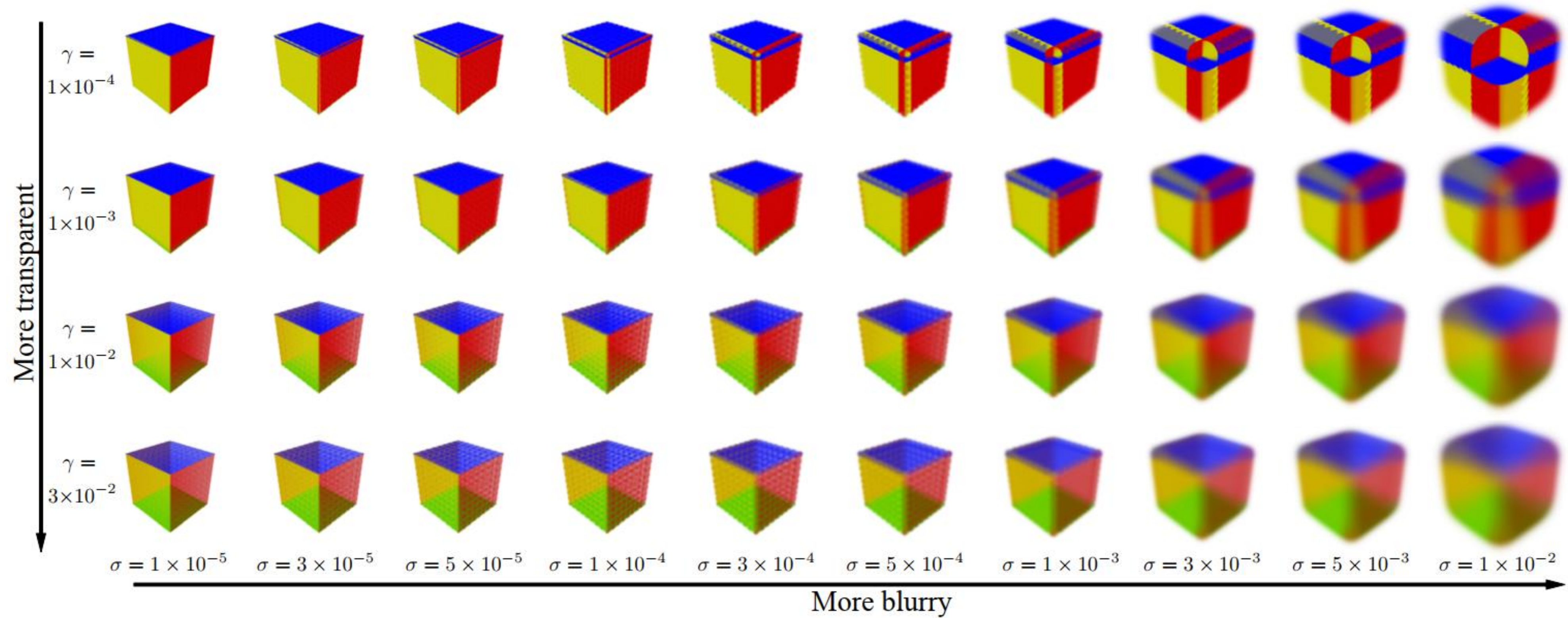


Screen-space gradient from pixels to vertices

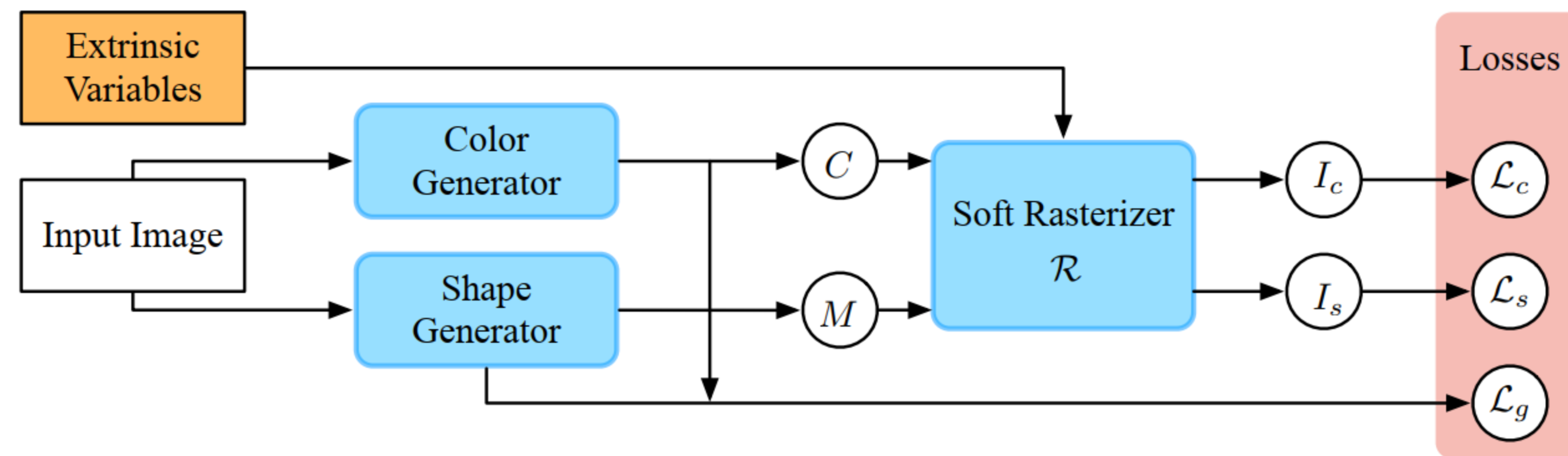


Applications – Forward Rendering

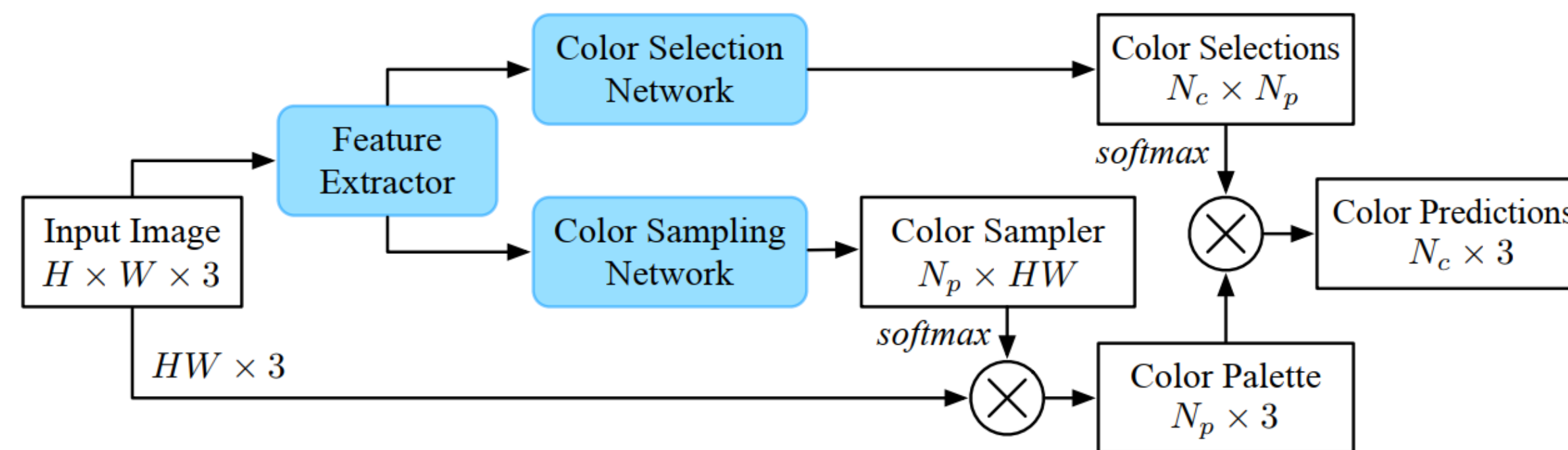
Controllable Rendering Effect



Applications – Single-view Mesh Reconstruction



Single-view Reconstruction Network



Color Generator

Loss function

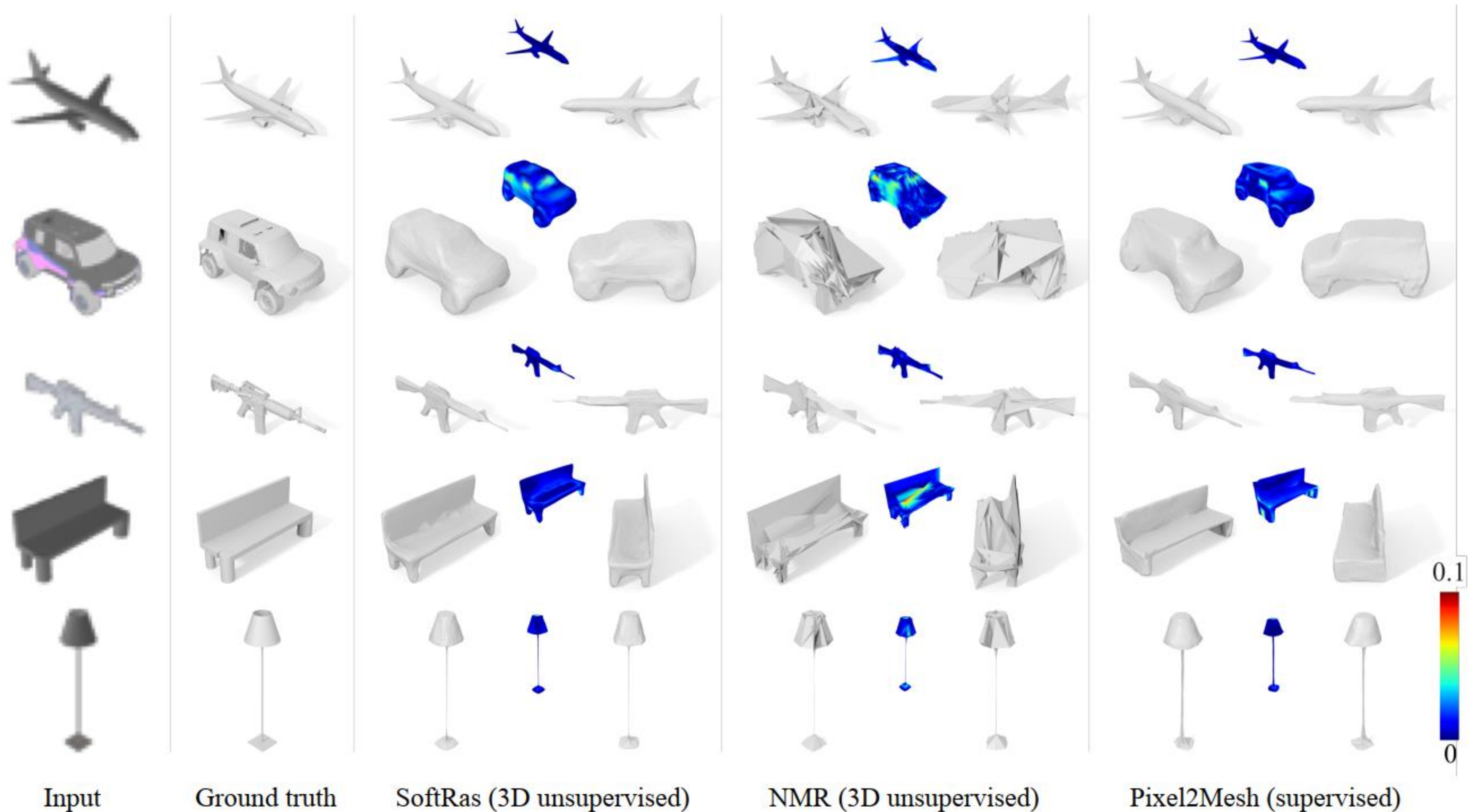
$$\mathcal{L} = \mathcal{L}_s + \lambda \mathcal{L}_c + \mu \mathcal{L}_g$$

Silhouette loss Color loss Geometry regularizer

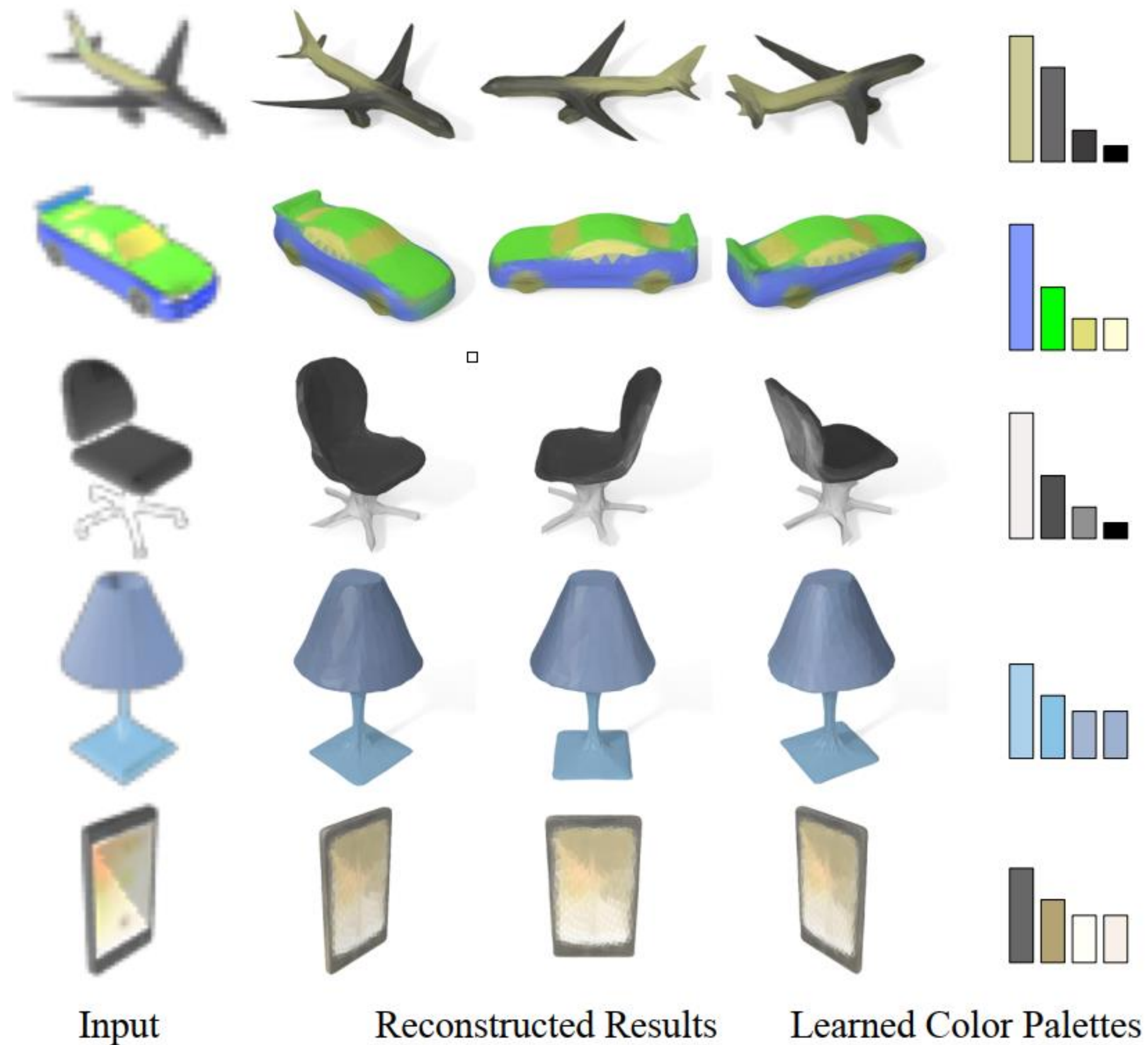
3D Unsupervised Learning!

Applications – Single-view Mesh Reconstruction

Qualitative Comparison



Applications – Single-view Mesh Reconstruction



Color Reconstruction

ShapeNet Dataset

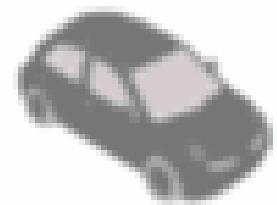
Category	Airplane	Bench	Dresser	Car	Chair	Display	Lamp
Retrieval [47]	0.5564	0.4875	0.5713	0.6519	0.3512	0.3958	0.2905
Voxel [47]	0.5556	0.4924	0.6823	0.7123	0.4494	0.5395	0.4223
NMR [19]	0.6172	0.4998	0.7143	0.7095	0.4990	0.5831	0.4126
Ours (sil.)	0.6419	0.5080	0.7116	0.7697	0.5270	0.6156	0.4628
Ours (full)	0.6670	0.5429	0.7382	0.7876	0.5470	0.6298	0.4580

Category	Speaker	Rifle	Sofa	Table	Phone	Vessel	Mean
Retrieval [47]	0.4600	0.5133	0.5314	0.3097	0.6696	0.4078	0.4766
Voxel [47]	0.5868	0.5987	0.6221	0.4938	0.7504	0.5507	0.5736
NMR [19]	0.6536	0.6322	0.6735	0.4829	0.7777	0.5645	0.6015
Ours (sil.)	0.6654	0.6811	0.6878	0.4487	0.7895	0.5953	0.6234
Ours (full)	0.6807	0.6702	0.7220	0.5325	0.8127	0.6145	0.6464

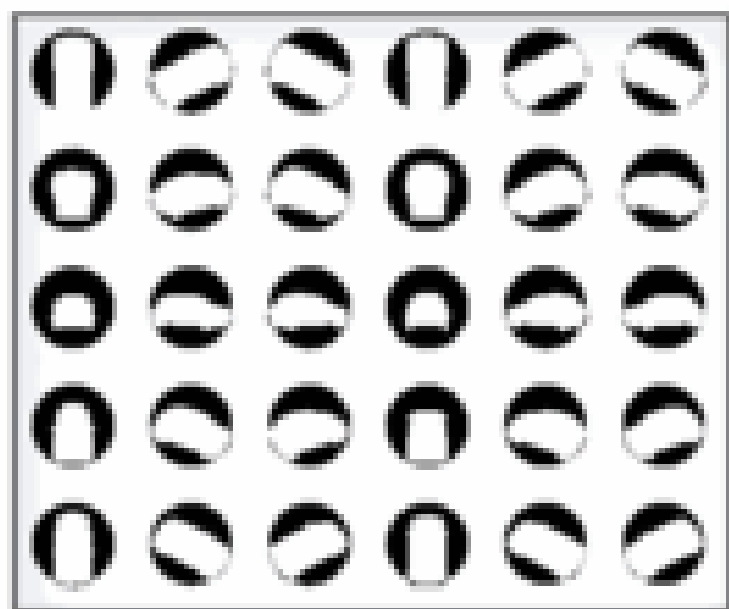
Quantitative Comparison

Applications – Shape Deformation

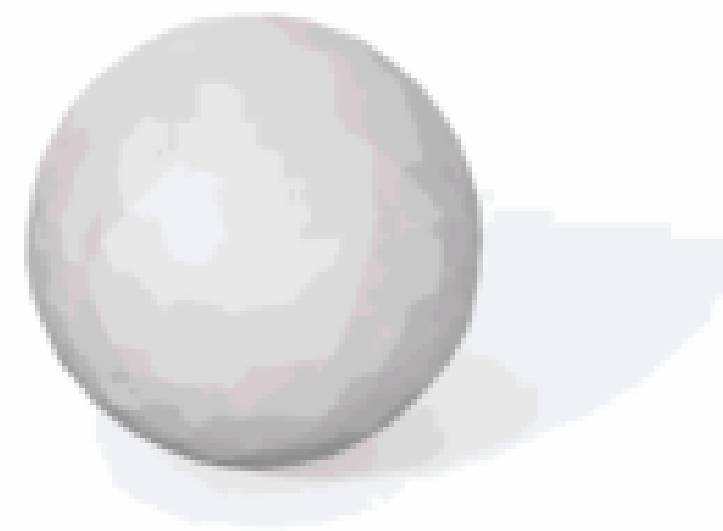
Deforming Sphere to Car



Target image



Multi-view silhouette difference

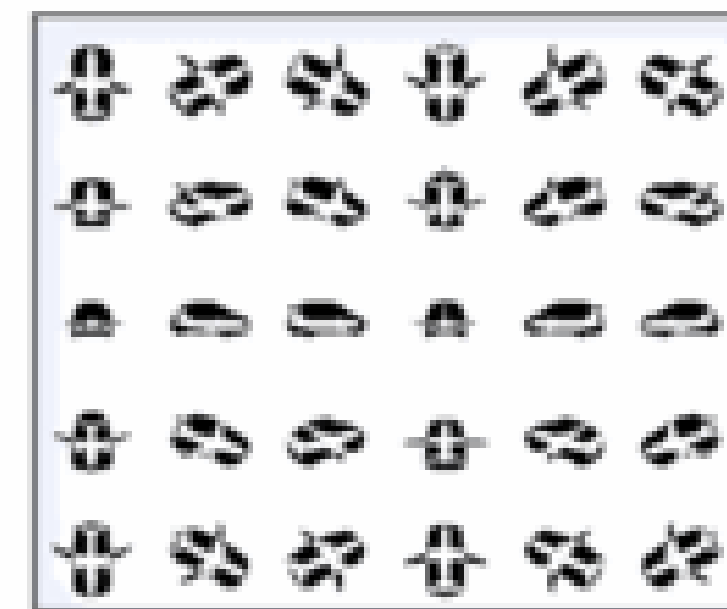


Deformed mesh

Deforming Car to Airplane



Target image

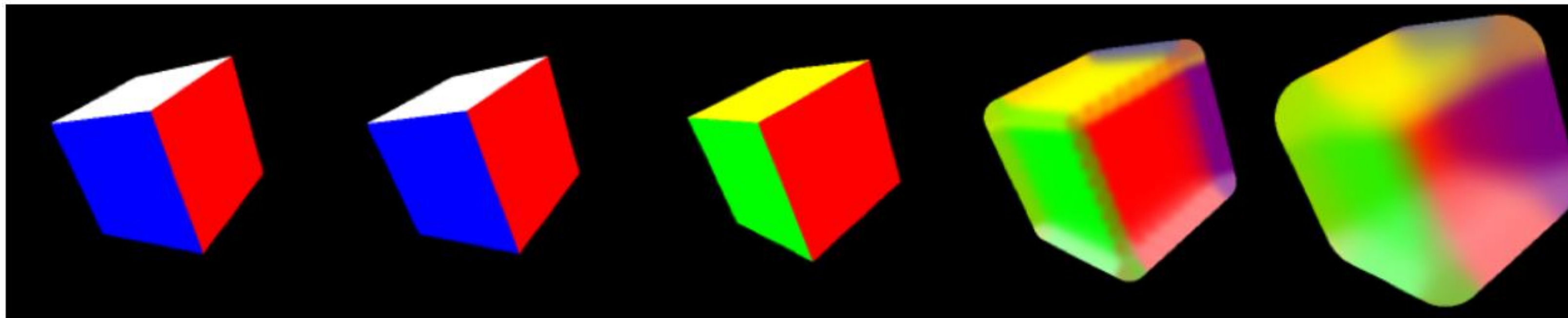


Multi-view silhouette difference



Deformed mesh

Applications – Rigid Pose Estimation



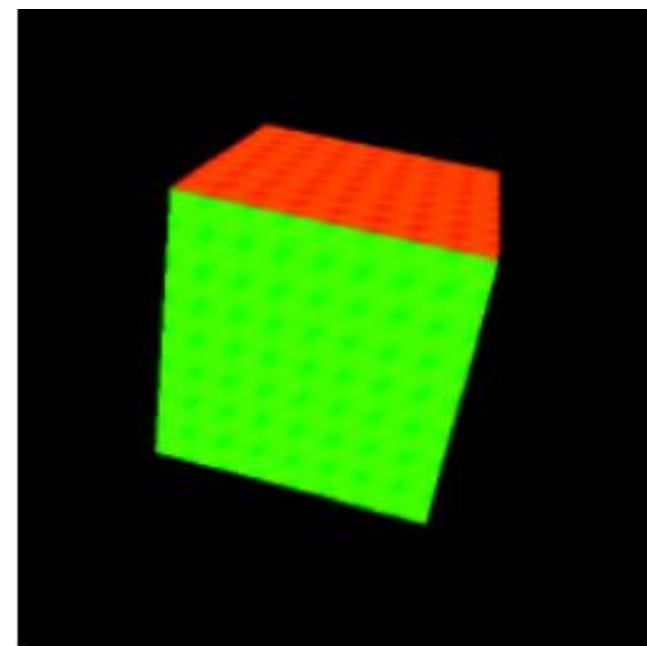
Target

Our Result

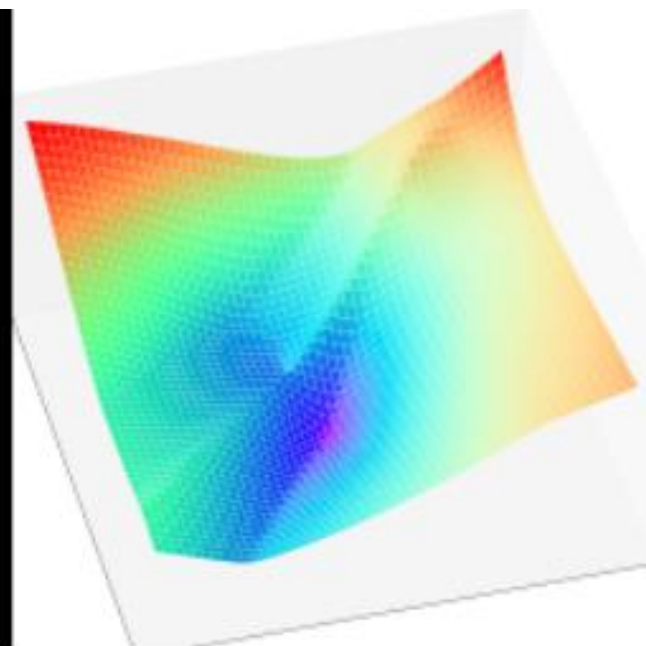
NMR Result

Smooth
rendering

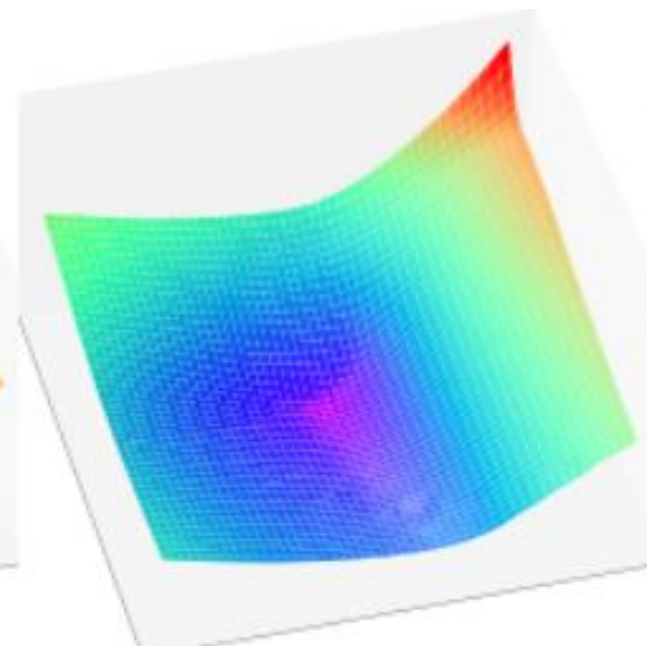
Smoother
rendering



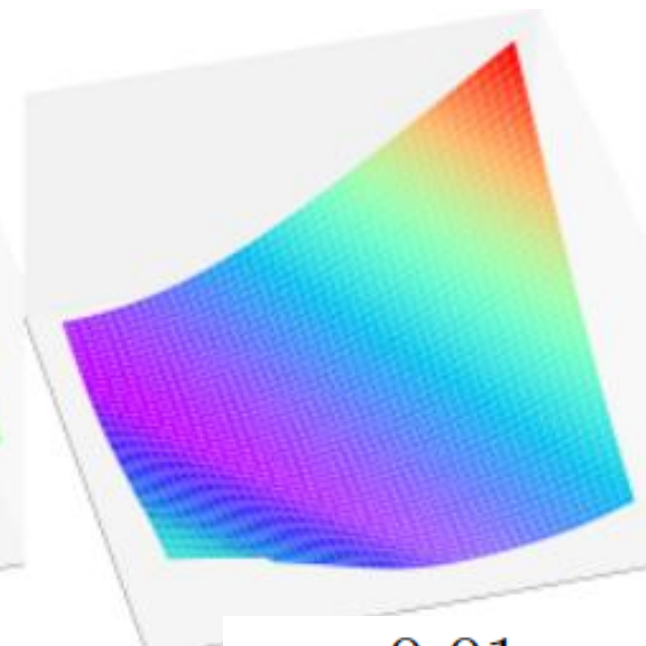
Initialization



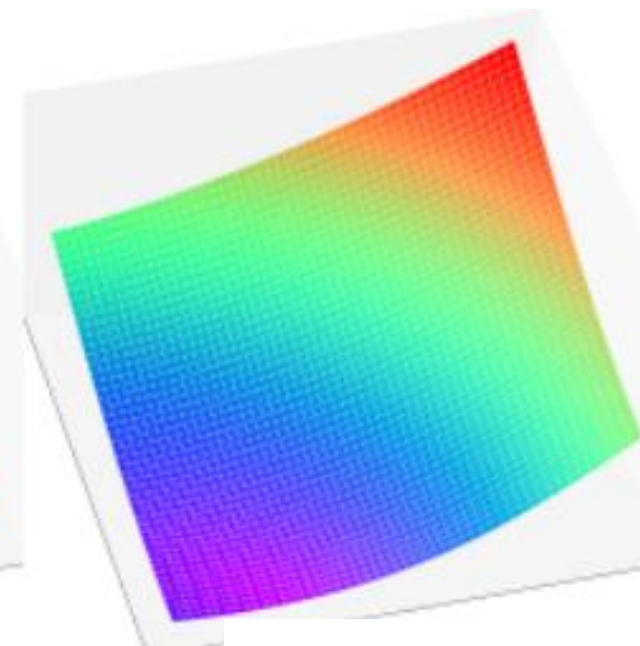
Global minimum



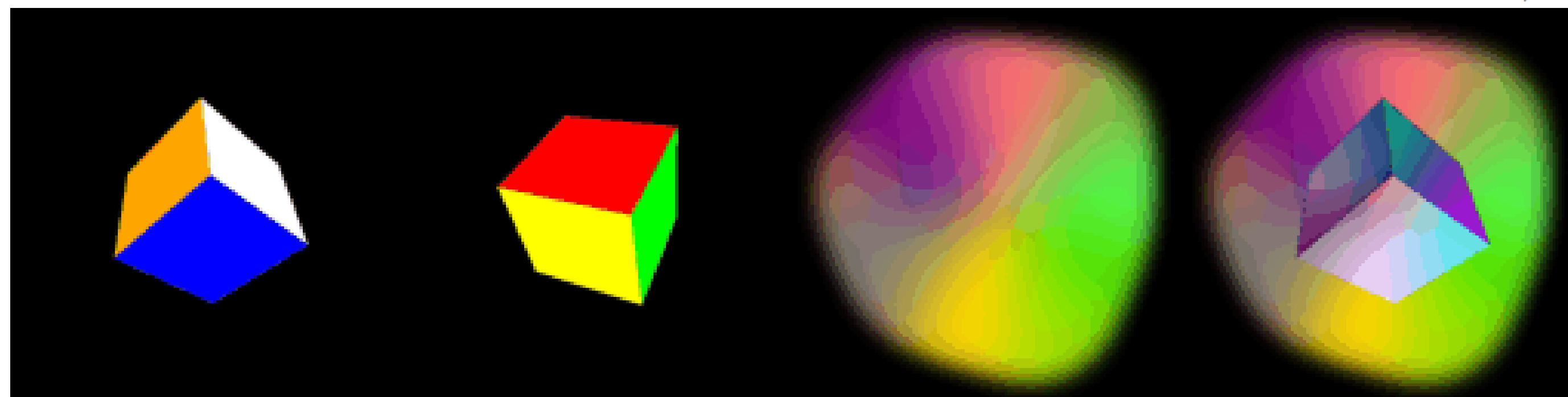
Local minimum



$\sigma = 0.01$
 $\gamma = 0.1$



$\sigma = 0.03$
 $\gamma = 0.3$



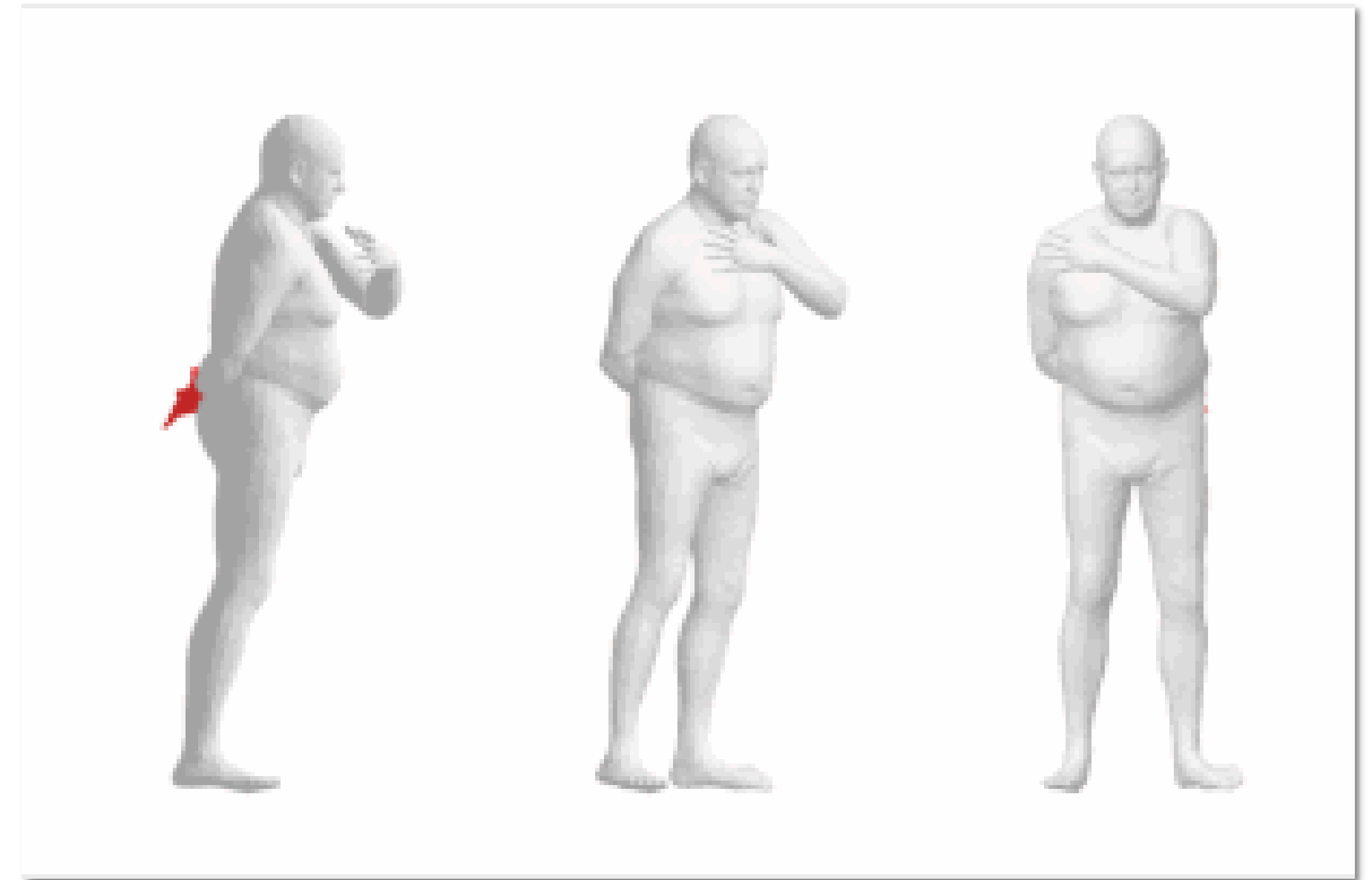
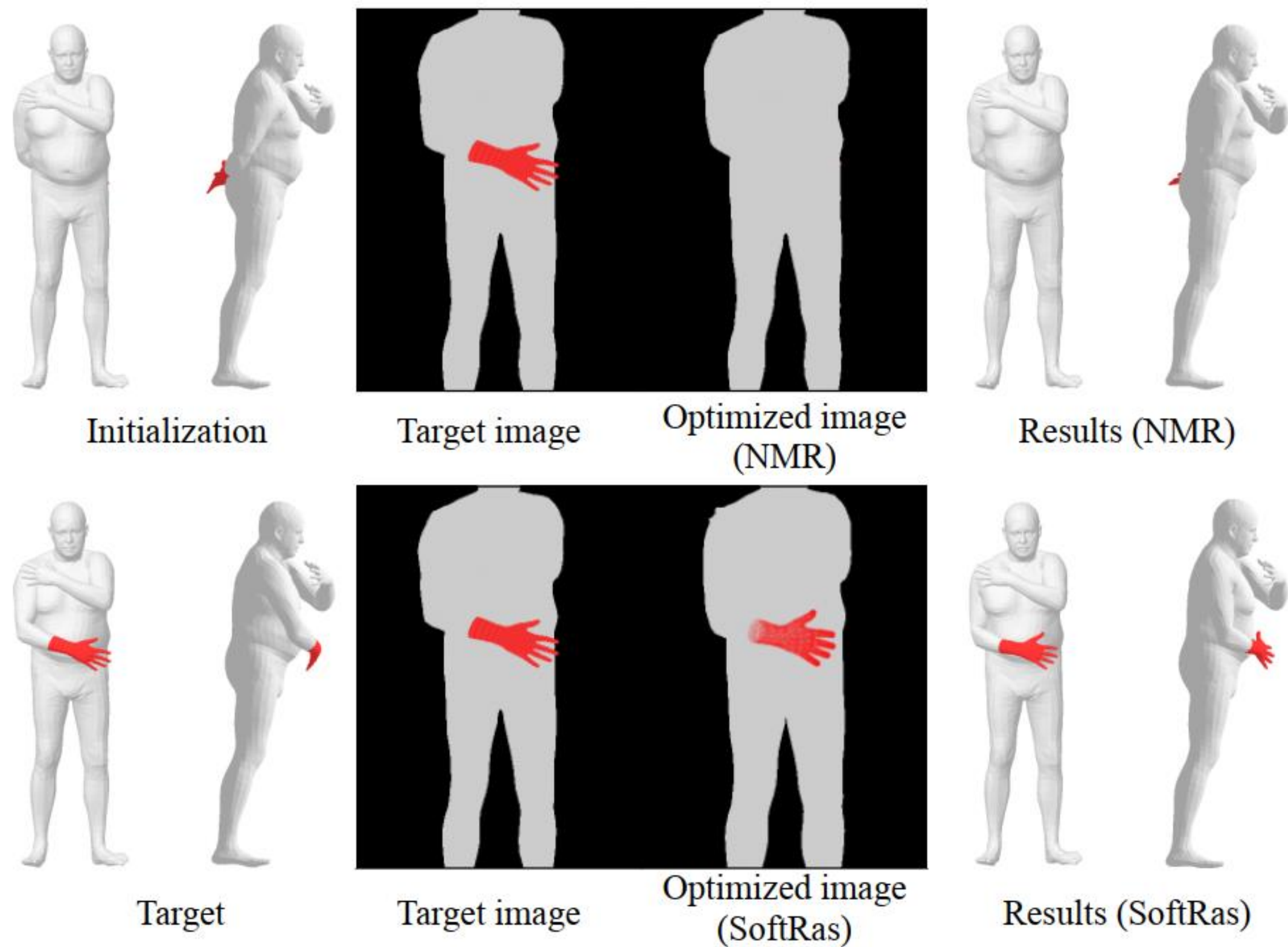
Target

Result pose

Rendering

Error Map

Applications – Non-Rigid Pose Estimation



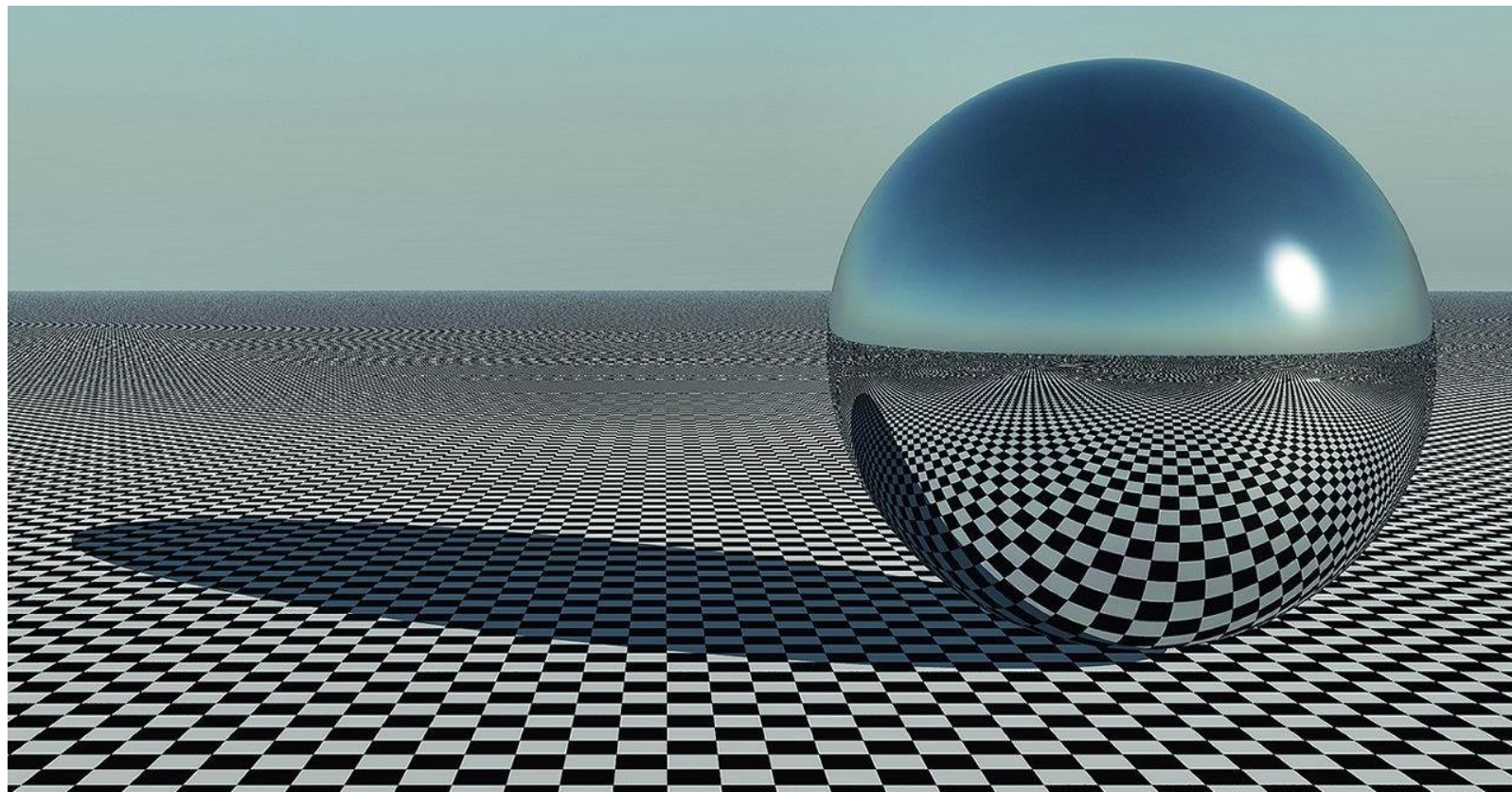
Non-Rigid Pose Optimization

Differentiable Rendering for Implicit Surface

Learning to Infer Implicit Surfaces without 3D Supervision, NeurIPS'19

What is Implicit Surface?

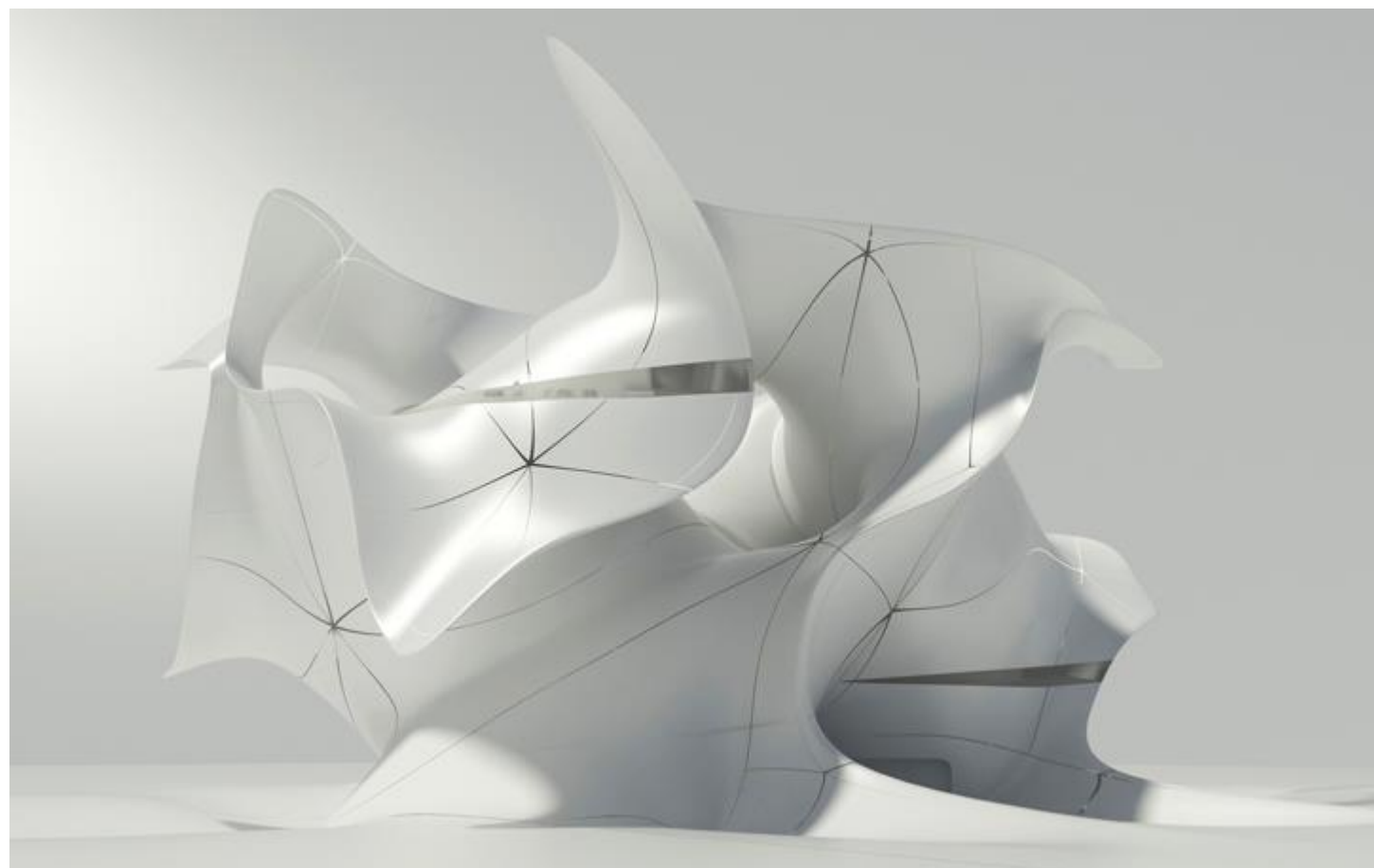
How to define a unit sphere?



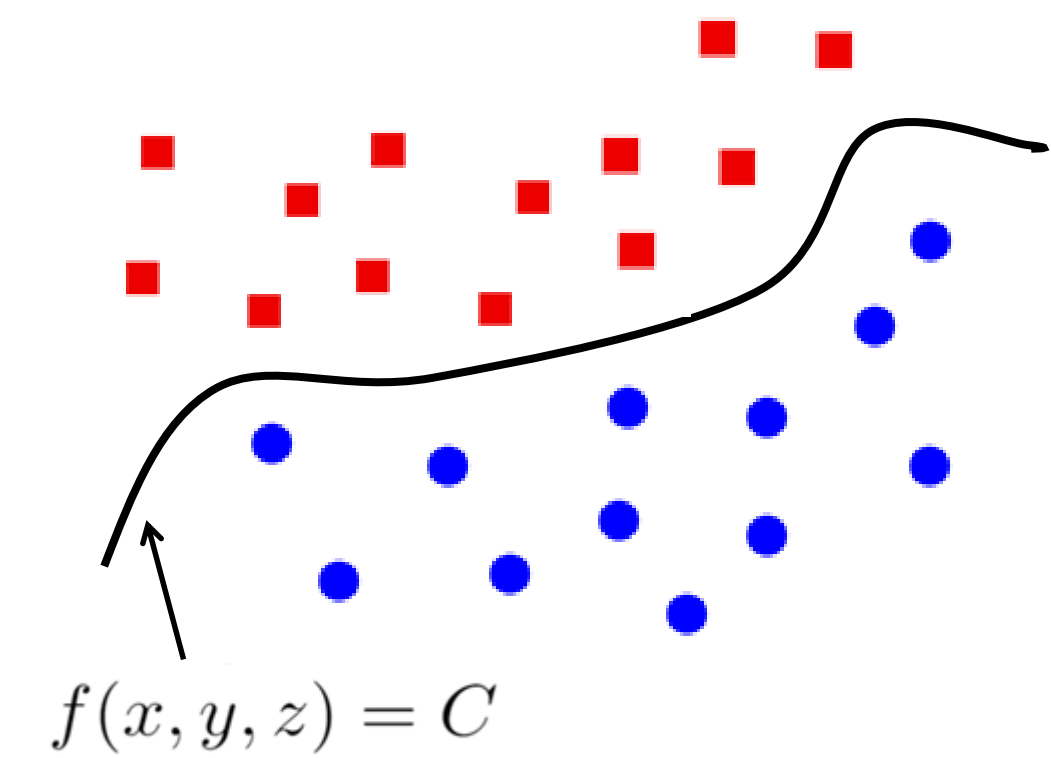
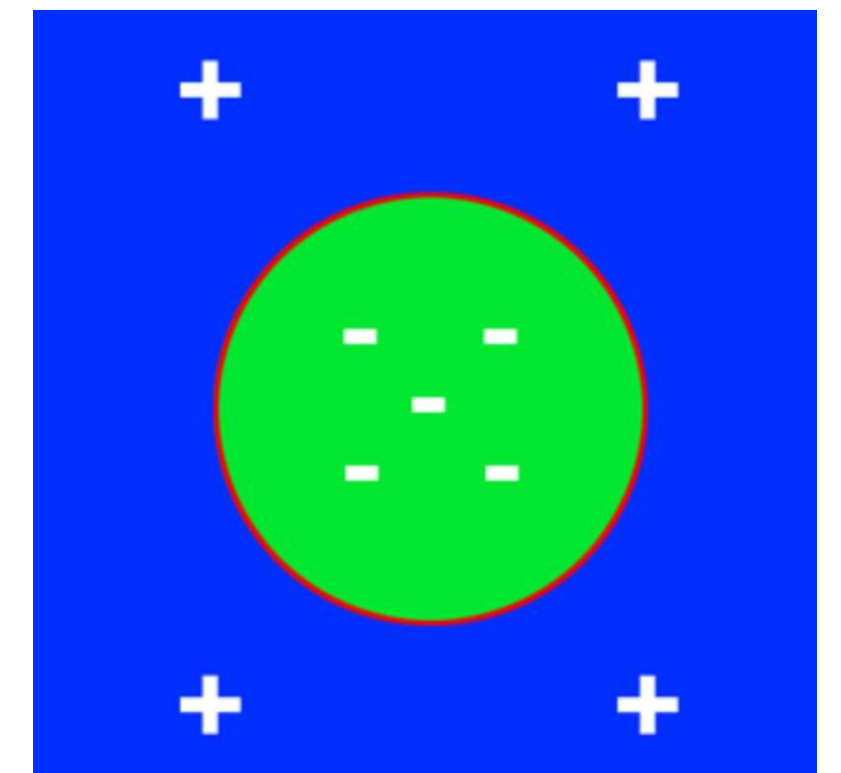
$$\underline{x^2 + y^2 + z^2} - \underline{1} = \underline{0}$$



$$f(x, y, z) = C$$



Iso-surface



Implicit surface can be instantiated as mesh using Marching Cube algorithm.

Implicit Surface v.s. Explicit Representations

Explicit Representations



Voxel

+Topology

-Fidelity



Point cloud

+Topology

-Fidelity



Mesh

-Topology

+Fidelity

Implicit Surface



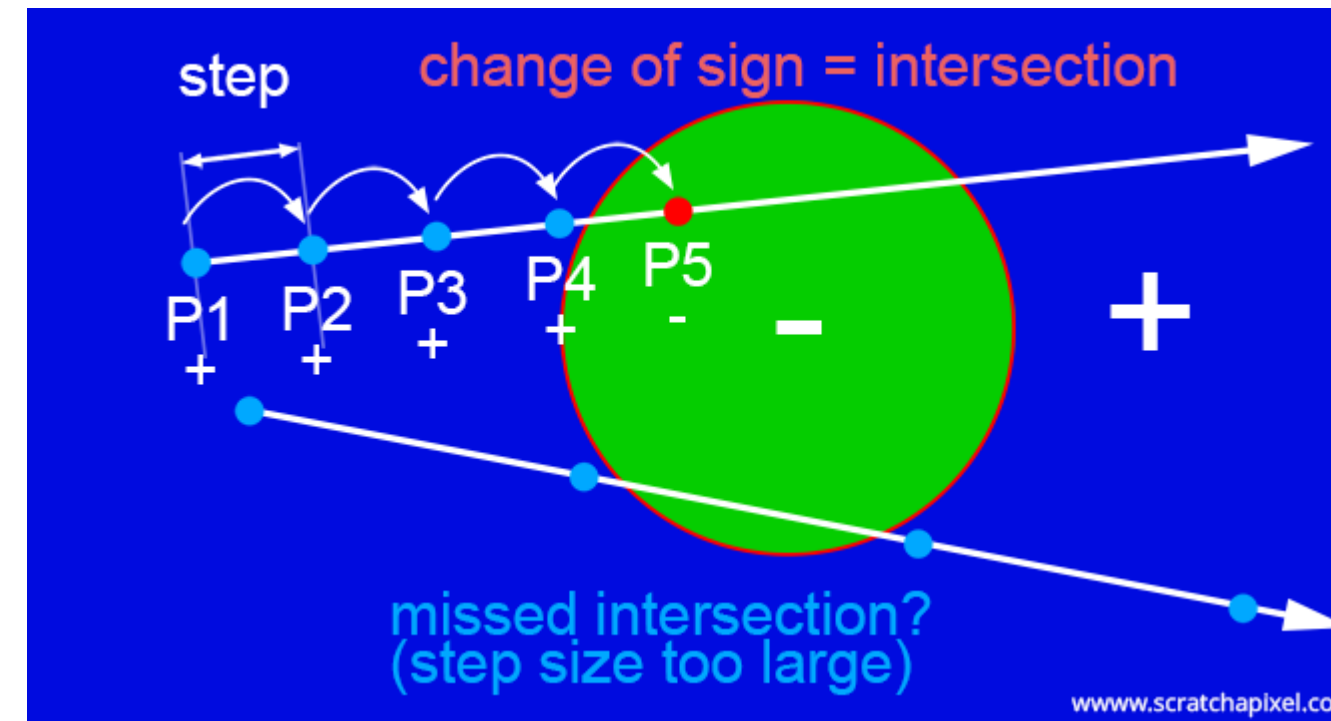
Occupancy field

+Topology

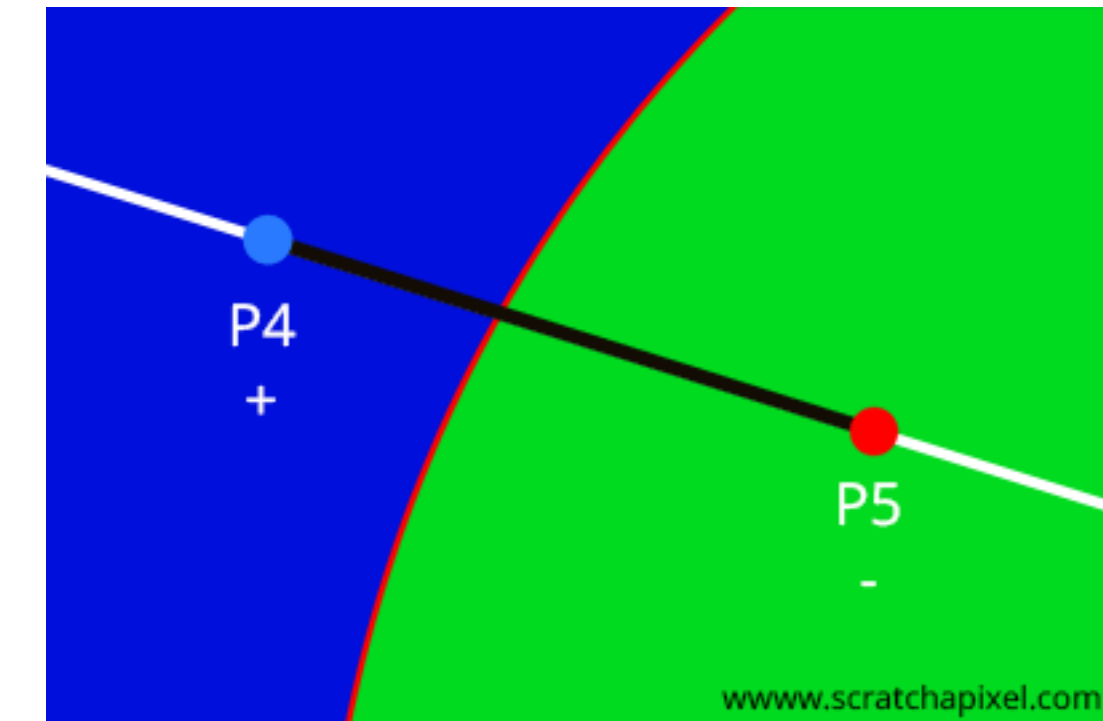
+Fidelity

Conventional Technique for Implicit Surface Rendering

Ray marching

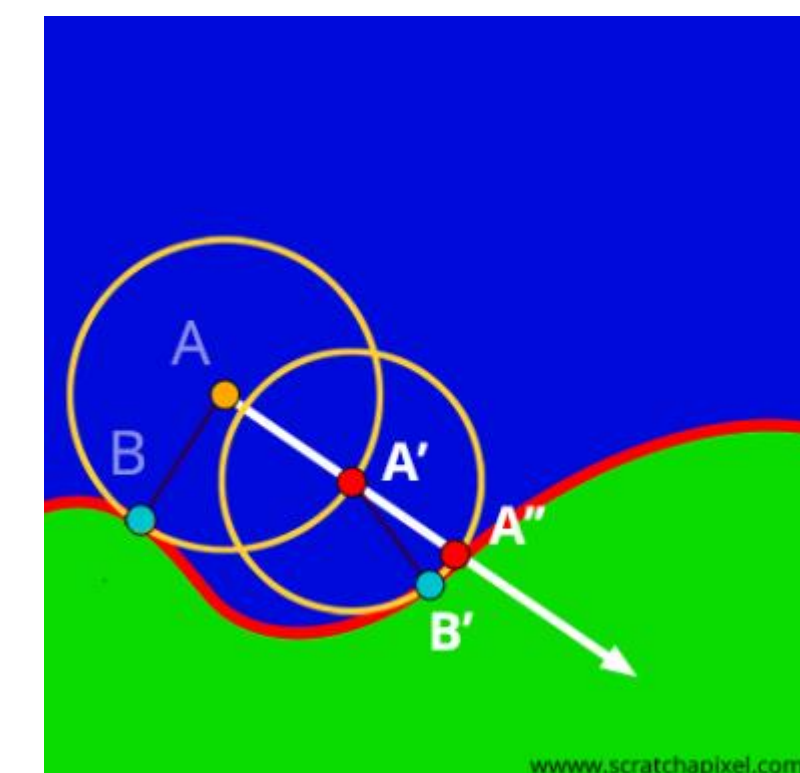
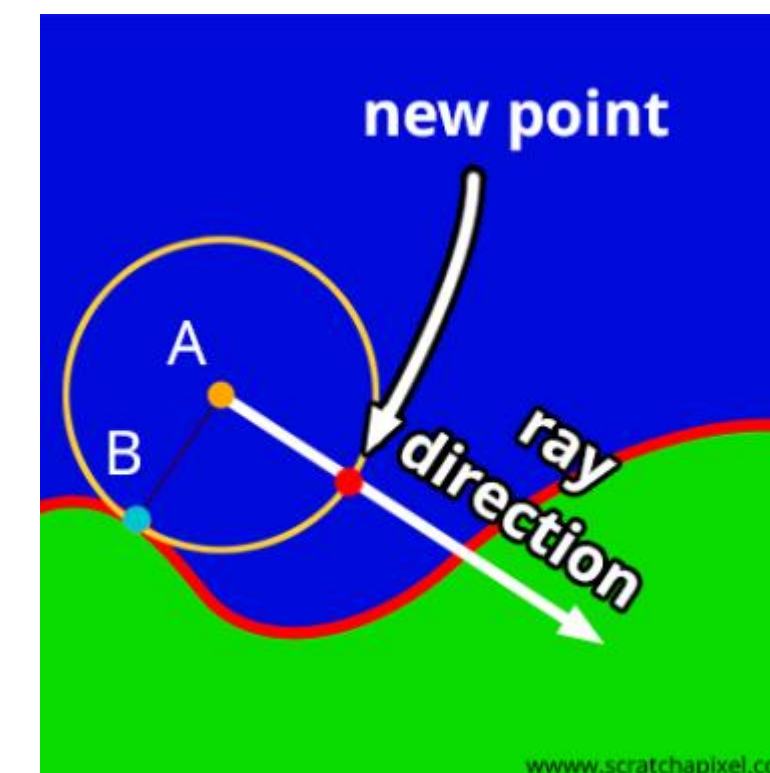
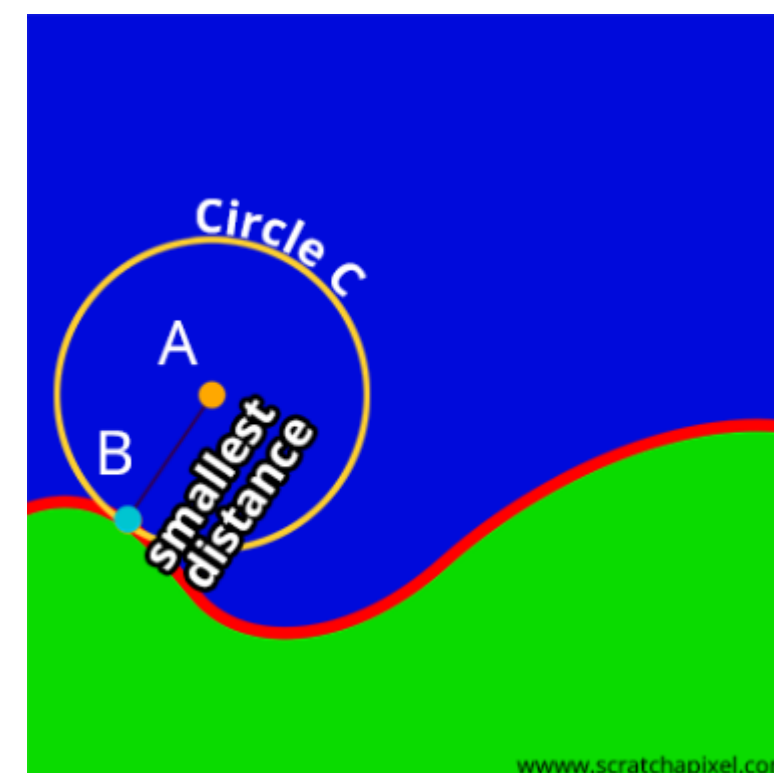


line search



binary search

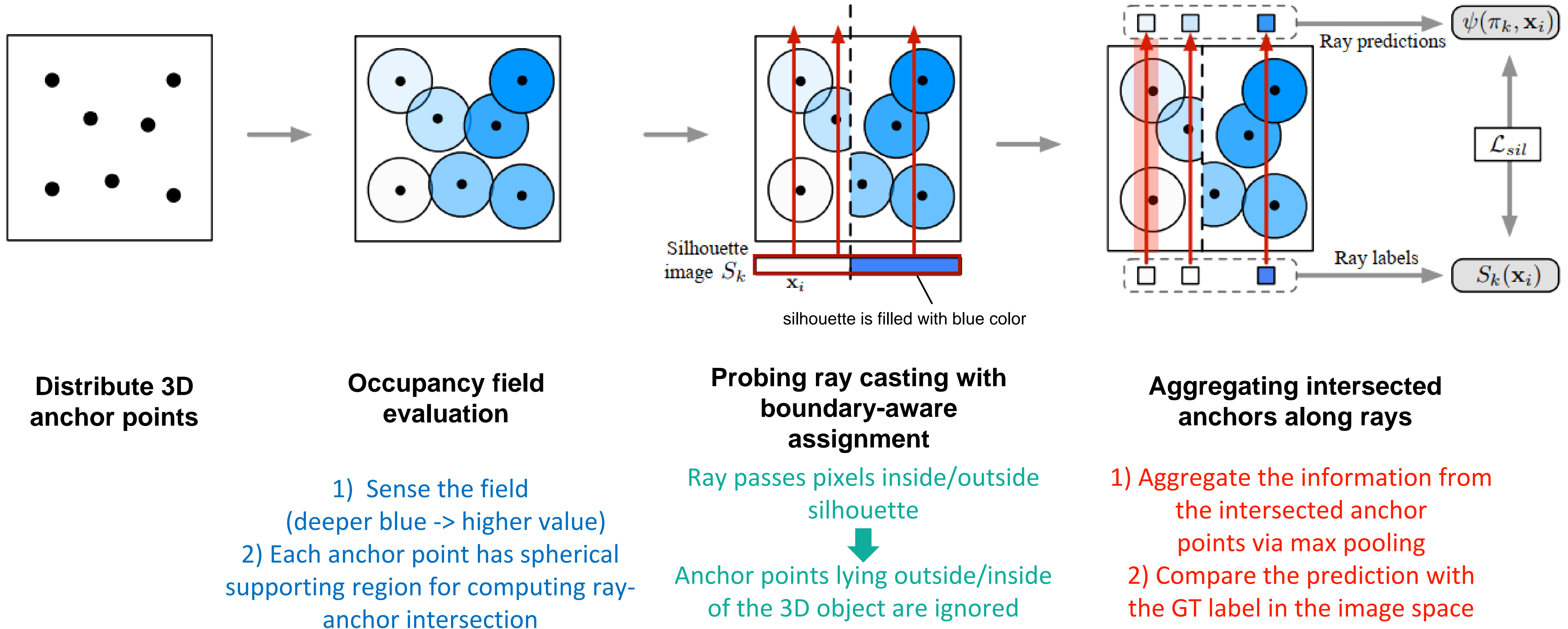
Sphere tracing



Time consuming and Non-differentiable!

Proposed Differentiable Implicit Renderer

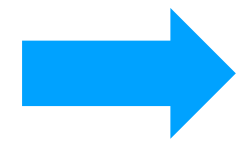
Ray-based Field Probing Technique



Importance Sampling

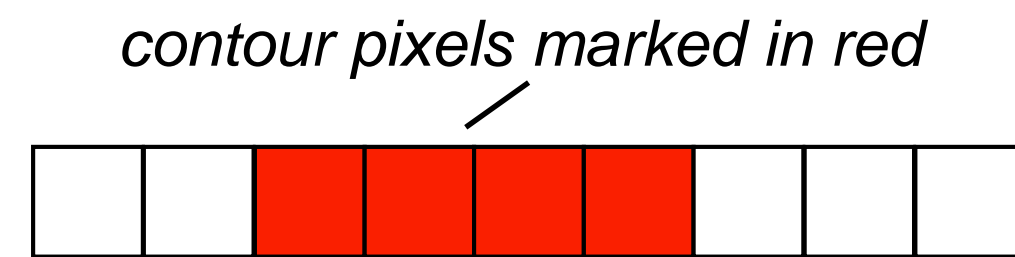
How to effectively sample anchor points and probing rays?

Sampling on 2D Image

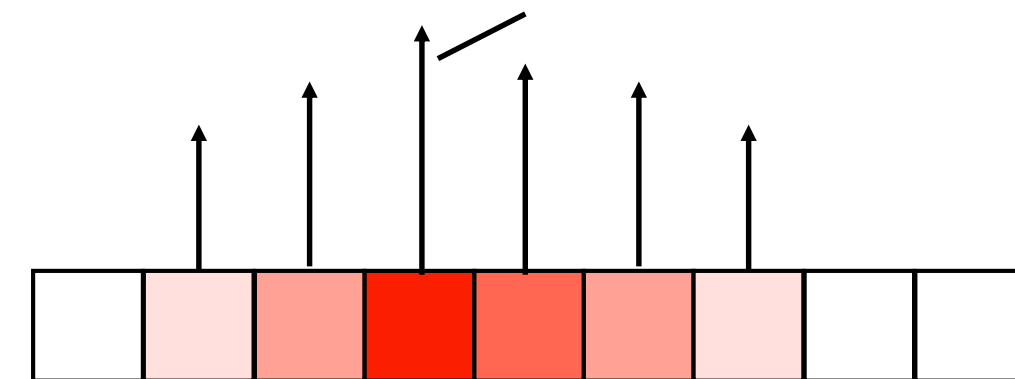


Importance sampling based on Gaussian mixture distribution computed from 2D object silhouette

2D Contour map visualized in 1D

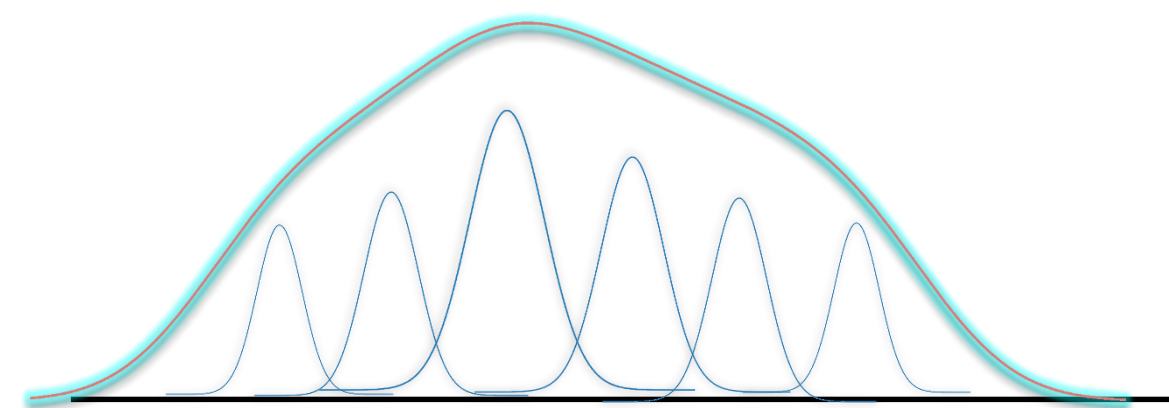


Magnitude of pixel intensity



Apply Gaussian smoothing

Generate Gaussian mixture distribution based on the obtained pixel intensity

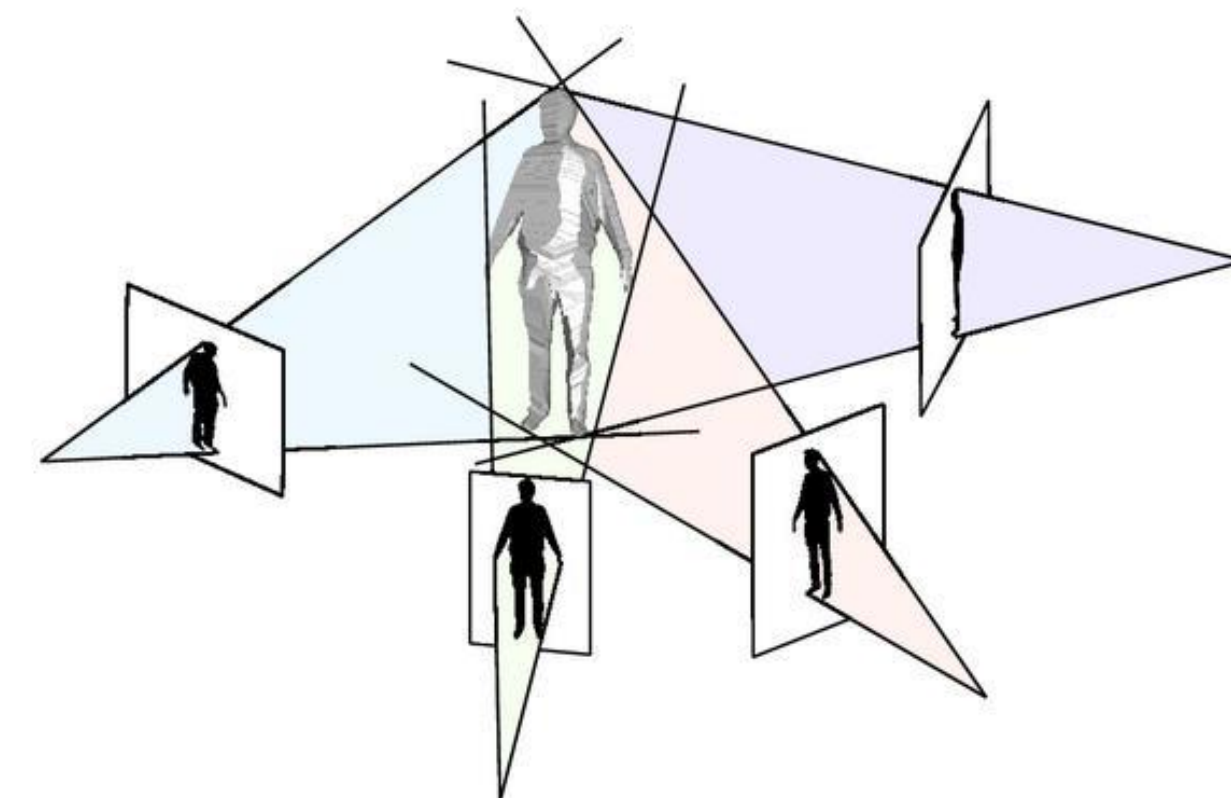


Draw 2D samples from the resulted distribution



Similar Sampling Strategy applied to 3D Anchor points

3D Contour is computed as the boundary of the visual hull



Geometric Regularization for Implicit Surface

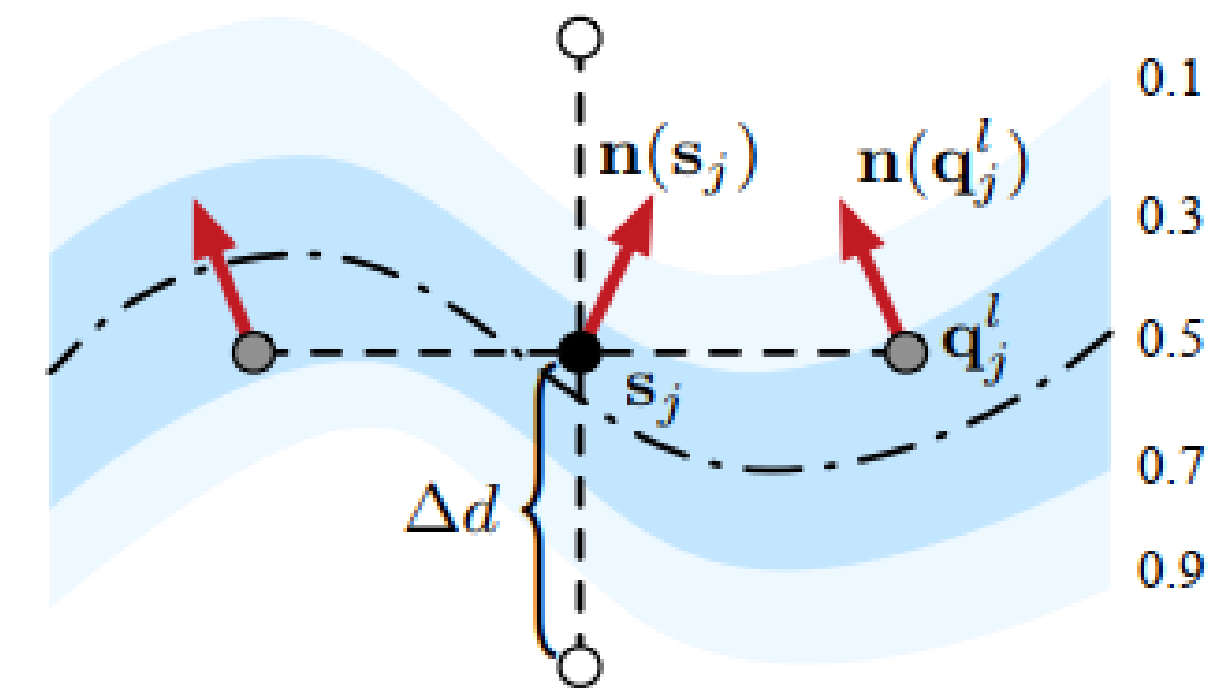
Regularizing geometric properties of implicit surface is challenging due to the **lack of explicit geometric entity**.

Implicit surface derivatives based on finite difference:

$$\frac{\delta^n \phi}{\delta \mathbf{p}_j^n} = \frac{1}{\Delta d^n} \sum_{l=0}^n (-1)^l \binom{n}{l} \phi(\mathbf{p}_j + (\frac{n}{2} - l)\Delta d) \quad \longrightarrow \quad \text{Used to compute **normal** and other **high-order derivatives** at point } \mathbf{p}_j$$

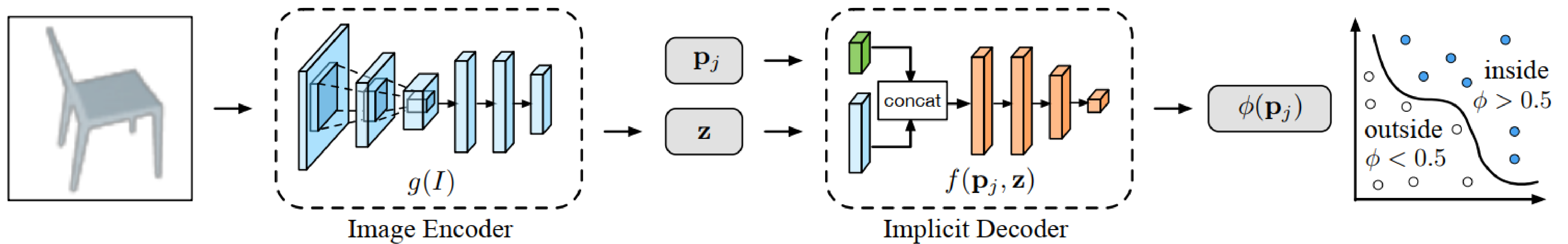
Geometric regularization based on Importance Weighting:

$$\mathcal{L}_{geo} = \frac{1}{N_p} \sum_{j=1}^{N_p} W(\phi(\mathbf{s}_j)) \frac{\sum_{l=1}^6 W(\phi(\mathbf{q}_j^l)) \|\mathbf{n}(\mathbf{s}_j) - \mathbf{n}(\mathbf{q}_j^l)\|_p^p}{\sum_{l=1}^6 W(\phi(\mathbf{q}_j^l))}$$



Unsupervised Learning of Implicit Surfaces

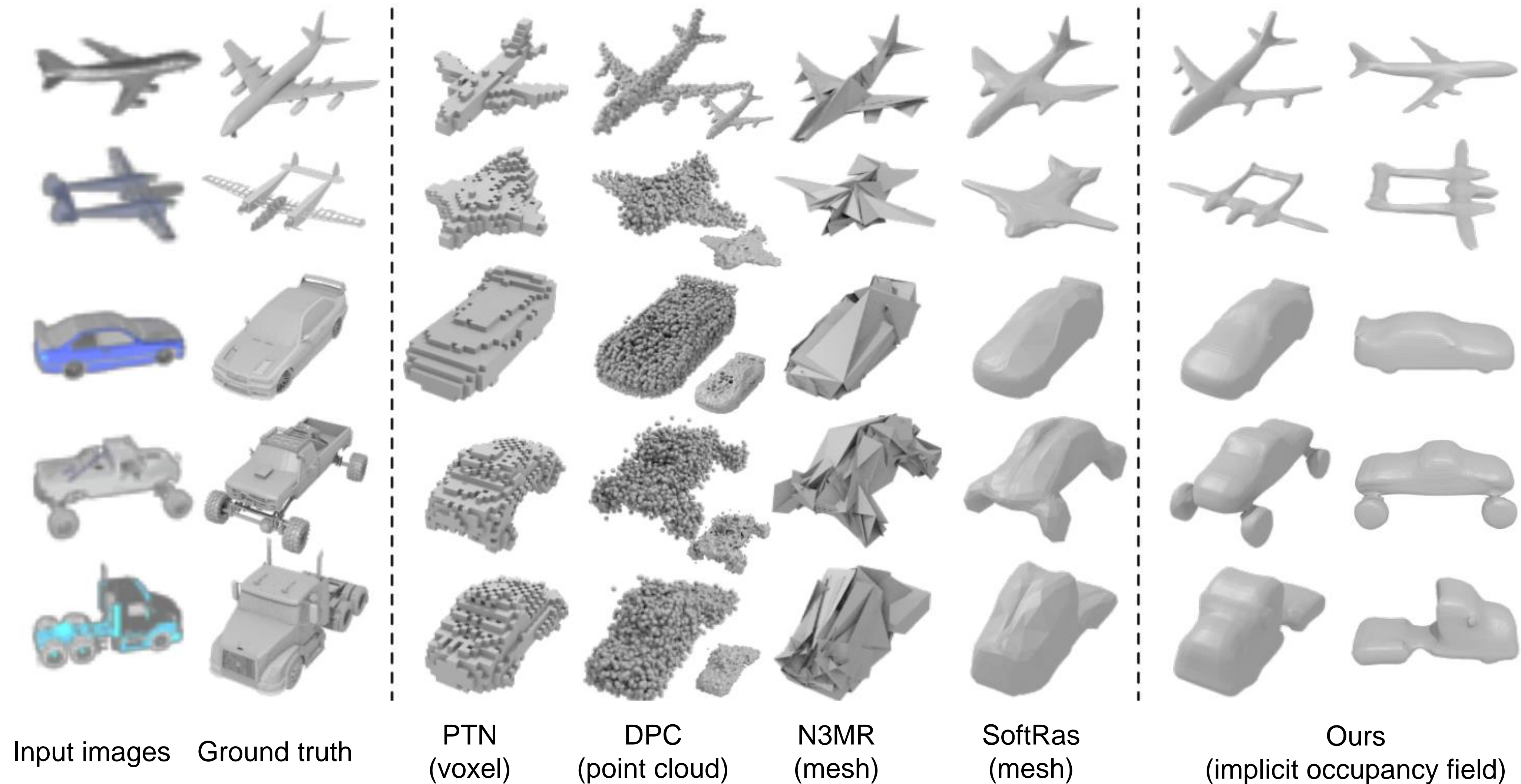
Network Structure



Loss function $\mathcal{L} = \mathcal{L}_{sil} + \lambda \mathcal{L}_{geo}$

Results

Qualitative Results of Single-view Reconstruction using Different Surface Representations

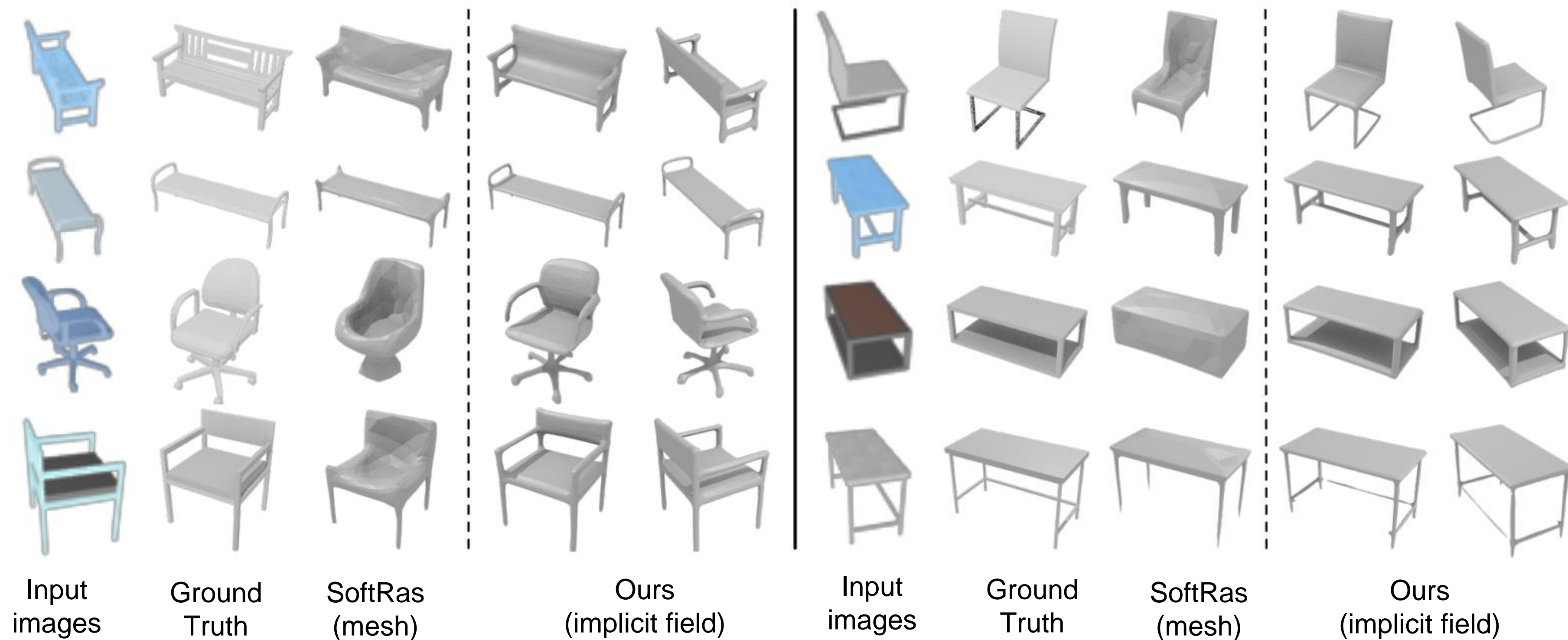


Results

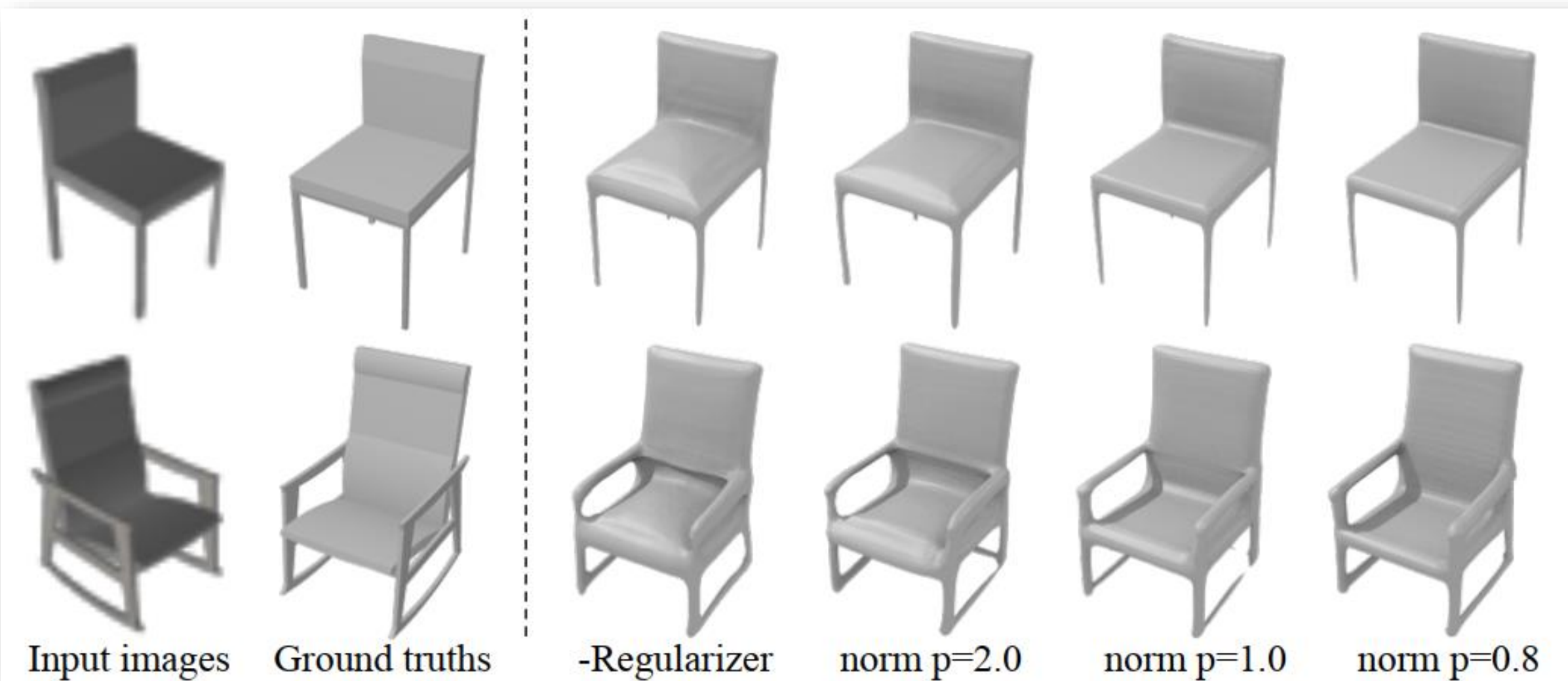
Comparisons of 3D IoU with Other Unsupervised Methods

Category	Airplane	Bench	Table	Car	Chair	Boat	Mean
PTN [4]	0.5564	0.4875	0.4938	0.7123	0.4494	0.5507	0.5417
NMR [1]	0.6172	0.4998	0.4829	0.7095	0.4990	0.5953	0.5673
SoftRas [2]	0.6419	0.5080	0.4487	0.7697	0.5270	0.6145	0.5850
Ours	0.6510	0.5360	0.5150	0.7820	0.5480	0.6080	0.6067

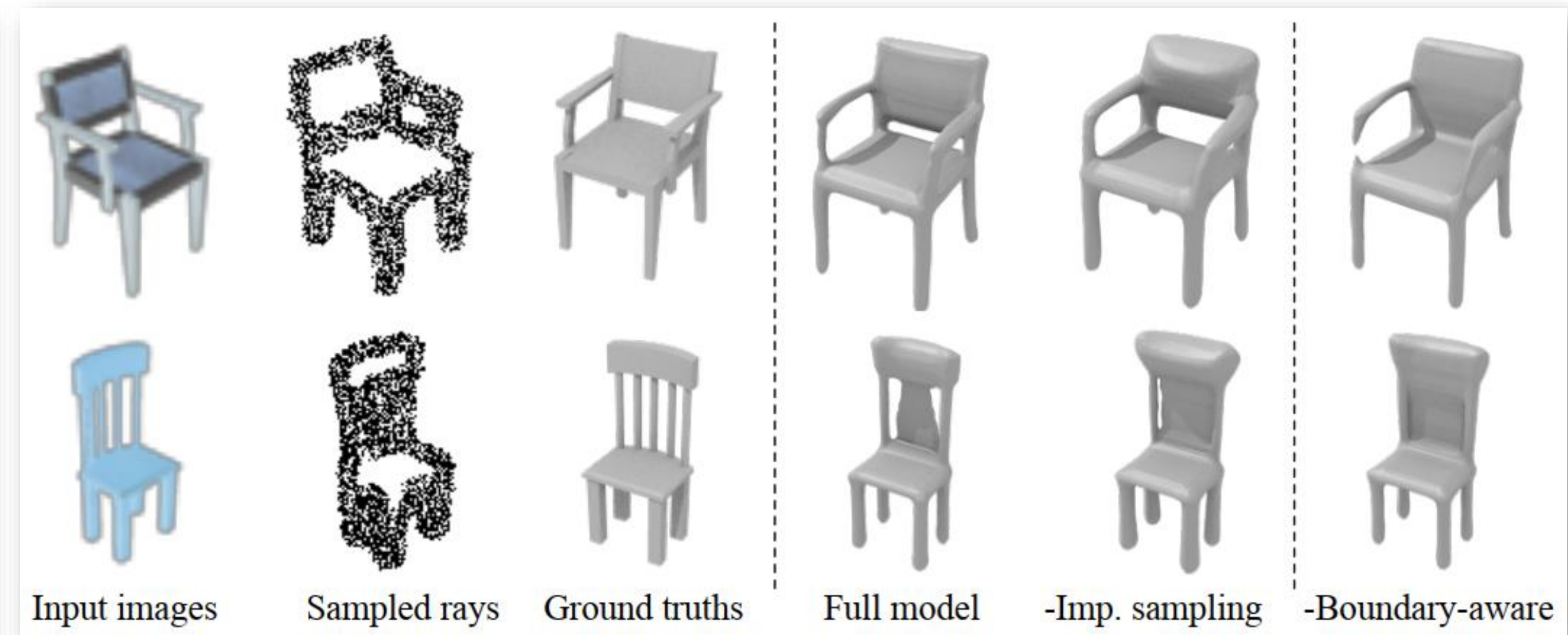
Qualitative comparisons with mesh-based approach in term of modeling capability



Ablation Analysis



**Qualitative evaluations of geometric regularization
by using different configurations**



**Qualitative analysis of importance sampling and boundary-
aware assignment for single-view reconstruction**

Conclusions

Soft Rasterizer: A Differentiable Renderer for Image-based 3D Reasoning

- A new differentiable rendering framework that can directly render a given mesh in a fully differentiable manner
- Formulate the conventional discrete operations – rasterization and z-buffering, as differentiable probabilistic processes
- Can flow gradients from image to unseen vertices and the z coordinates of the mesh triangles
- Applied to 3D unsupervised single-view reconstruction and image-based shape fitting

Learning to Infer Implicit Surfaces without 3D Supervision

- A new framework that enables learning of implicit surfaces for shape modeling without 3D supervision
- A novel field probing approach based on anchor points and probing rays that efficiently correlates the implicit field and the observed images
- An efficient point and ray sampling method for implicit surface generation from image-based supervision
- A general formulation of geometric regularization that can constrain the geometric properties of a continuous implicit surface

We have open sourced the code of SoftRas!
<https://github.com/ShichenLiu/SoftRas>



PYTORCH

Thank you!