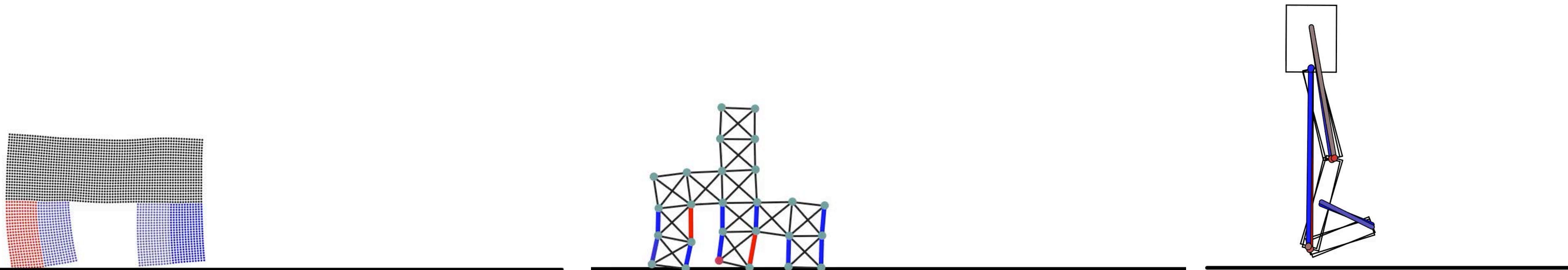


Yuanming Hu, Luke Anderson, Tzu-Mao Li, Qi Sun, Nathan Carr, Jonathan Ragan-Kelley, Fredo Durand
(ICLR 2020)

DiffTaichi: Differentiable Programming for Physical Simulation



End2end optimization of neural network controllers with gradient descent

Yuanming Hu MIT CSAIL

内容概览

- ◆ Taichi项目简介 (10min)
- ◆ DiffTaichi可微编程原理(ICLR 2020, 20min)
- ◆ Tachi与DiffTaichi入门教程 (5min)
- ◆ Q&A (10 min)

Two Missions of the Taichi Project

- ♦ Explore novel language abstractions and compilation approaches for visual computing
- ♦ Practically simplify the process of computer graphics development/deployment

The screenshot shows the GitHub profile for the 'taichi-dev / taichi' repository. The repository has 315 stars, 10.2k forks, and 1k issues. It features tabs for Code, Issues (103), Pull requests (3), Actions, Security, Insights, and Settings. The description highlights Taichi as a productive programming language for portable, high-performance, sparse & differentiable computing, with a link to <http://taichi.graphics>. Topics include differentiable-programming, gpu-programming, graphics, and sparse-computing. Key metrics at the bottom show 5,566 commits, 14 branches, 0 packages, 5 releases, 23 contributors, and an MIT license.

taichi-dev / taichi

Unwatch 315 Unstar 10.2k Fork 1k

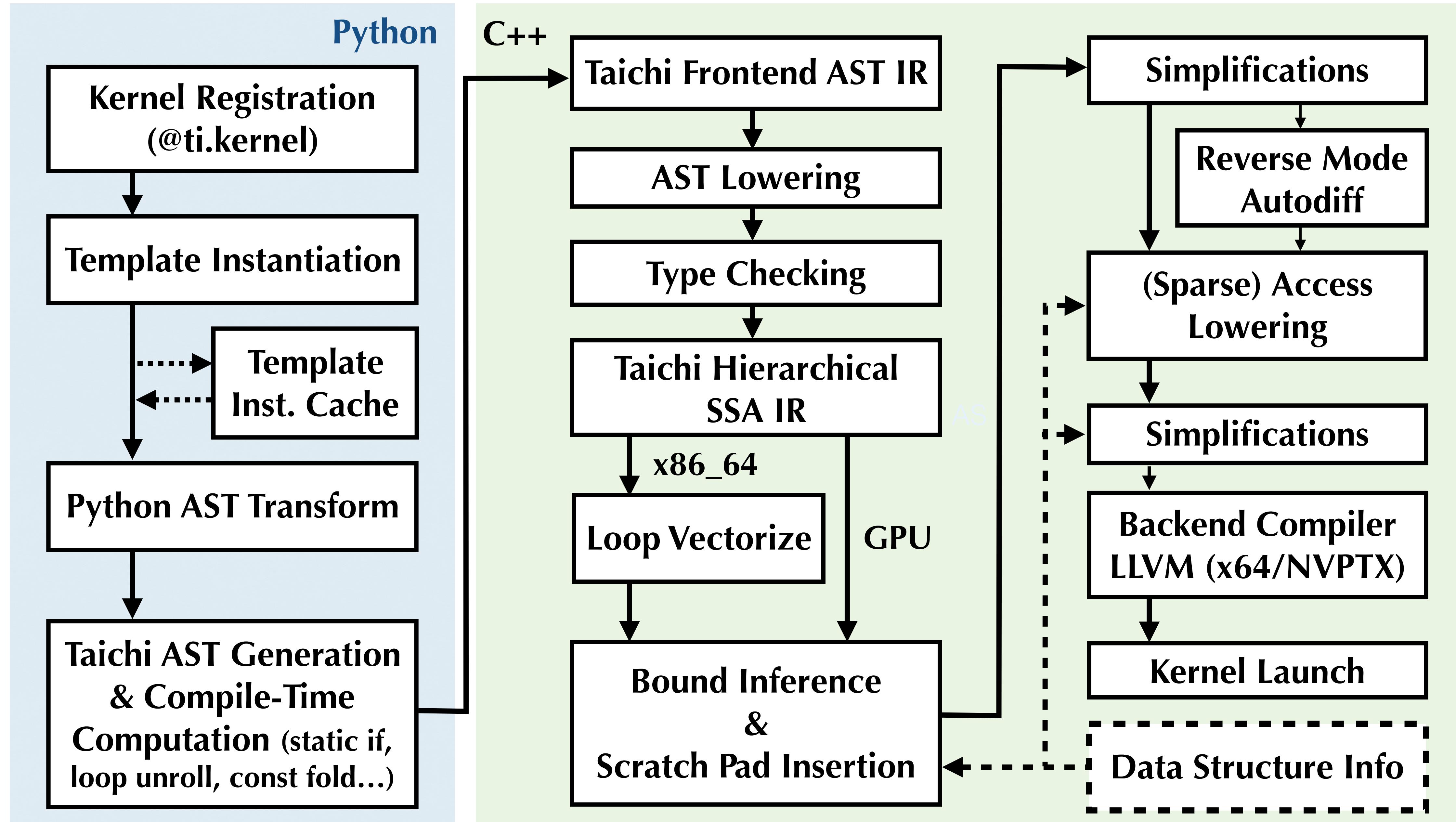
Code Issues 103 Pull requests 3 Actions Security Insights Settings

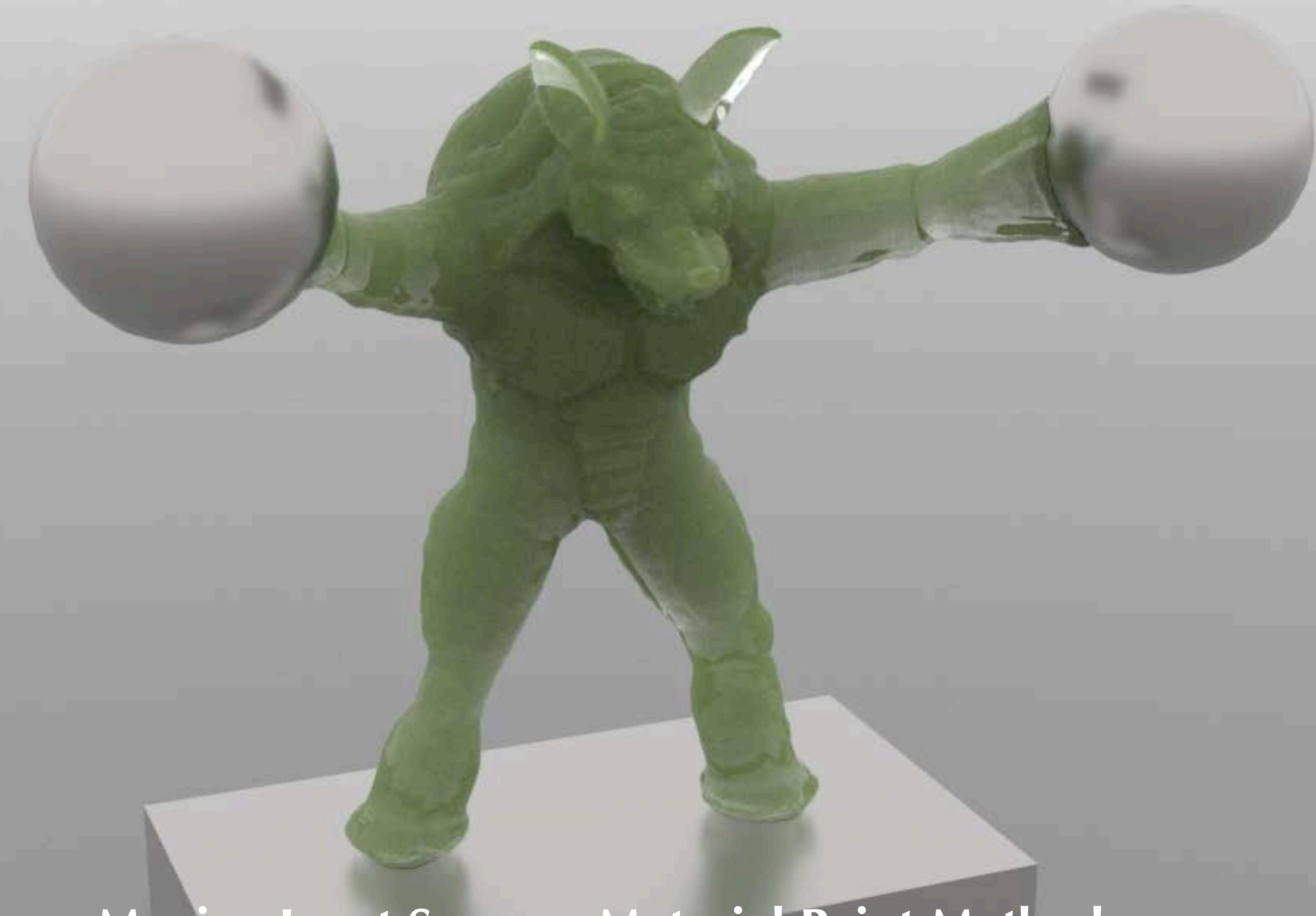
Productive programming language for portable, high-performance, sparse & differentiable computing <http://taichi.graphics>

differentiable-programming gpu-programming graphics sparse-computing Manage topics

5,566 commits 14 branches 0 packages 5 releases 23 contributors MIT

The Life of a Taichi Kernel





Moving Least Squares Material Point Method
Hu, Fang, Ge, Qu, Zhu, Pradhana, Jiang (SIGGRAPH 2018)



Moving Least Squares Material Point Method
Hu, Fang, Ge, Qu, Zhu, Pradhana, Jiang (SIGGRAPH 2018)

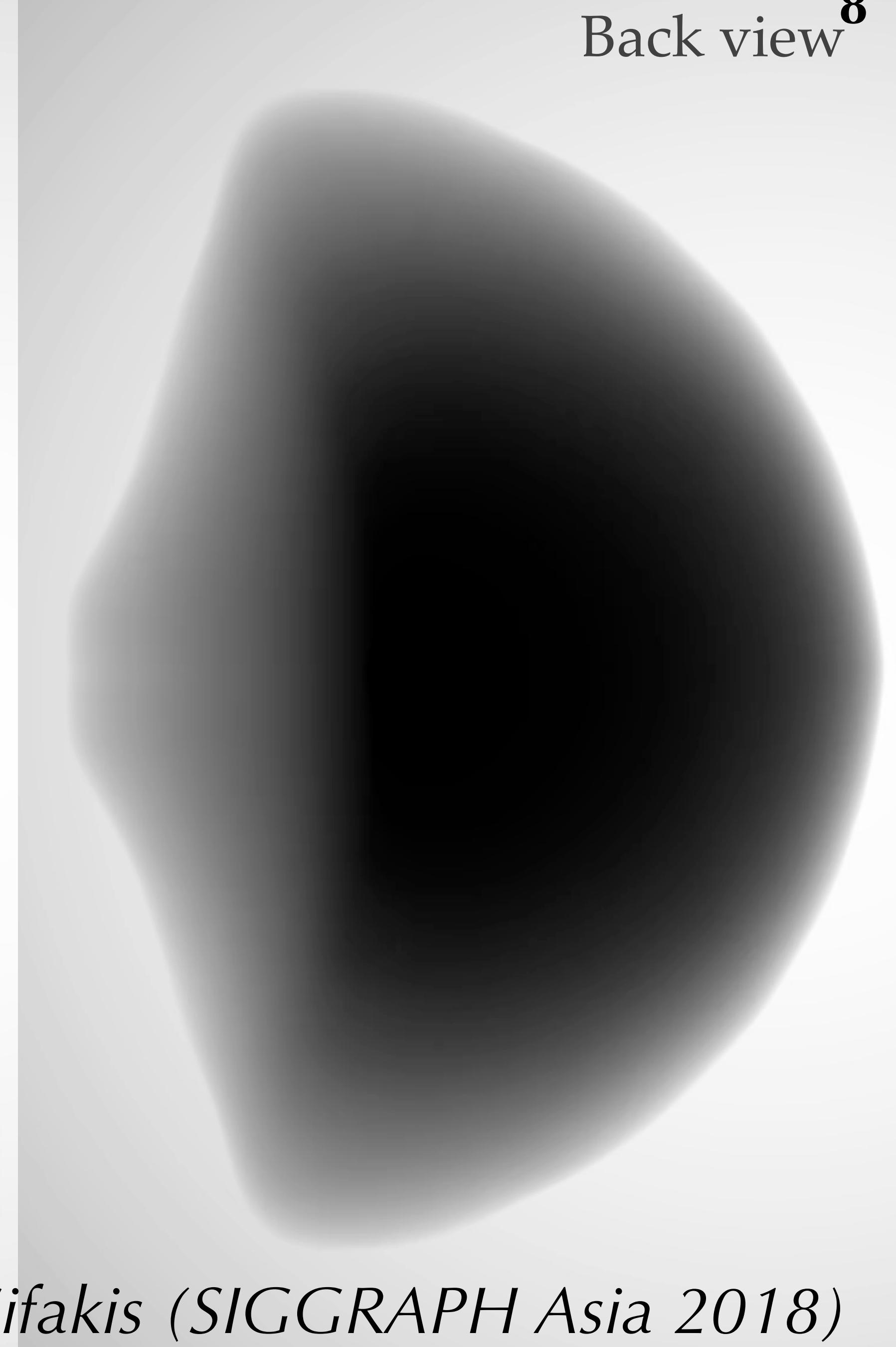
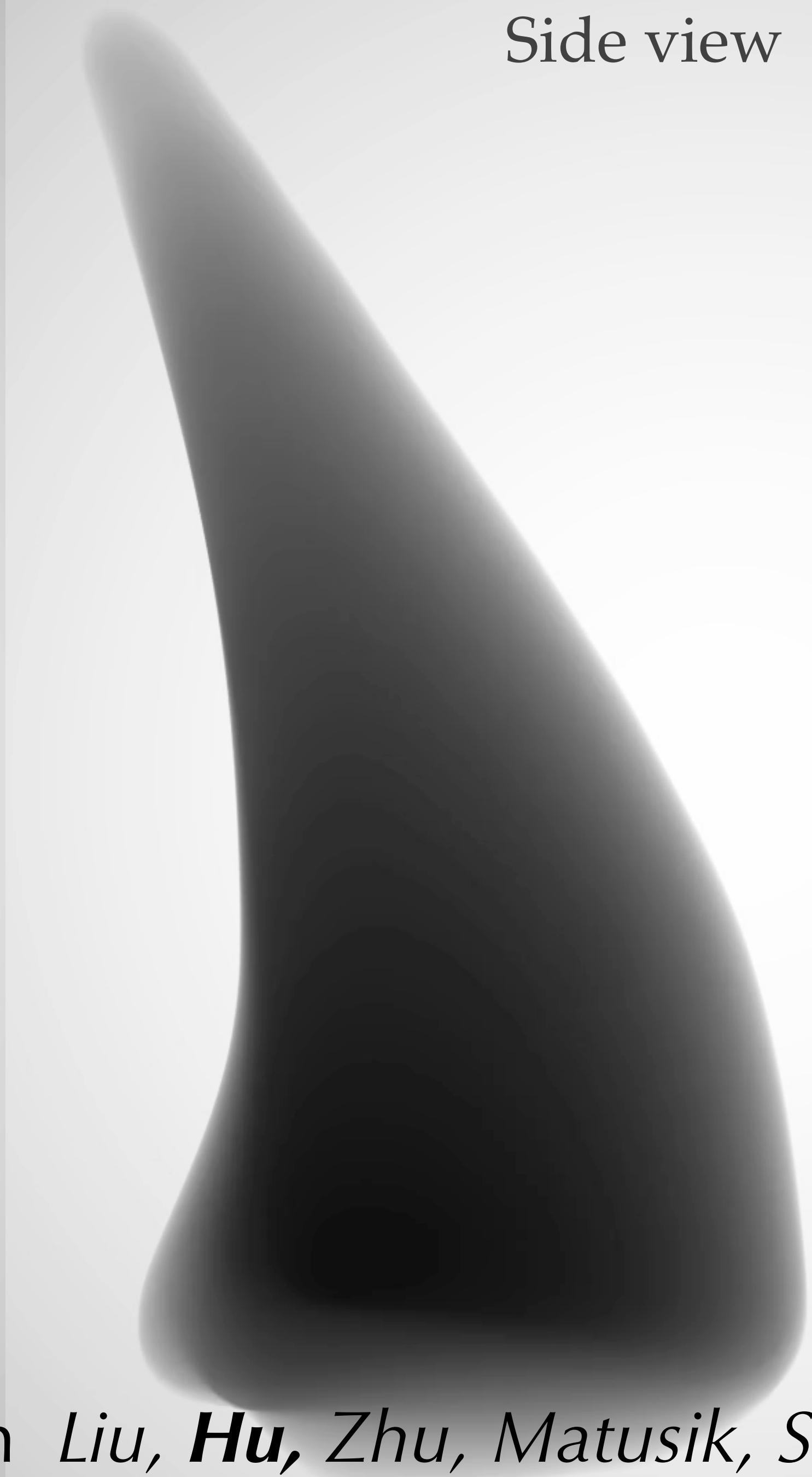
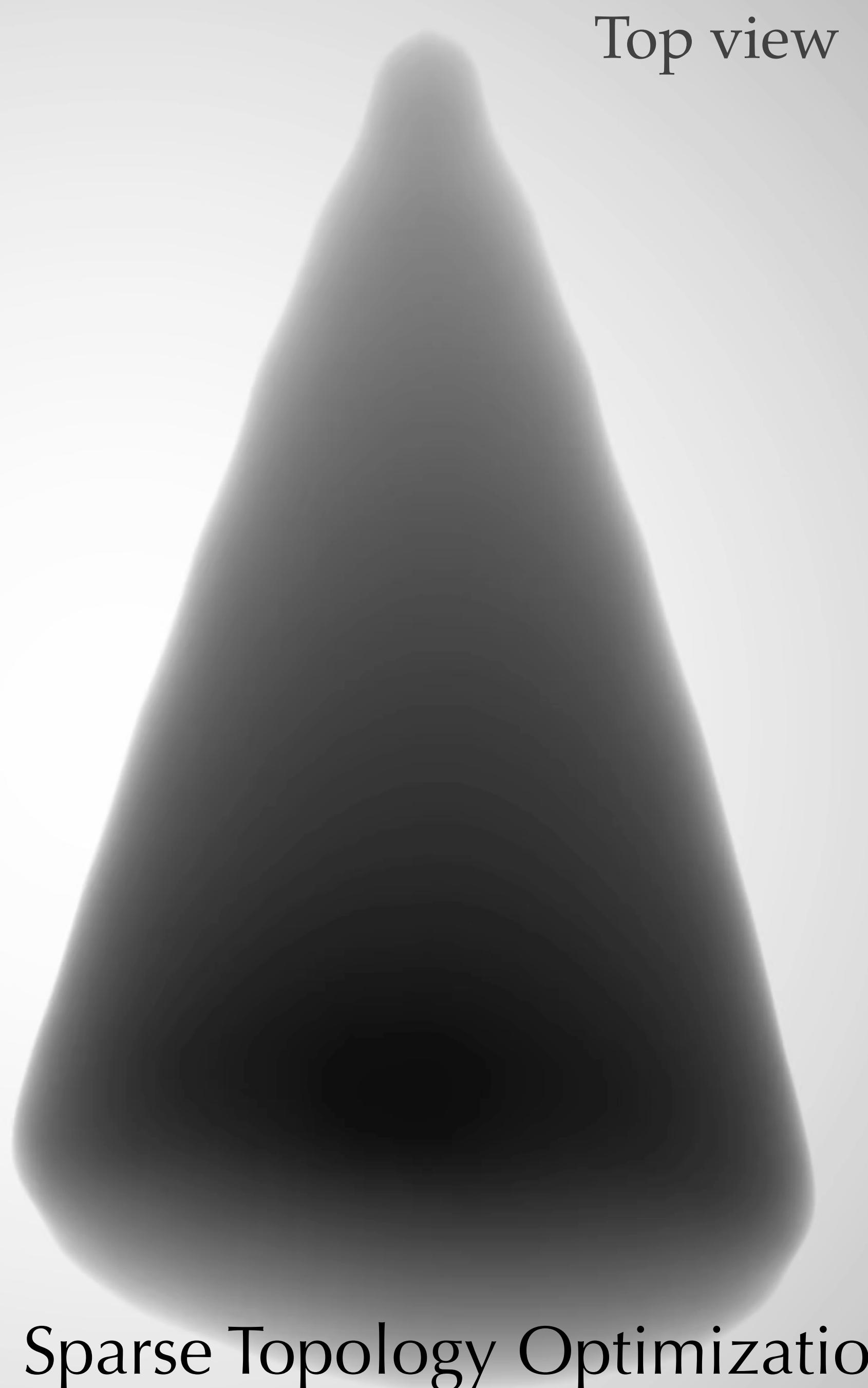


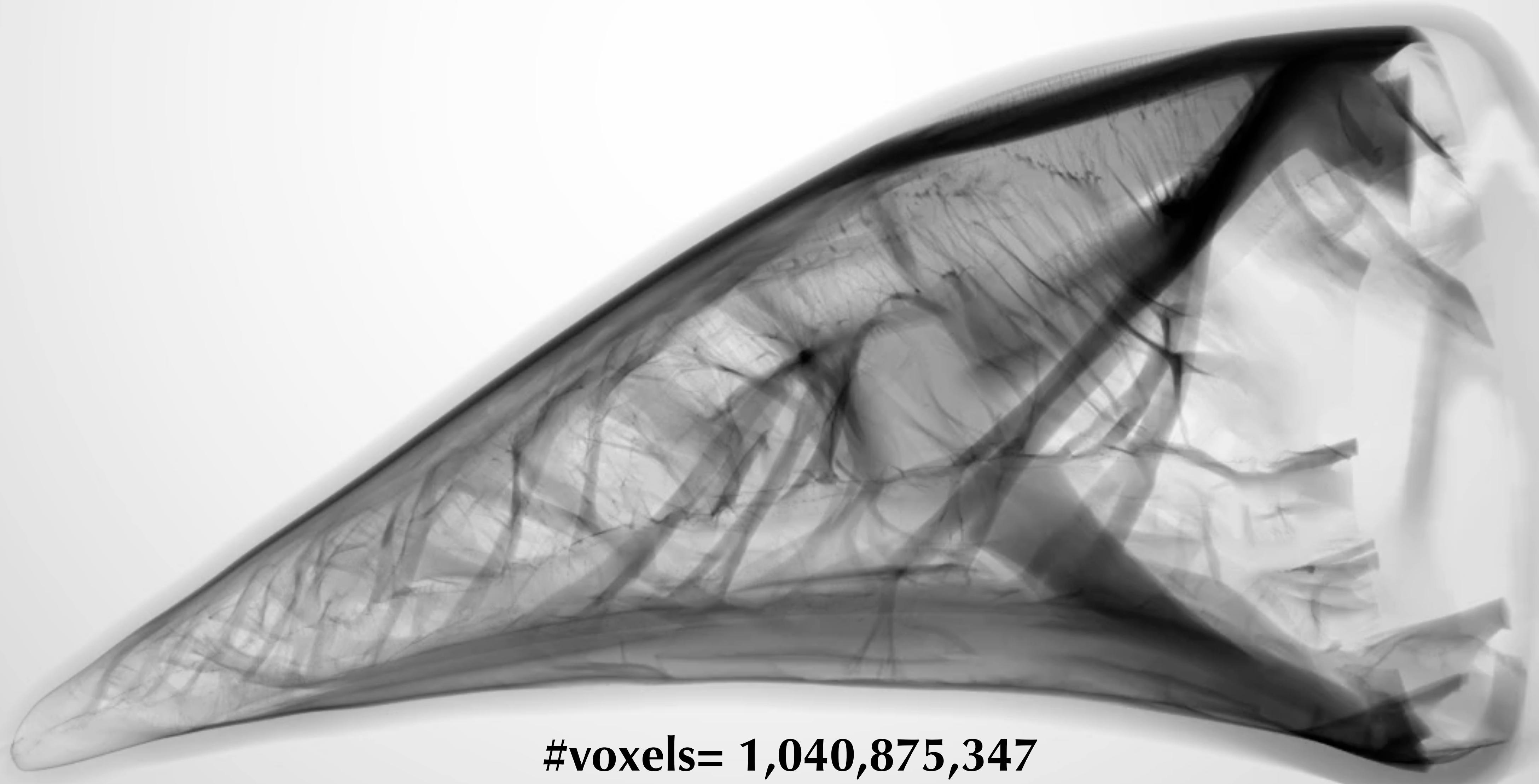
Moving Least Squares Material Point Method
Hu, Fang, Ge, Qu, Zhu, Pradhana, Jiang (SIGGRAPH 2018)

Back view⁸

Side view

Top view





#voxels= 1,040,875,347

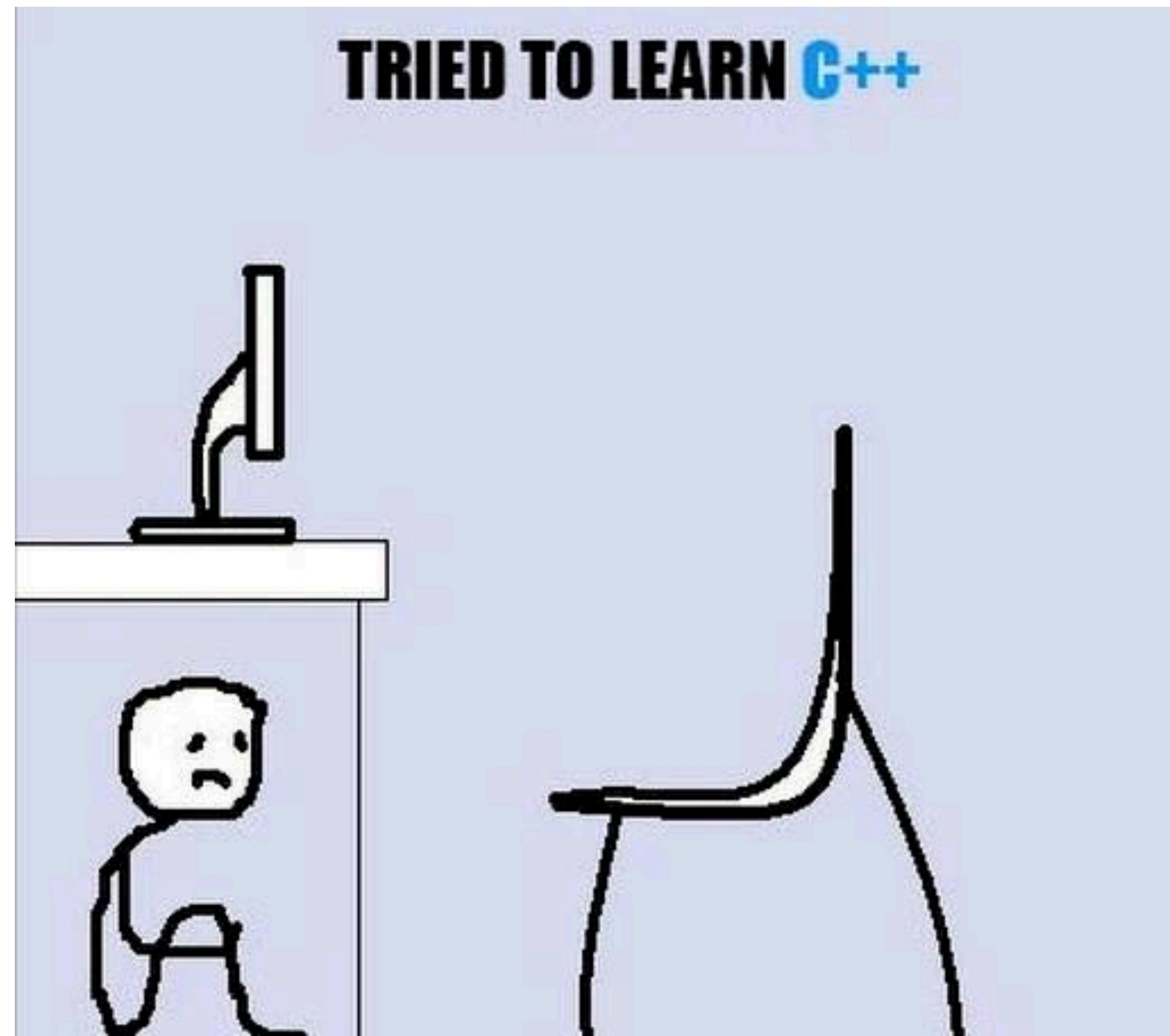
Grid resolution= $3000 \times 2400 \times 1600$

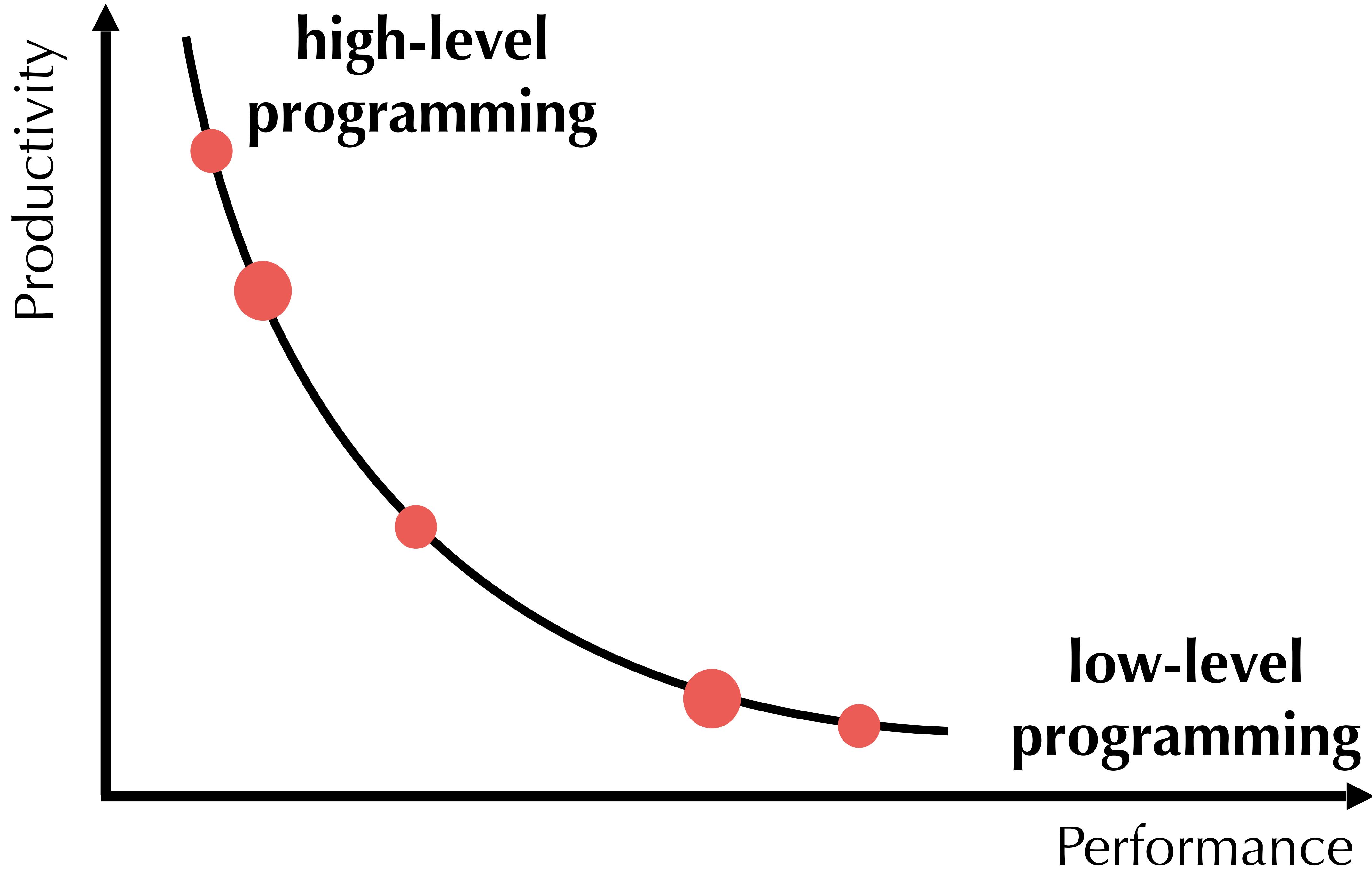
Want High-Resolution?

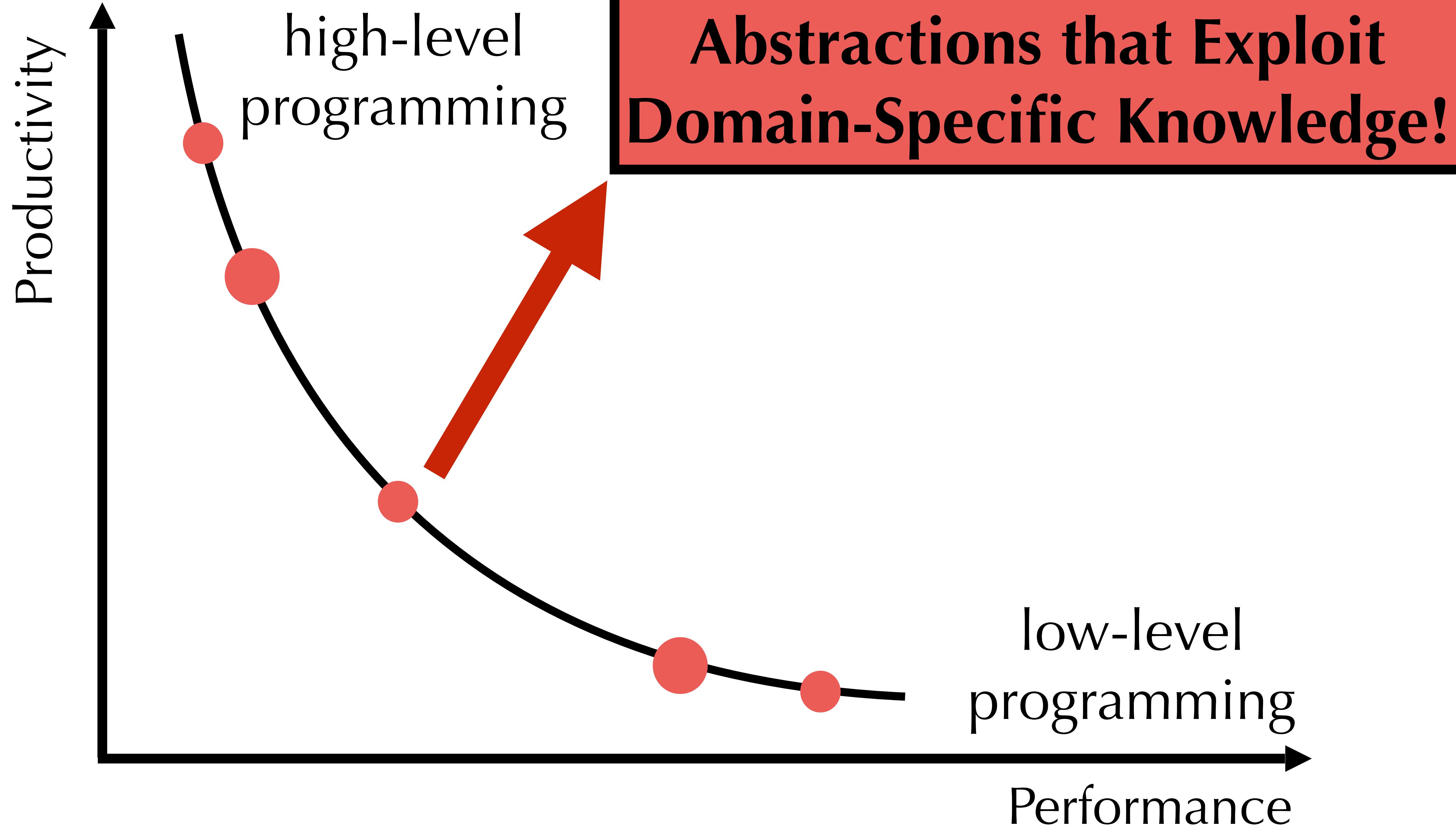
Want High-Resolution?



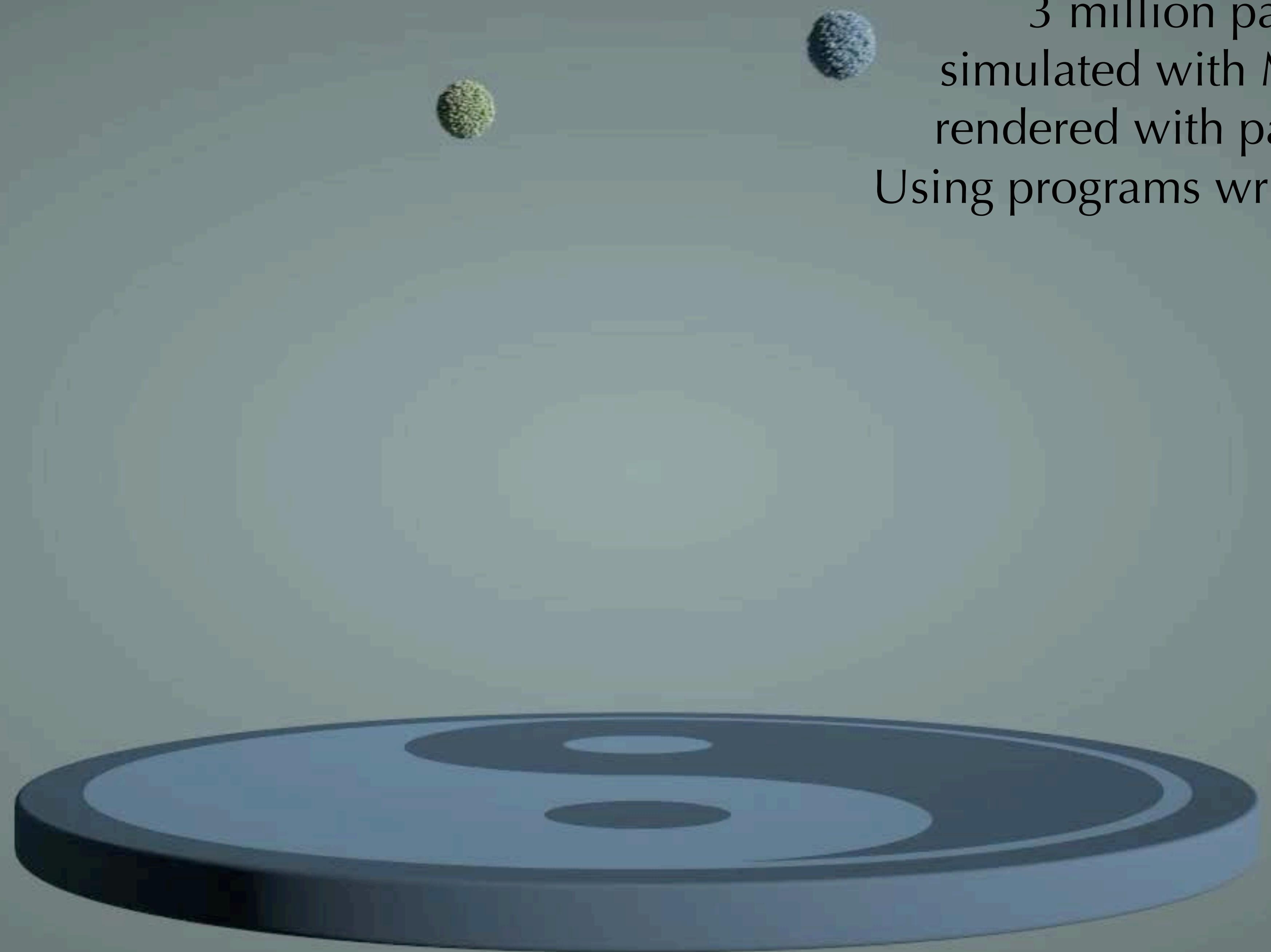
Want Performance?







3 million particles
simulated with MLS-MPM;
rendered with path tracing.
Using programs written in *Taichi*.

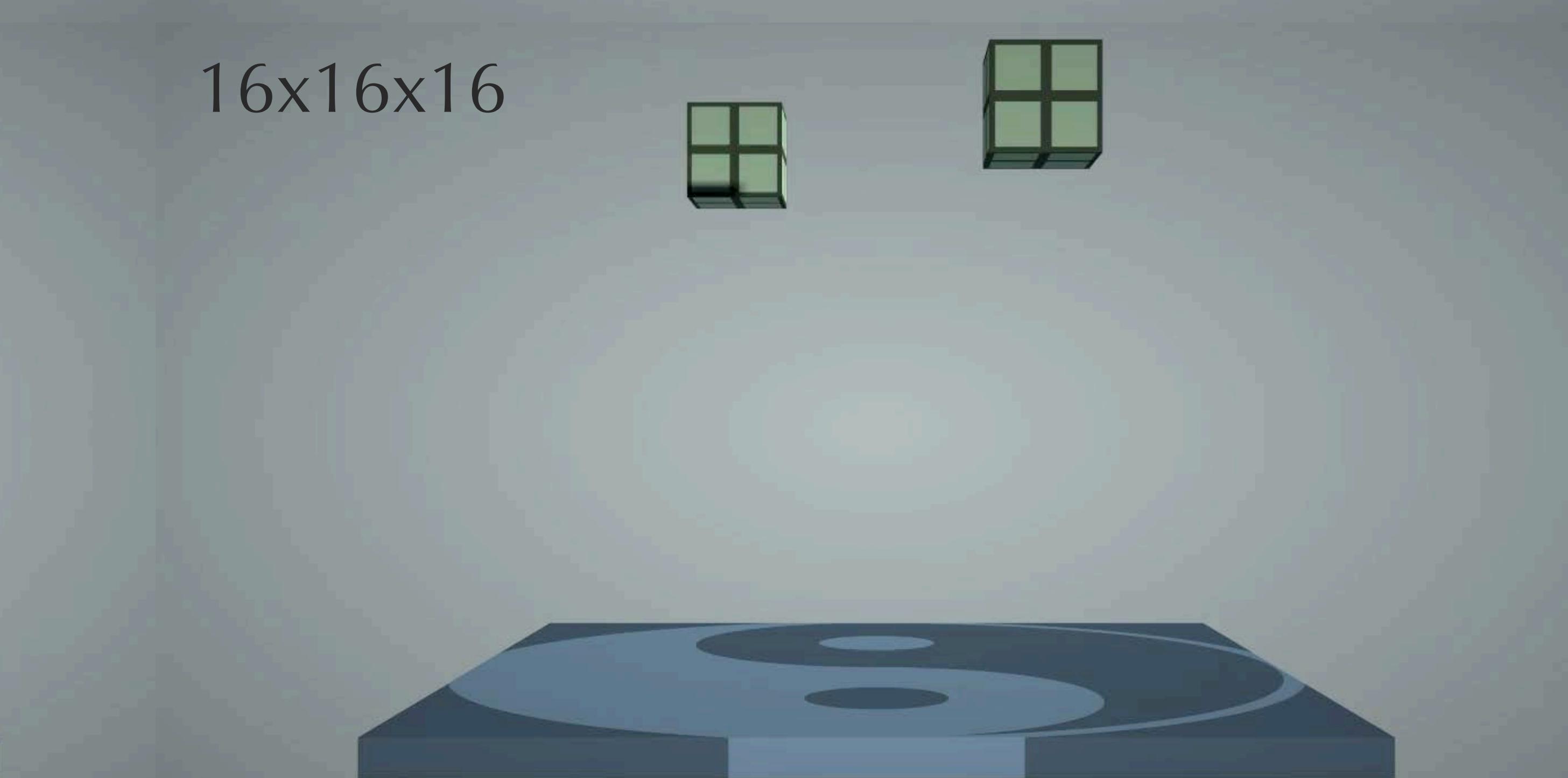
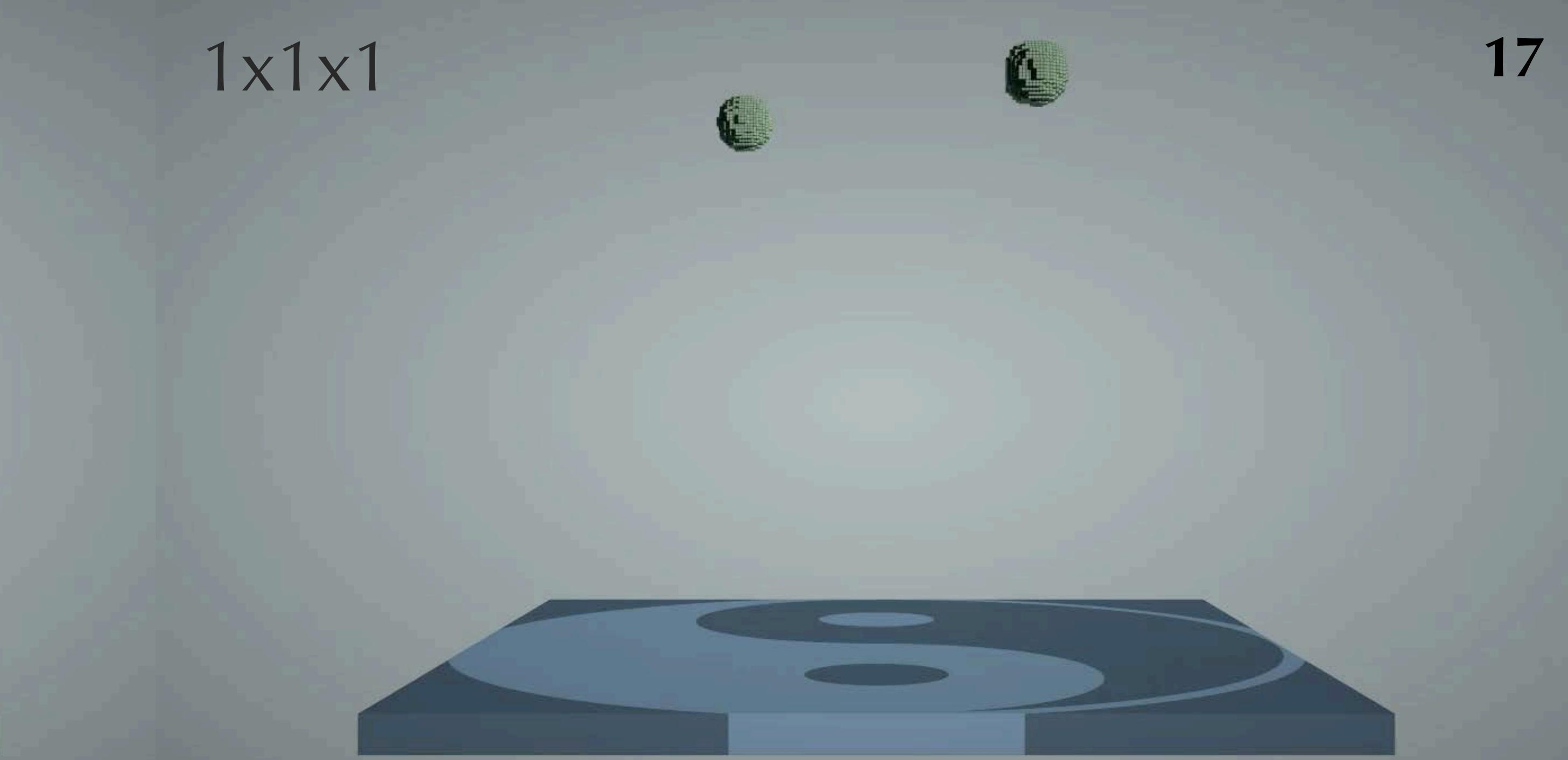
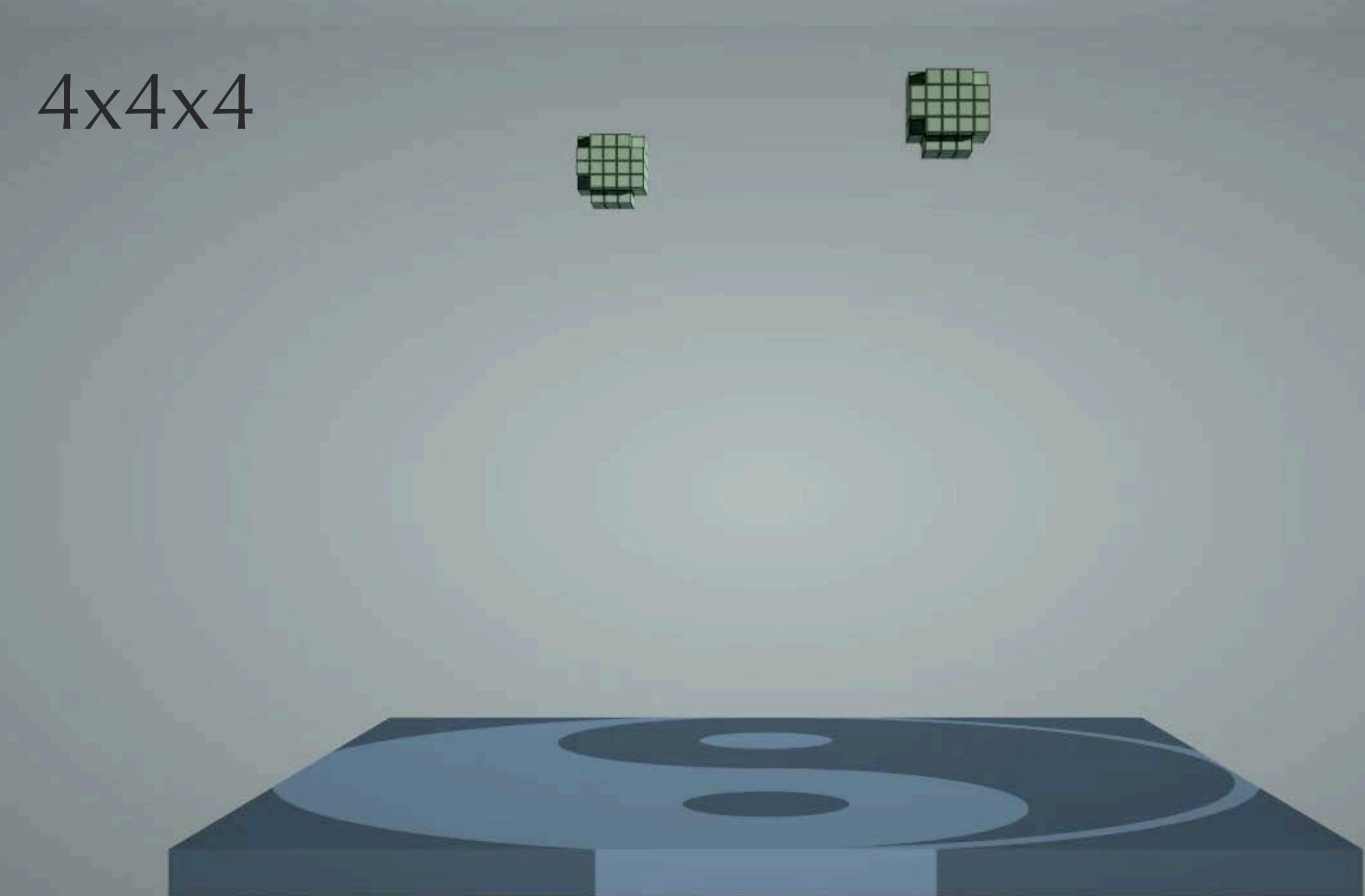
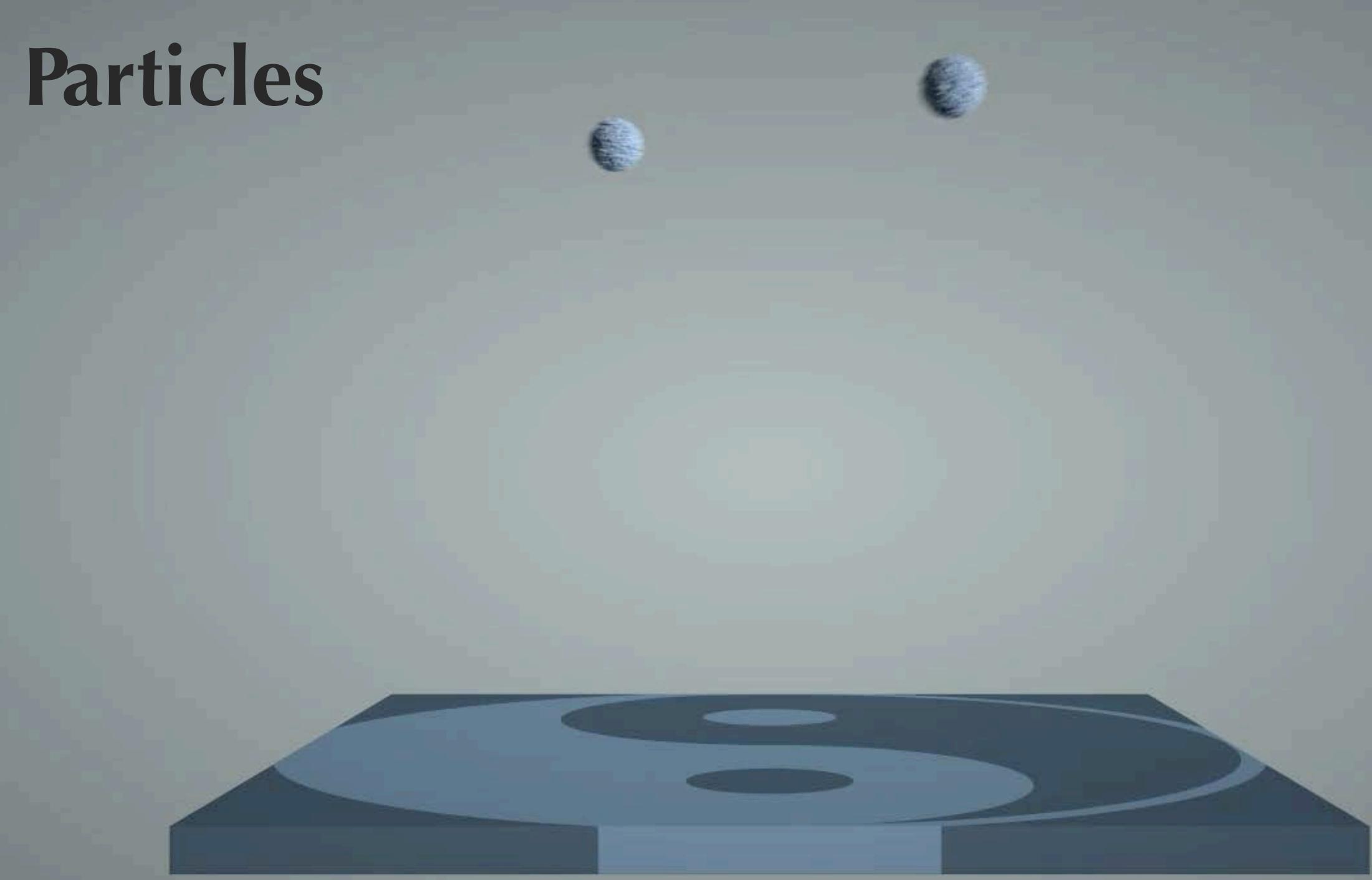


Spatial Sparsity:
Regions of interest only occupy a small fraction of
the bounding volume.

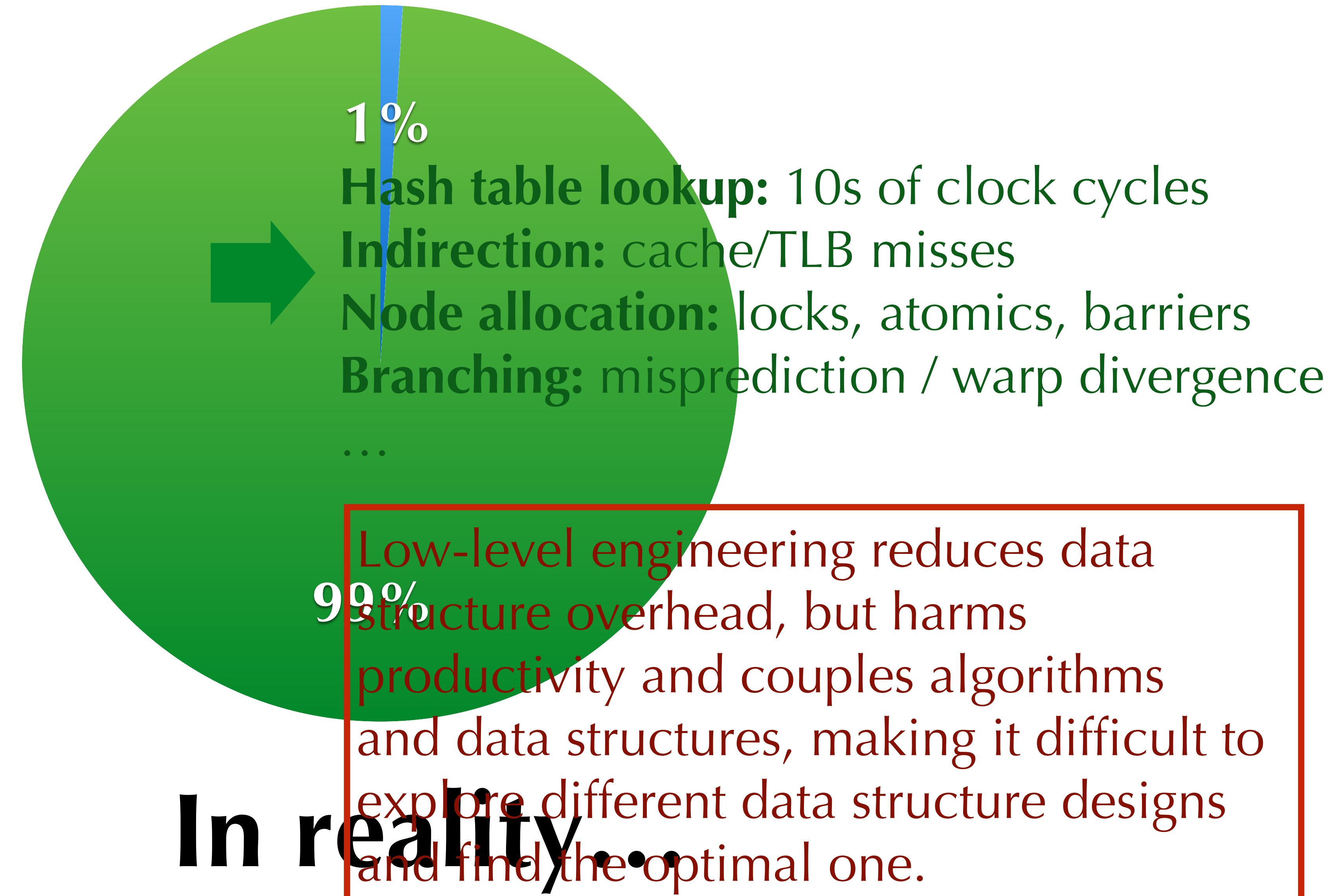


Particles

17



- Essential Computation
- Data Structure Overhead



Our Solution:

The Taichi Programming Language

1) Decouple computation from data structures

Computational Kernels

```
Kernel(laplace).def(&() {
    For(u, [&](Expr i, Expr j){
        auto c = 1.0f / (dx * dx);
        u[i, j] = c * (4 * v[i, j] - v[i+1, j]
                        - v[i-1, j] - v[i, j+1] - v[i, j-1]);
    });
});
```

2D Laplace operator

(Sparse) Data Structures

```
Global(u, f32); Global(v, f32);
layout(&() {
    auto ij = Indices(0, 1);
    root.dense(ij, {128, 128}).pointer()
        .dense(ij, {8, 8}).place(u, v);
});
```

1024² sparse grid with 8²

IR & Optimizing Compiler

10x shorter code, 4.55x faster

High-Performance CPU/GPU Kernels

Ours v.s. State-of-the-art:	
MLS-MPM	13x shorter code, 1.2x faster
FEM Kernel	13x shorter code, 14.5x faster
MGPG	7x shorter code, 1.9x faster
Sparse CNN	9x shorter code, 13x faster

2) Imperative computation language

3) Hierarchical data structure description language

4) Intermediate representation (IR) & data structure access optimizations

5) Auto parallelization, memory management, ...

Runtime System

Defining Computation

Finite Difference Stencil

$$u_{i,j} = \frac{1}{\Delta x^2} (4v_{i,j} - v_{i+1,j} - v_{i-1,j} - v_{i,j+1} - v_{i,j-1})$$



Taichi Kernel

```

1 @ti.kernel
2 def laplace():
3     for i, j in u:
4         c = 1 / (dx * dx)
5         u[i, j] = c * (4.0 * v[i, j] - v[i-1, j] - v[i+1, j]
6                           - v[i, j-1] - v[i, j+1])

```

- Program on **sparse** data structures as if they are **dense**;
- **Parallel** for-loops (Single-Program-Multiple-Data, like CUDA/ispc);
- Loop over only active elements in the sparse data structure;
- Complex **control flows** (e.g. **If**, **While**) supported.

Sample/pixel/sec: 7.126

depth_limit: 20

21

density_scale: 400.000

max_density: 724.000

ground_y: 0.029

light_phi: 0.419

light_theta: 0.218

light_smoothness: 0.050

light_ambient: 0.150

exposure: 0.567

gamma: 0.500

file_id: 0

output_samples: 10

grid_level: 1

video_step: 1

Save

Render All

Results

10.0x shorter code

4.55x higher performance

High-Performance CPU/GPU Kernels

Ours v.s. State-of-the-art:

MLS-MPM 13x shorter code, 1.2x faster

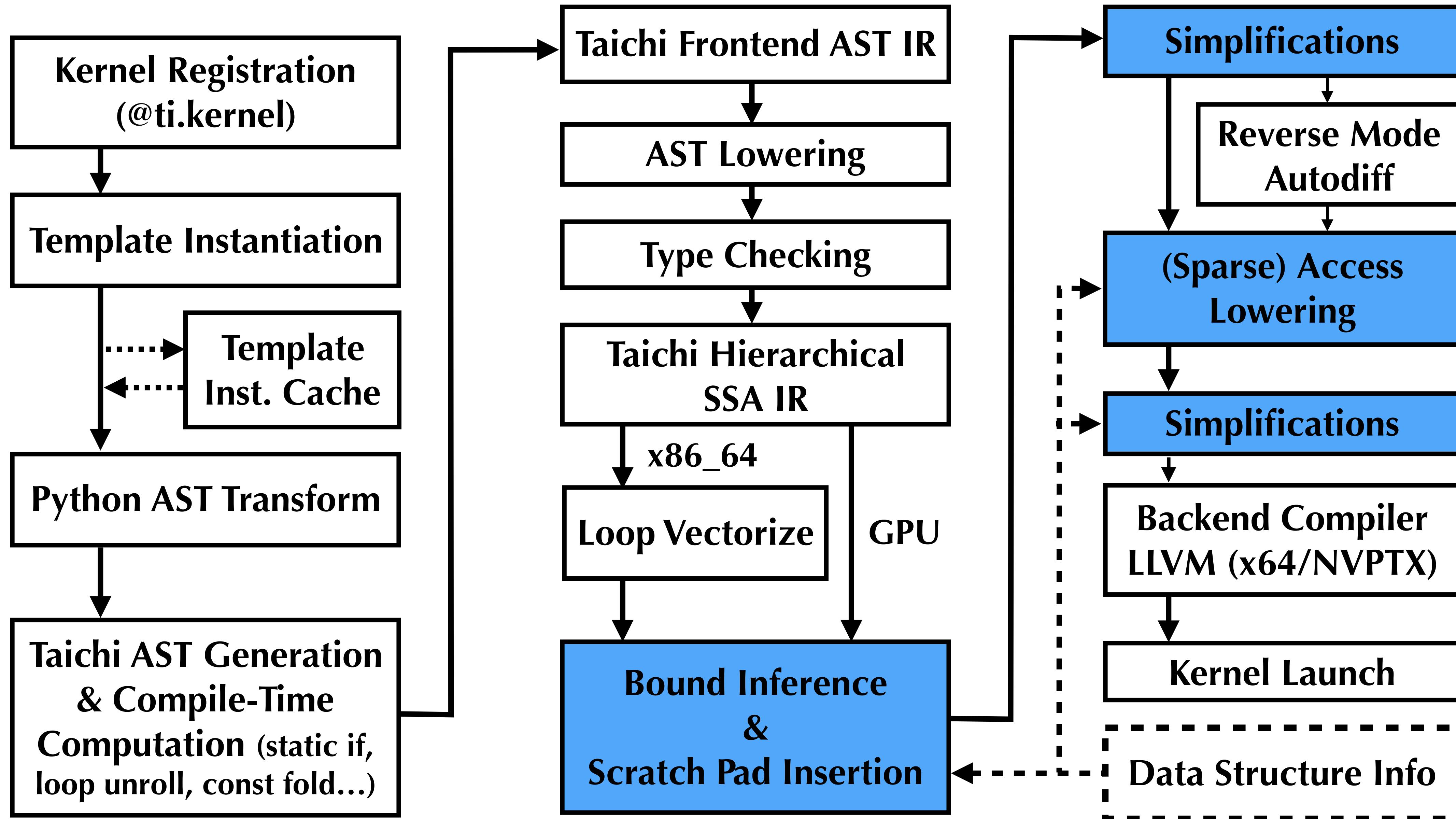
FEM Kernel 13x shorter code, 14.5x faster

MGPCG 7x shorter code, 1.9x faster

Sparse CNN 9x shorter code, 13x faster

The Life of a Taichi Kernel

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Taichi's Intermediate Representation (IR)

CHI 气

CHI Hierarchical Instructions

「阴阳，气之大者也。」 —— 《庄子·则阳》 ~300 B.C.

Optimization-Oriented Intermediate Representation Design

♦ Hierarchical IR

- Keeps loop information
- Static scoping
- Strictly (strongly) & statically typed

♦ Static Single Assignment (SSA)

♦ Progressive lowering. ~70 Instructions in total.

Why can't traditional compilers do the optimizations?

- 1) Index analysis
- 2) Instruction granularity
- 3) Data access semantics

The Granularity Spectrum

x[i, j]

End2end access

access1(i, j)
access2(i, j)

Level-wise Access

Taichi IR
(CHI)

```
$4 = [S4][root]::lookup(root, $3) coord = {$2}
    activate = false
$5 = get child [S4->S3] $4
$6 = bit_extract($2 + 0, 7~14)
$7 = linearized(ind {$6}, stride {128})
$8 = [S3][dense]::lookup($5, $7) coord = {$2} a
    = false
$9 = get child [S3->S2] $8
$10 = bit_extract($2 + 0, 0~7)
$11 = linearized(ind {$10}, stride {128})
$12 = [S2][dense]::lookup($9, $11) coord = {$2}
    activate = false
```

```
%63 = lshr i32 %62, 0
%64 = and i32 %63, 255
%65 = add i32 %37, 0
%66 = lshr i32 %65, 0
%67 = and i32 %66, 255
%68 = add i32 0, %64
%69 = mul i32 %68, 256
%70 = add i32 %69, %67
%71 = bitcast %struct.DenseMeta* %5 to
call void @StructMeta_set_snode_id(%si
call void @StructMeta_set_element_size(
call void @StructMeta_set_max_num_ele
call void @StructMeta_set_lookup_eleme
_element)
call void @StructMeta_set_is_active(%:
elements)
call void @StructMeta_set_get_num_ele
elements)
call void @StructMeta_set_from_parent.
```

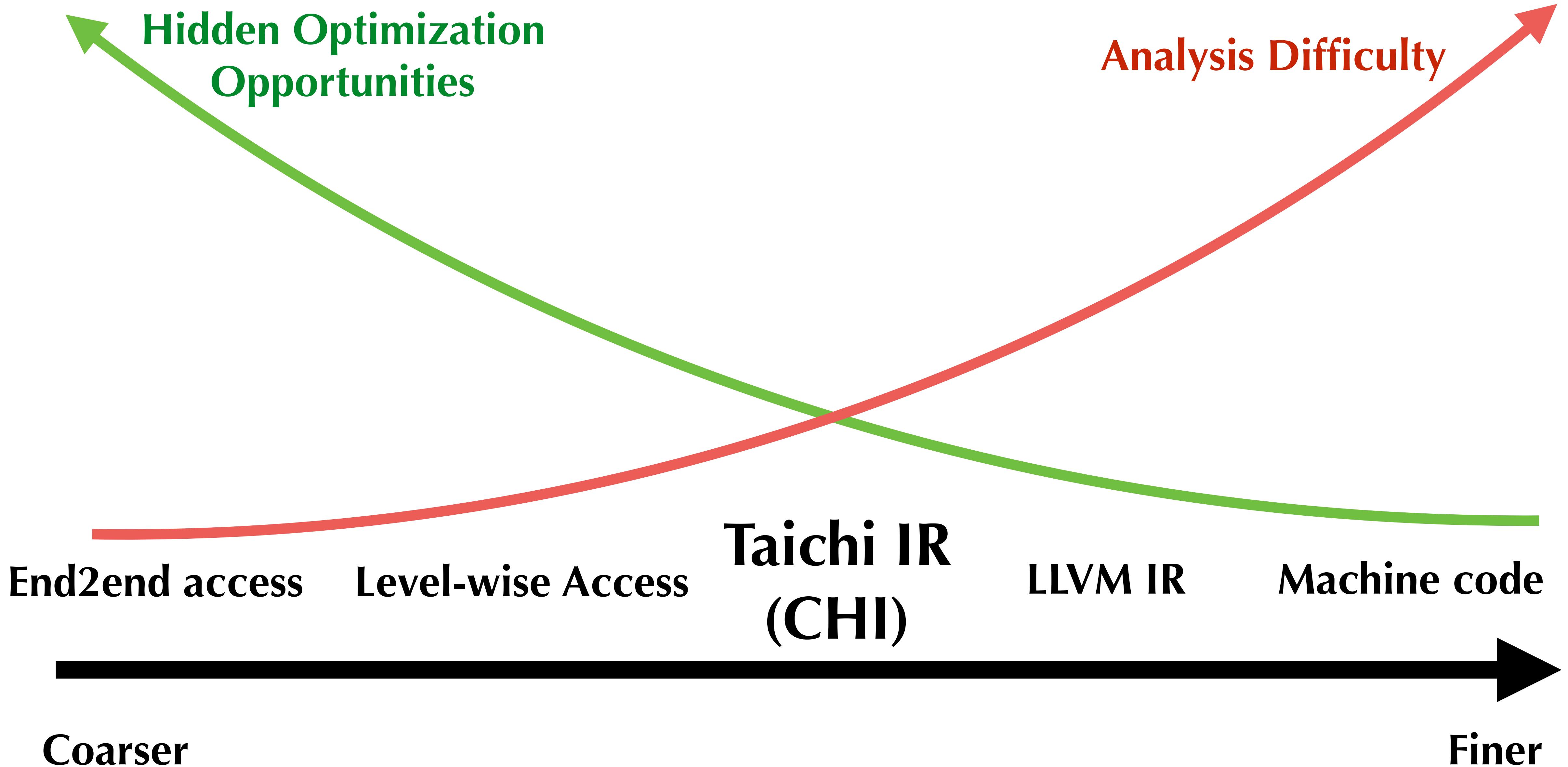
```
movl $0, %eax
addl %eax, %ebx
popl %eax
looptop:
imul %edx
andl $0xFF, %eax
cmpl $100, %eax
jb looptop
leal 4(%esp), %ebp
movl %esi, %edi
subl $8, %edi
shrl %cl, %ebx
movw %bx, -2(%ebp)
movl $0, %eax
addl %eax, %ebx
popl %eax
looptop:
imul %edx
andl $0xFF, %eax
cmpl $100, %eax
jb looptop
leal 4(%esp), %ebp
movl %esi, %edi
subl $8, %edi
shrl %cl, %ebx
movw %bx, -2(%ebp)
```

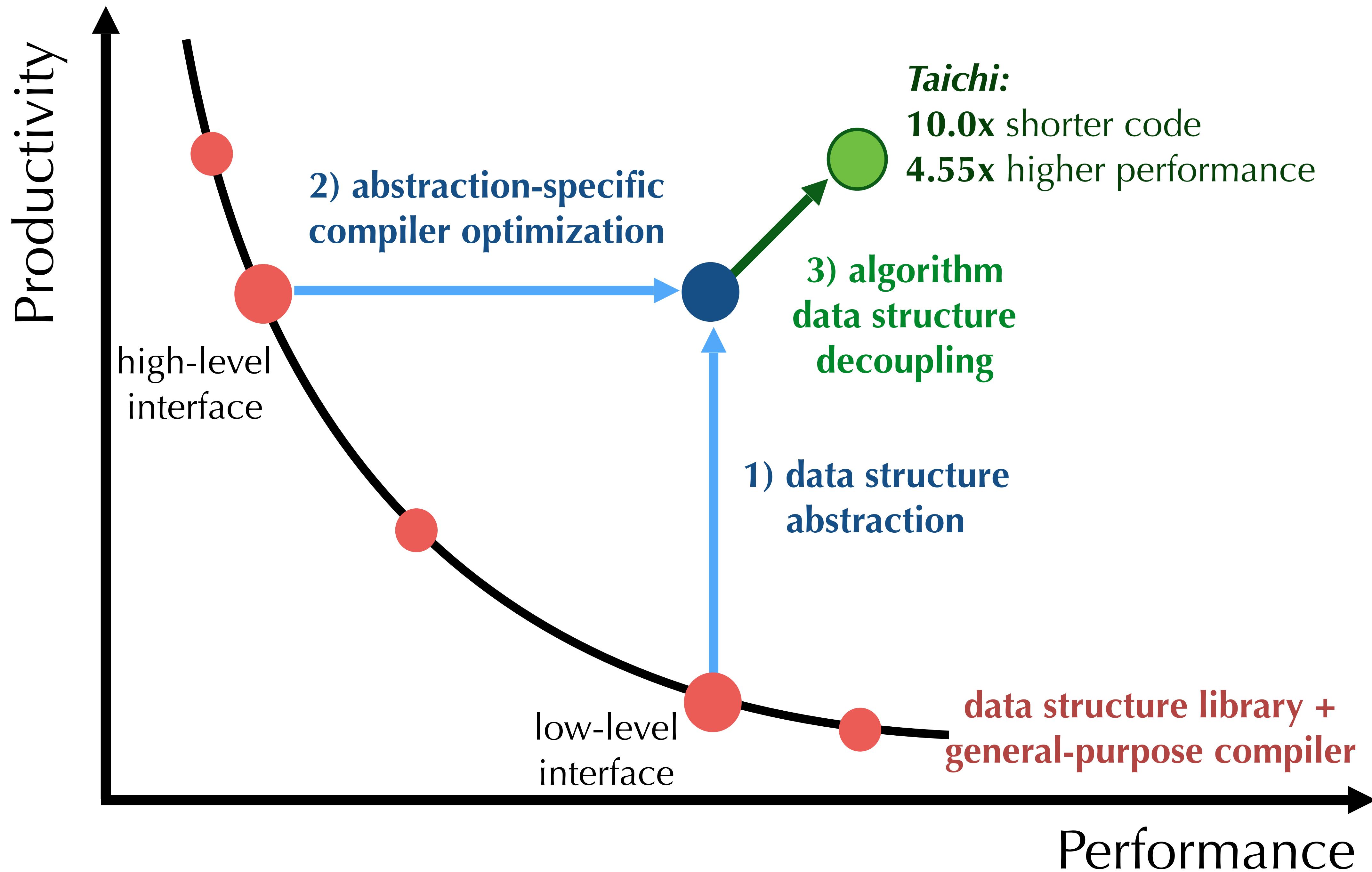
LLVM IR

Machine code

Coarser

Finer

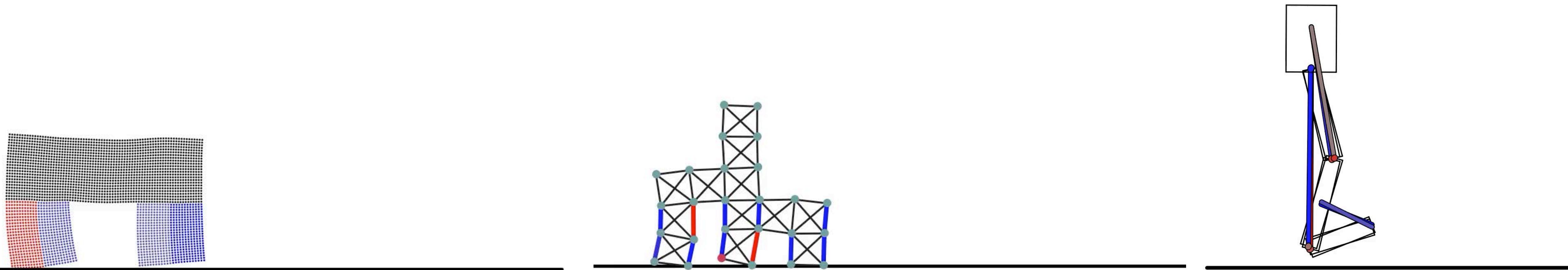




DiffTaichi:

Differentiable Programming on Taichi

(for physical simulation and many other apps)



End2end optimization of neural network controllers with gradient descent

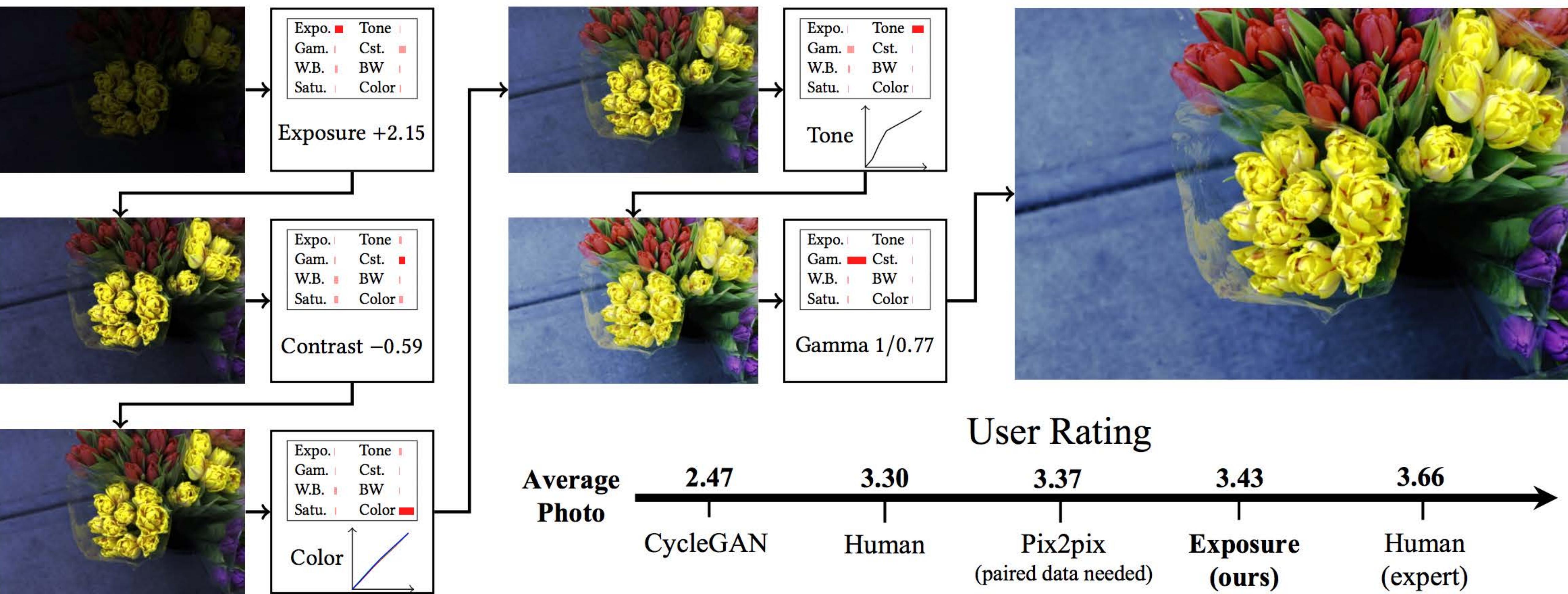
Exposure: A White-Box Photo Post-Processing Framework³¹ (TOG 2018)

Yuanming Hu^{1,2} Hao He^{1,2} Chenxi Xu^{1,3} Baoyuan Wang¹ Stephen Lin¹

¹Microsoft Research

²MIT CSAIL

³Peking University



Exposure:

Learn image operations, instead of pixels.

Differentiable Photo Postprocessing Model

resolution independent
content preserving
human-understandable

Deep Reinforcement Learning

Learn image **operations**,
instead of **pixels**

Generative Adversarial Networks



Modelling

Optimization

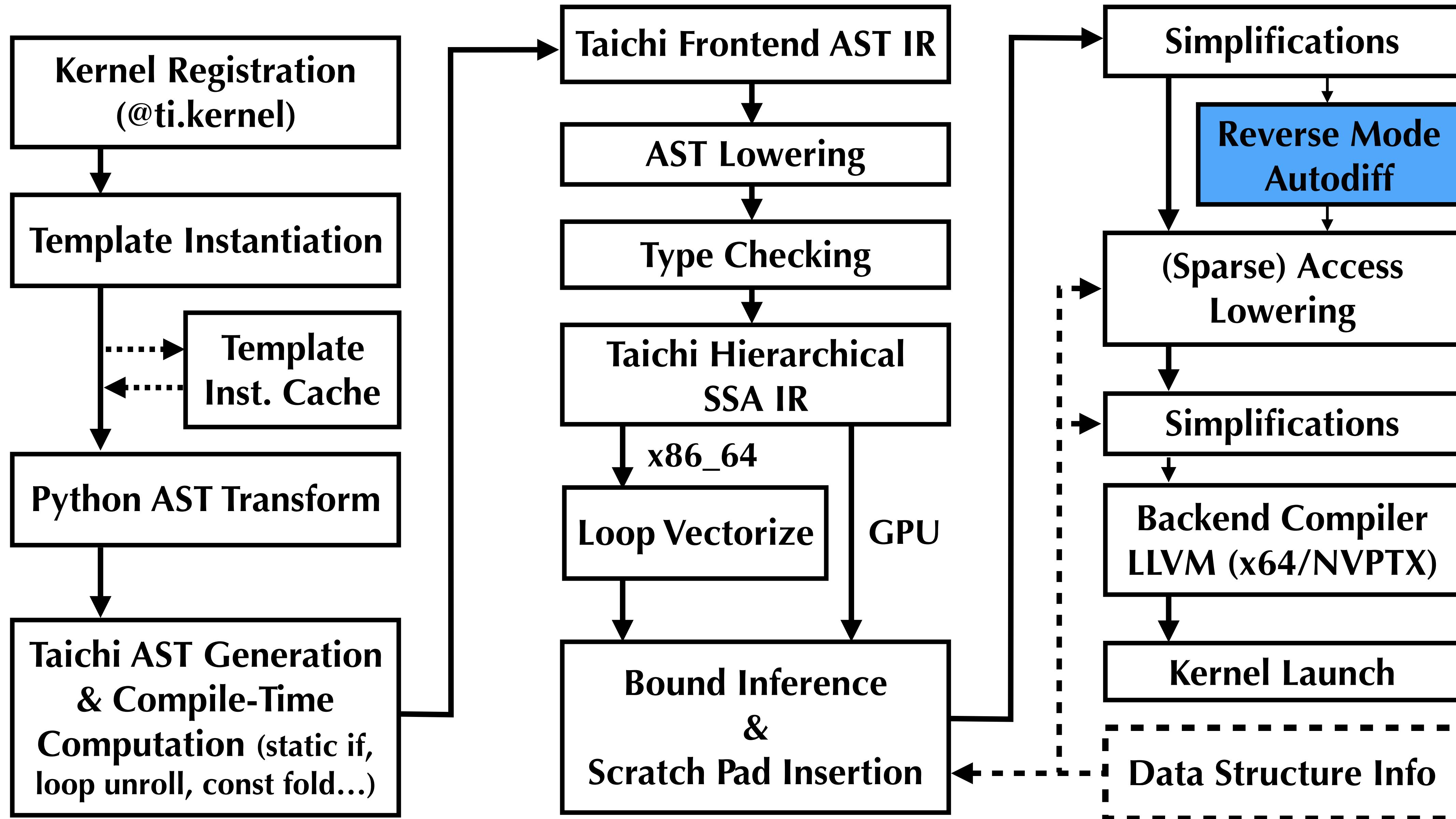
Hand-written CUDA 132x
faster than TensorFlow

Iteration 0

ChainQueen: *Differentiable MLS-MPM*
Hu, Liu, Spielberg, Tenenbaum
Freeman, Wu, Rus, Matusik (ICRA 2019)

The Life of a Taichi Kernel

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Differentiable Programming v.s. Deep Learning: What are they?

$$L(x) \longrightarrow \frac{\partial L}{\partial x}$$

Optimization/Learning via **gradient descent!**

Differentiable Programming v.s. Deep Learning: What are the differences?

- ♦ **Deep learning operations:**
 - convolution, batch normalization, pooling...
- ♦ **Differentiable programming further enables**
 - Stencils, gathering/scattering, fine-grained branching and loops...
 - More expressive & higher performance for irregular operations
- ♦ **Granularity**
 - Why not TensorFlow/PyTorch?
 - Physical simulator written in TF is **132x** slower than CUDA [Hu et al. 2019, ChainQueen]
- ♦ **Reverse-Mode Automatic Differentiation is the key component to differentiable programming**

The DiffTaichi Programming Language & Compiler: Automatic Differentiation for Physical Simulation

Key language designs:

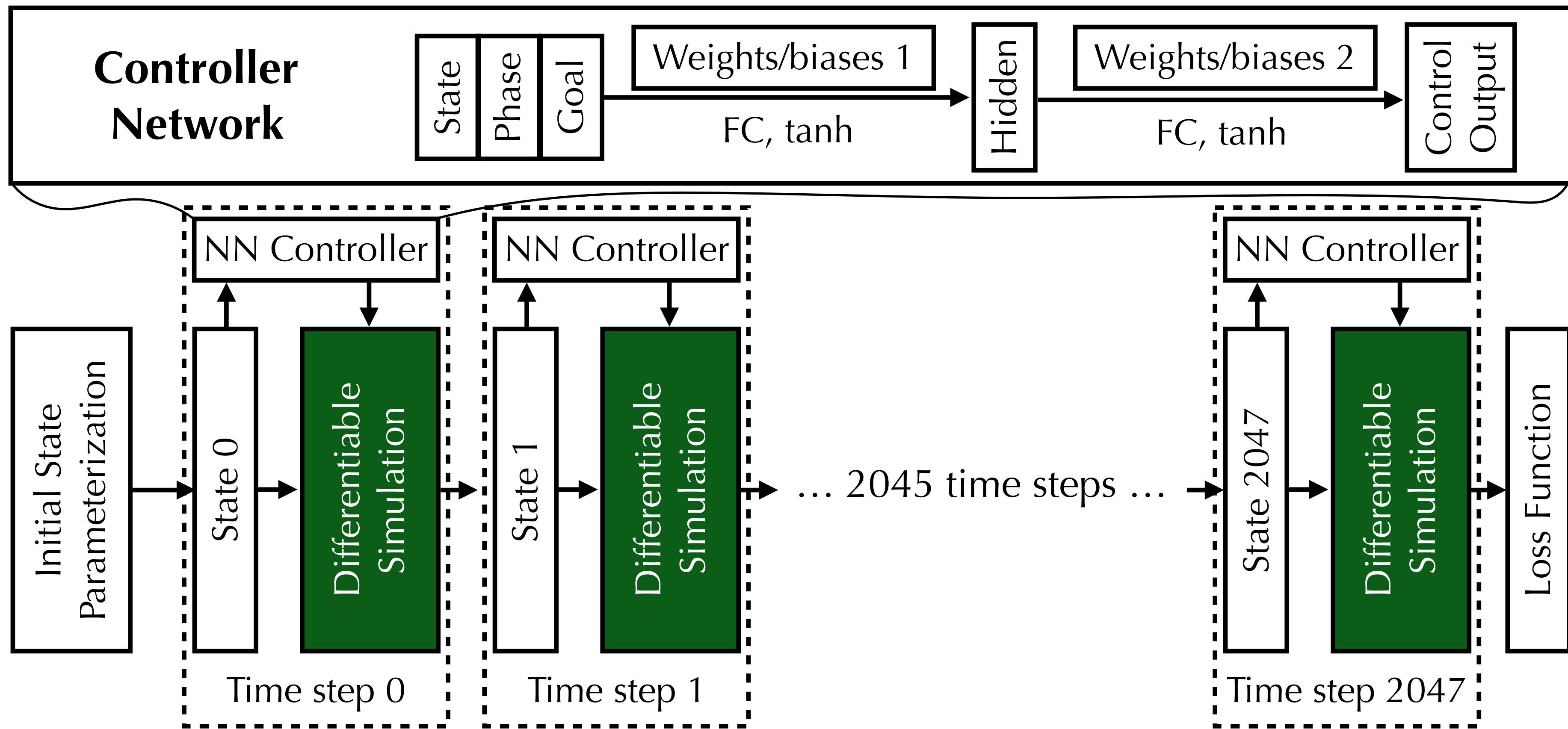
- **Differentiable**
- **Imperative**
- **Parallel**
- **Megakernels**

```
@ti.kernel
def apply_spring_force(t: ti.i32):
    # Kernels can have parameters. Here t is a parameter with type int32.
    for i in range(n_springs): # A parallel for, preferably on GPU
        a, b = spring_anchor_a[i], spring_anchor_b[i]
        x_a, x_b = x[t - 1, a], x[t - 1, b]
        dist = x_a - x_b
        length = dist.norm() + 1e-4
        F = (length - spring_length[i]) * spring_stiffness * dist / length
        # Apply spring impulses to mass points. Use atomic_add for parallel safety.
        ti.atomic_add(force[t, a], -F)
        ti.atomic_add(force[t, b], F)
```

4.2x shorter code compared to hand-engineered CUDA.

188x faster than TensorFlow.

Please check out our paper for more details.



Our language allows programmers to easily build **differentiable physical modules** that work in deep neural networks.
The whole program is **end-to-end differentiable**.

$$l_{i\mathbf{n}} = \sum_{\alpha} \mathbf{v}_{i\alpha} \mathbf{n}_{i\alpha} \quad (102)$$

$$\mathbf{v}_{i\mathbf{t}} = \mathbf{v}_i - l_{i\mathbf{n}} \mathbf{n}_i \quad (103)$$

$$l_{i\mathbf{t}} = \sqrt{\sum_{\alpha} \mathbf{v}_{i\mathbf{t}\alpha}^2 + \varepsilon} \quad (104)$$

$$\hat{\mathbf{v}}_{i\mathbf{t}} = \frac{1}{l_{i\mathbf{t}}} \mathbf{v}_{i\mathbf{t}} \quad (105)$$

$$l_{i\mathbf{t}}^* = \max\{l_{i\mathbf{t}} + c_i \min\{l_{i\mathbf{n}}, 0\}, 0\} \quad (106)$$

$$\mathbf{v}_i^* = l_{i\mathbf{t}}^* \hat{\mathbf{v}}_{i\mathbf{t}} + \max\{l_{i\mathbf{n}}, 0\} \mathbf{n}_i \quad (107)$$

$$H(x) := [x \geq 0] \quad (108)$$

$$R := l_{i\mathbf{t}} + c_i \min\{l_{i\mathbf{n},0}\} \quad (109)$$

$$l_{i\mathbf{n}} = \sum_{\alpha} \mathbf{v}_{i\alpha} \mathbf{n}_{i\alpha} \quad (102)$$

$$\mathbf{v}_{i\mathbf{t}} = \mathbf{v}_i - l_{i\mathbf{n}} \mathbf{n}_i \quad (103)$$

$$l_{i\mathbf{t}} = \sqrt{\sum_{\alpha} \mathbf{v}_{i\mathbf{t}\alpha}^2 + \varepsilon} \quad (104)$$

$$\hat{\mathbf{v}}_{i\mathbf{t}} = \frac{1}{l_{i\mathbf{t}}} \mathbf{v}_{i\mathbf{t}} \quad (105)$$

$$l_{i\mathbf{t}}^* = \max\{l_{i\mathbf{t}} + c_i \min\{l_{i\mathbf{n}}, 0\}, 0\} \quad (106)$$

$$\mathbf{v}_i^* = l_{i\mathbf{t}}^* \hat{\mathbf{v}}_{i\mathbf{t}} + \max\{l_{i\mathbf{n}}, 0\} \mathbf{n}_i \quad (107)$$

$$H(x) := [x \geq 0] \quad (108)$$

$$R := l_{i\mathbf{t}} + c_i \min\{l_{i\mathbf{n}, 0}\} \quad (109)$$

$$\implies \frac{\partial L}{\partial l_{i\mathbf{t}}^*} = \sum_{\alpha} \frac{\partial L}{\partial \mathbf{v}_{i\alpha}^*} \hat{\mathbf{v}}_{i\mathbf{t}\alpha} \quad (110)$$

$$\frac{\partial L}{\partial \hat{\mathbf{v}}_{i\mathbf{t}}} = \frac{\partial L}{\partial \mathbf{v}_{i\alpha}^*} l_{i\mathbf{t}}^* \quad (111)$$

$$\frac{\partial L}{\partial l_{i\mathbf{t}}} = -\frac{1}{l_{i\mathbf{t}}^2} \sum_{\alpha} \mathbf{v}_{i\mathbf{t}\alpha} \frac{\partial L}{\partial \hat{\mathbf{v}}_{i\mathbf{t}\alpha}} + \frac{\partial L}{\partial l_{i\mathbf{t}}^*} H(R) \quad (112)$$

$$\begin{aligned} \frac{\partial L}{\partial \mathbf{v}_{i\mathbf{t}\alpha}} &= \frac{\mathbf{v}_{i\mathbf{t}\alpha}}{l_{i\mathbf{t}}} \frac{\partial L}{\partial l_{i\mathbf{t}}} + \frac{1}{l_{i\mathbf{t}}} \frac{\partial L}{\partial \hat{\mathbf{v}}_{i\mathbf{t}\alpha}} \\ &= \frac{1}{l_{i\mathbf{t}}} \left[\frac{\partial L}{\partial l_{i\mathbf{t}}} \mathbf{v}_{i\mathbf{t}\alpha} + \frac{\partial L}{\partial \hat{\mathbf{v}}_{i\mathbf{t}\alpha}} \right] \end{aligned} \quad (113)$$

$$\begin{aligned} \frac{\partial L}{\partial l_{i\mathbf{n}}} &= - \left[\sum_{\alpha} \frac{\partial L}{\partial \mathbf{v}_{i\mathbf{t}\alpha}} \mathbf{n}_{i\alpha} \right] + \frac{\partial L}{\partial l_{i\mathbf{t}}^*} H(R) c_i H(-l_{i\mathbf{n}}) + \sum_{\alpha} H(l_{i\mathbf{n}}) \mathbf{n}_{i\alpha} \frac{\partial L}{\partial \mathbf{v}_{i\alpha}^*} \\ \frac{\partial L}{\partial \mathbf{v}_{i\alpha}} &= \frac{\partial L}{\partial l_{i\mathbf{n}}} \mathbf{n}_{i\alpha} + \frac{\partial L}{\partial \mathbf{v}_{i\mathbf{t}\alpha}} \end{aligned} \quad (115) \quad (116)$$

$$(117)$$

Reverse-Mode Auto Differentiation

$$y_i = \sin x_i^2$$

```

for i in range(0, 16, step 1) do - - - - -
    %1 = load x[i]
    %2 = mul %1, %1
    %3 = sin(%2)
    store y[i] = %3 - - - - -
end for

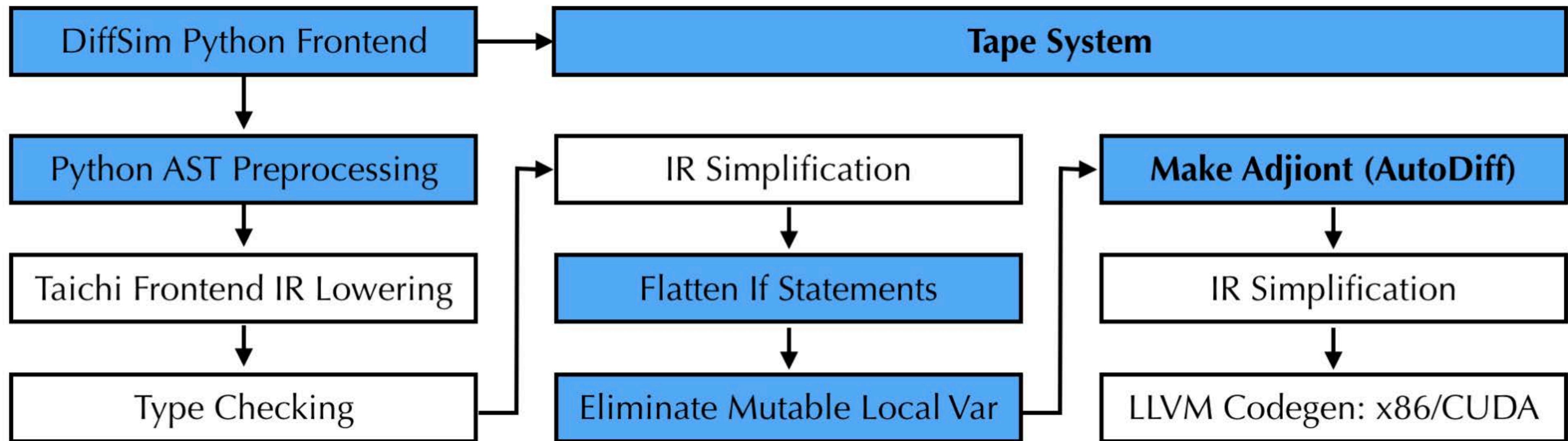
```

```

for i in range(0, 16, step 1) do
    // adjoint variables
    %1adj = alloca 0.0
    %2adj = alloca 0.0
    %3adj = alloca 0.0
    // original forward computation
    %1 = load x[i]
    %2 = mul %1, %1
    %3 = sin(%2)
    // reverse accumulation
    %4 = load y_adj[i]
    %3adj += %4
    %5 = cos(%2)
    %2adj += %3adj * %5
    %1adj += 2 * %1 * %2adj
    atomic add x_adj[i], %1adj
end for

```

Two-Scale AutoDiff



Forward Program

```
with ti.Tape(loss)
    for i in range(3):
        compute_force(i)
        move_partcies(i)
    compute_loss()
```

Tape Contents

```
compute_force, args=(0)
move_partcies, args=(0)
compute_force, args=(1)
move_partcies, args=(1)
compute_force, args=(2)
move_partcies, args=(2)
compute_loss, args=()
```

Backward Program

```
compute_loss.grad()
move_partcies.grad(2)
compute_force.grad(2)
move_partcies.grad(1)
compute_force.grad(1)
move_partcies.grad(0)
compute_force.grad(0)
```

Related Work

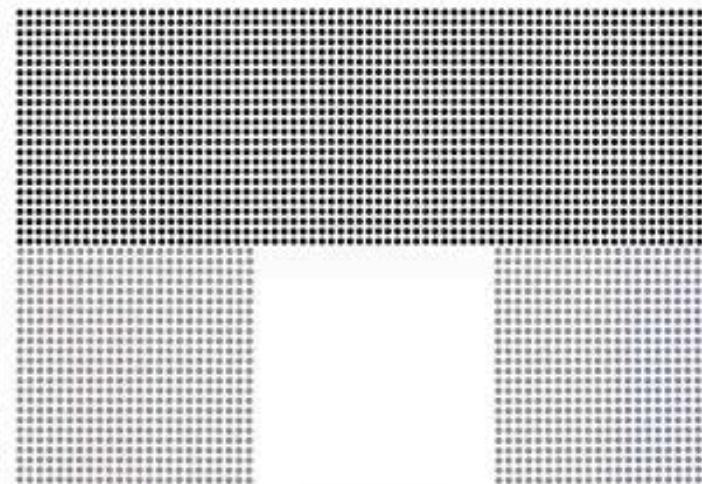
Table 3: Comparisons between DiffTaichi and other differentiable programming tools. **Note that this table only discusses features related to differentiable physical simulation**, and the other tools may not have been designed for this purpose. For example, PyTorch and TensorFlow are designed for classical deep learning tasks and have proven successful in their target domains. Also note that the XLA backend of TensorFlow and JIT feature of PyTorch allow them to fuse operators to some extent, but for simulation we want complete operator fusion within megakernels. “Swift” AD (Wei et al., 2019) is partially implemented as of November 2019. “Julia” refers to Innes et al. (2019).

(DiffSim=DiffTaichi)

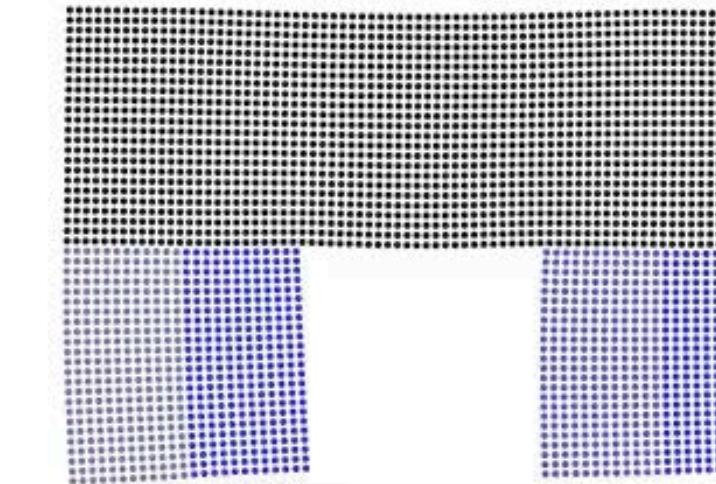
Feature	DiffSim	PyTorch	TensorFlow	Enoki	JAX	Halide	Julia	Swift
GPU Megakernels	✓	△	△	✓	✓	✓		
Imperative Scheme	✓			✓			✓	✓
Parallelism	✓	✓	✓	✓	✓	✓		
Flexible Indexing	✓					✓	✓	✓

Differentiable Elastic Object Simulation

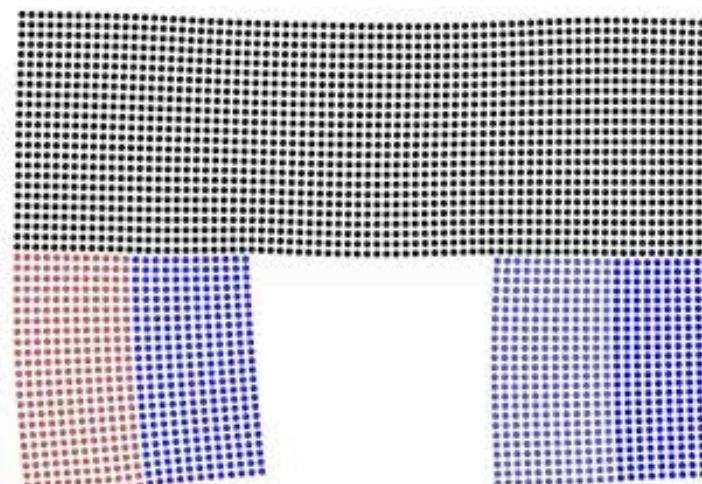
Iteration 0



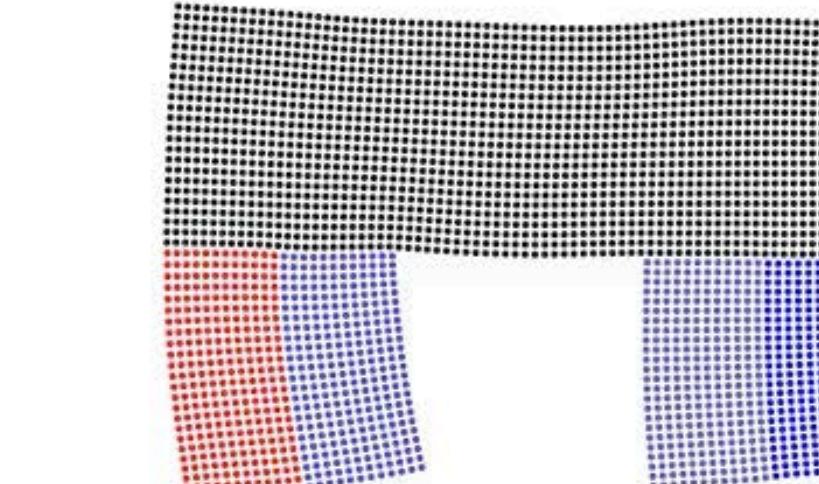
Iteration 20



Iteration 40



Iteration 80



Continuum modeled with both particles and grids. Open-loop controller.

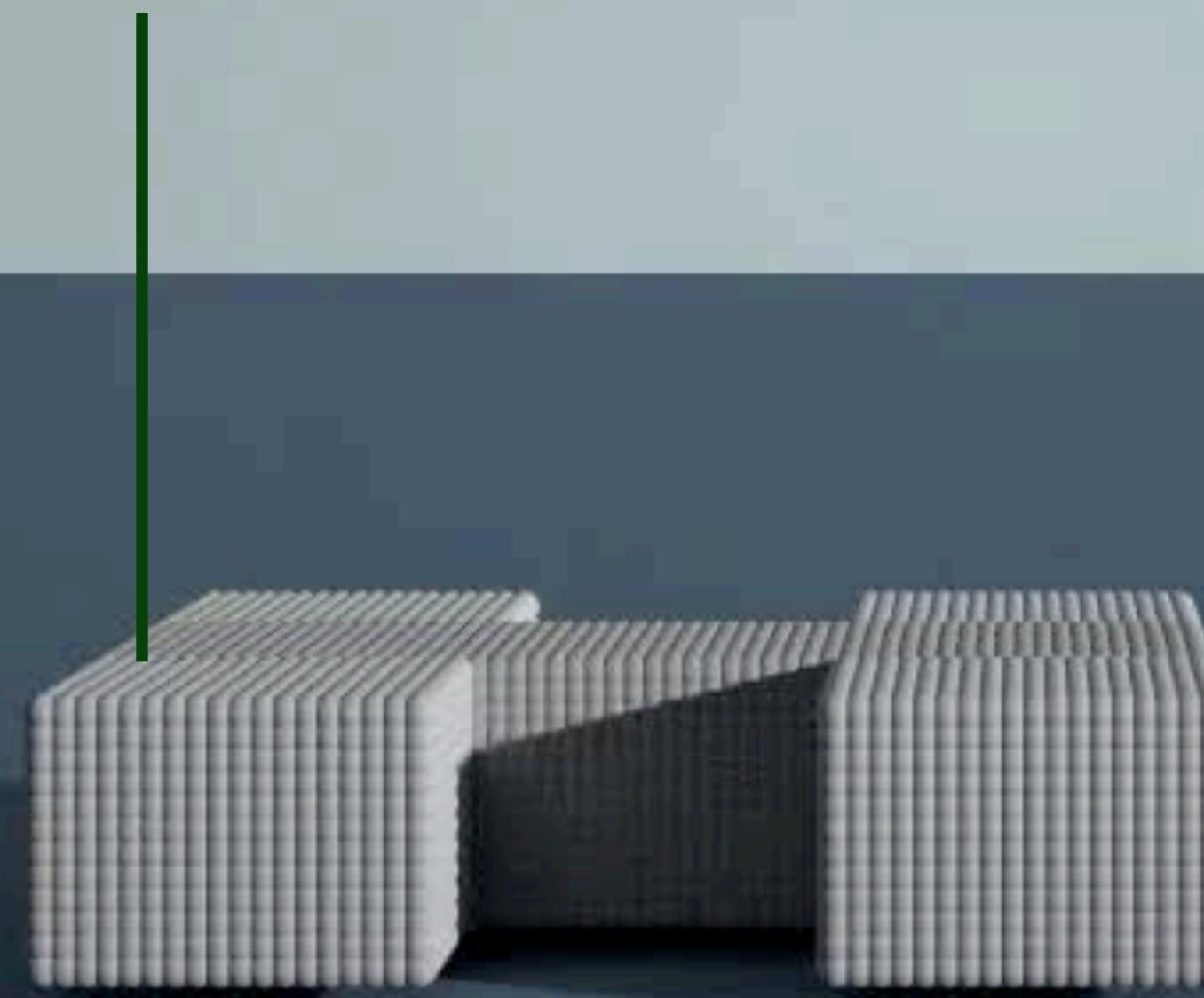
4.2x shorter code than ChainQueen [Hu et al. ICRA 2019]; 188x faster than TensorFlow.
1024 time steps, 80 gradient descent iter. Run time=2min. **Red=extension blue=contraction.**

Reproduce: `python3 diffmpm.py`

Differentiable Elastic Object Simulation (3D)

30.5K particles, 512 time steps, 40 gradient descent iter.
Total run time=4min. Red=extension blue=contraction.

Initial guess



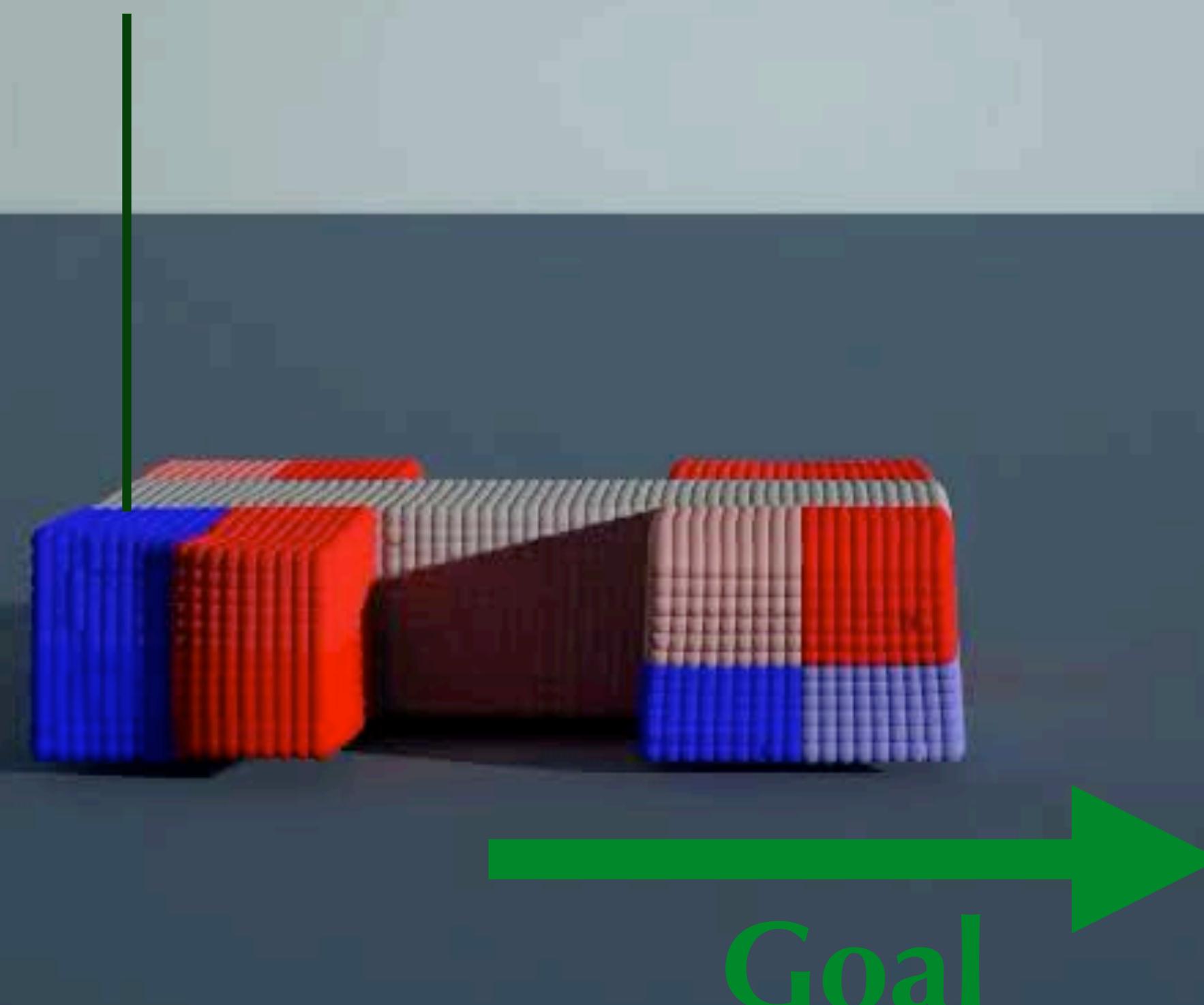
Goal

Reproduce: `python3 diffmpm3d.py`

Differentiable Elastic Object Simulation (3D)

30.5K particles, 512 time steps, 40 gradient descent iter.
Total run time=4min. Red=extension blue=contraction.

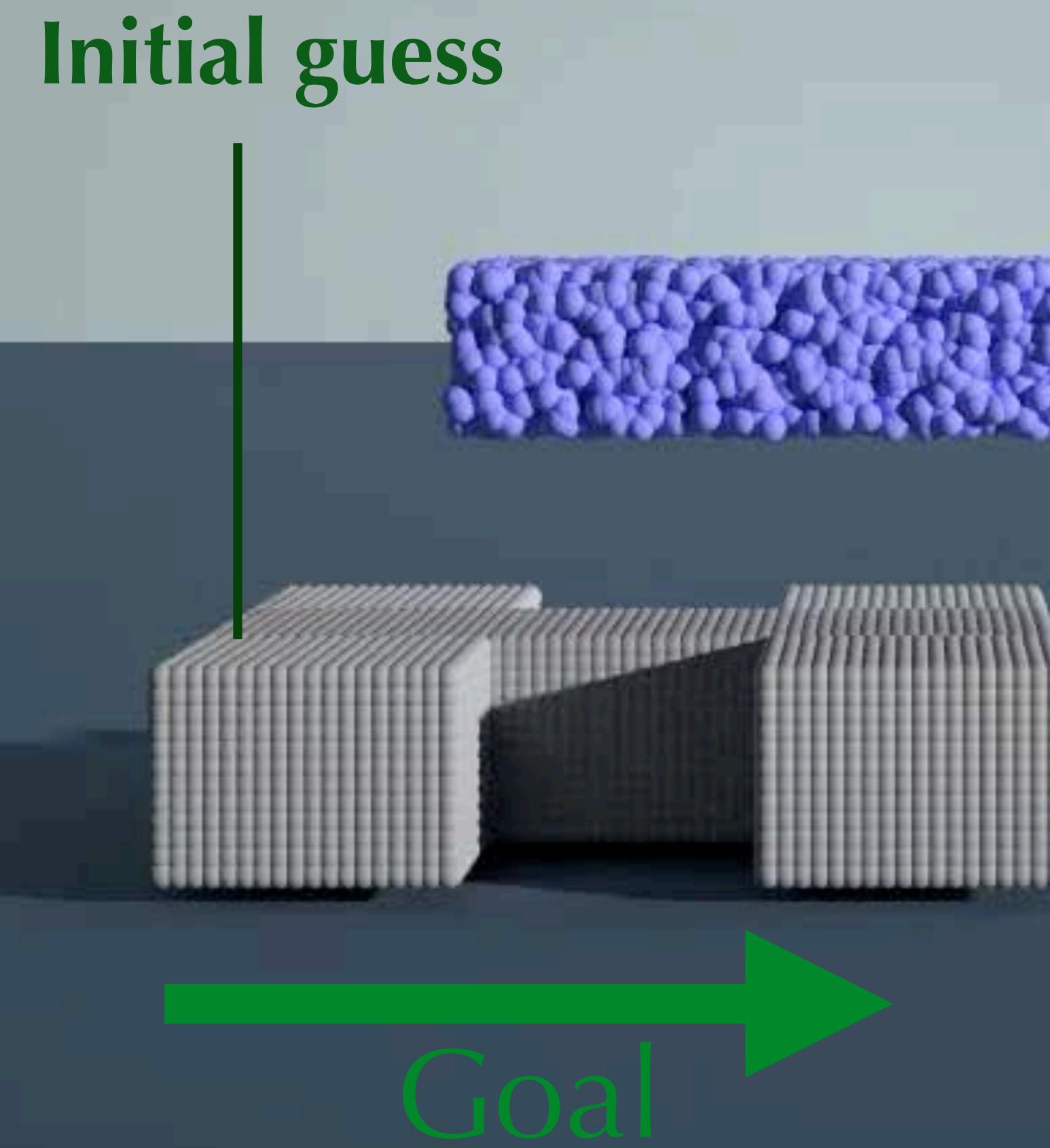
40 iterations



Reproduce: `python3 diffmpm3d.py`

Differentiable Liquid Simulation (3D)

Couples with elastic objects. 43.5K particles in total, 512 time steps, 450 gradient descent iter.
Run time=45min. Red=extension blue=contraction.

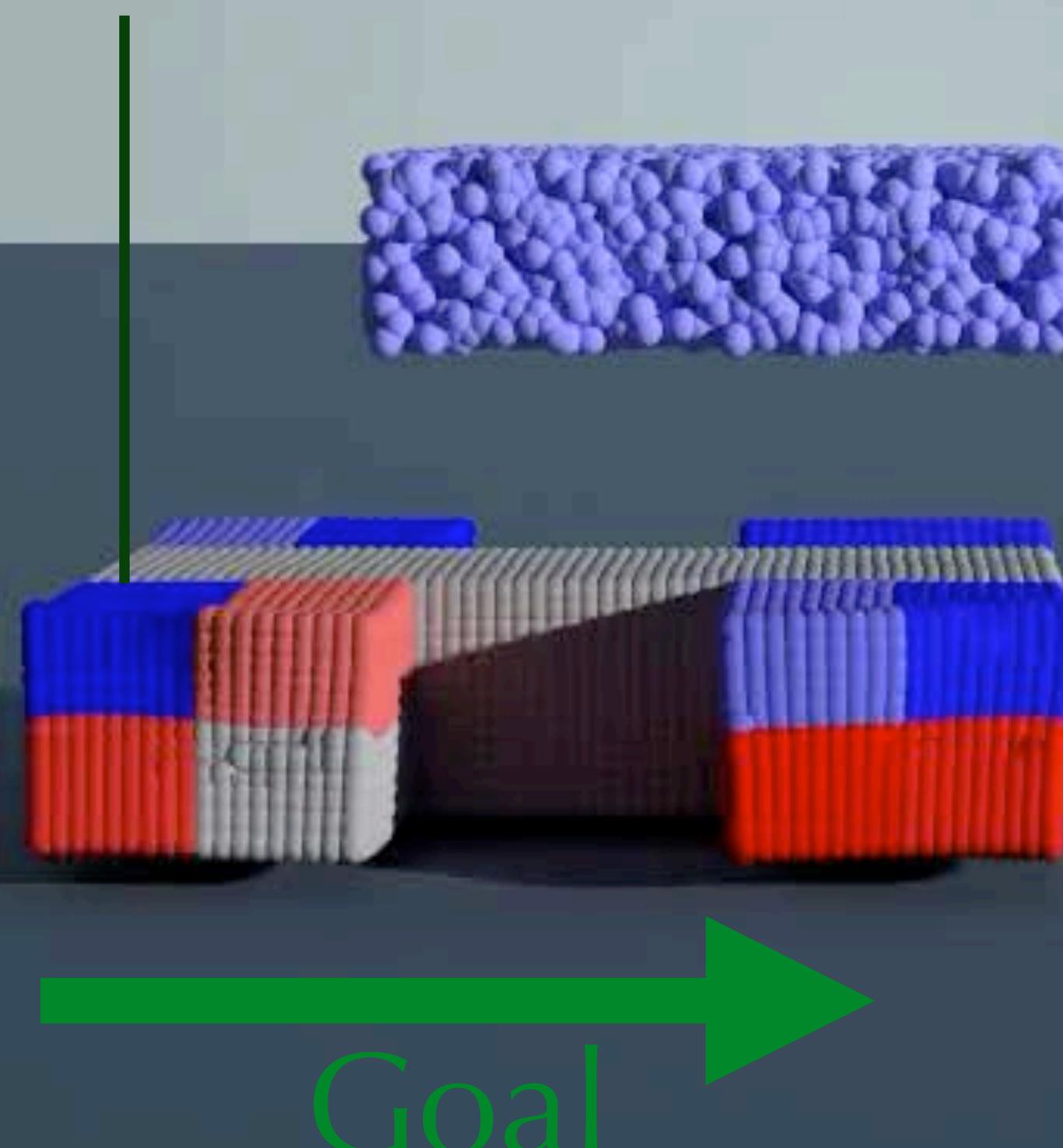


Reproduce: `python3 liquid.py`

Differentiable Liquid Simulation (3D)

Couples with elastic objects. 43.5K particles in total, 512 time steps, 450 gradient descent iter.
Run time=45min. Red=extension blue=contraction.

450 iterations



Reproduce: `python3 liquid.py`

Differentiable Mass-Spring Simulation

Random Initialization



Iteration 100

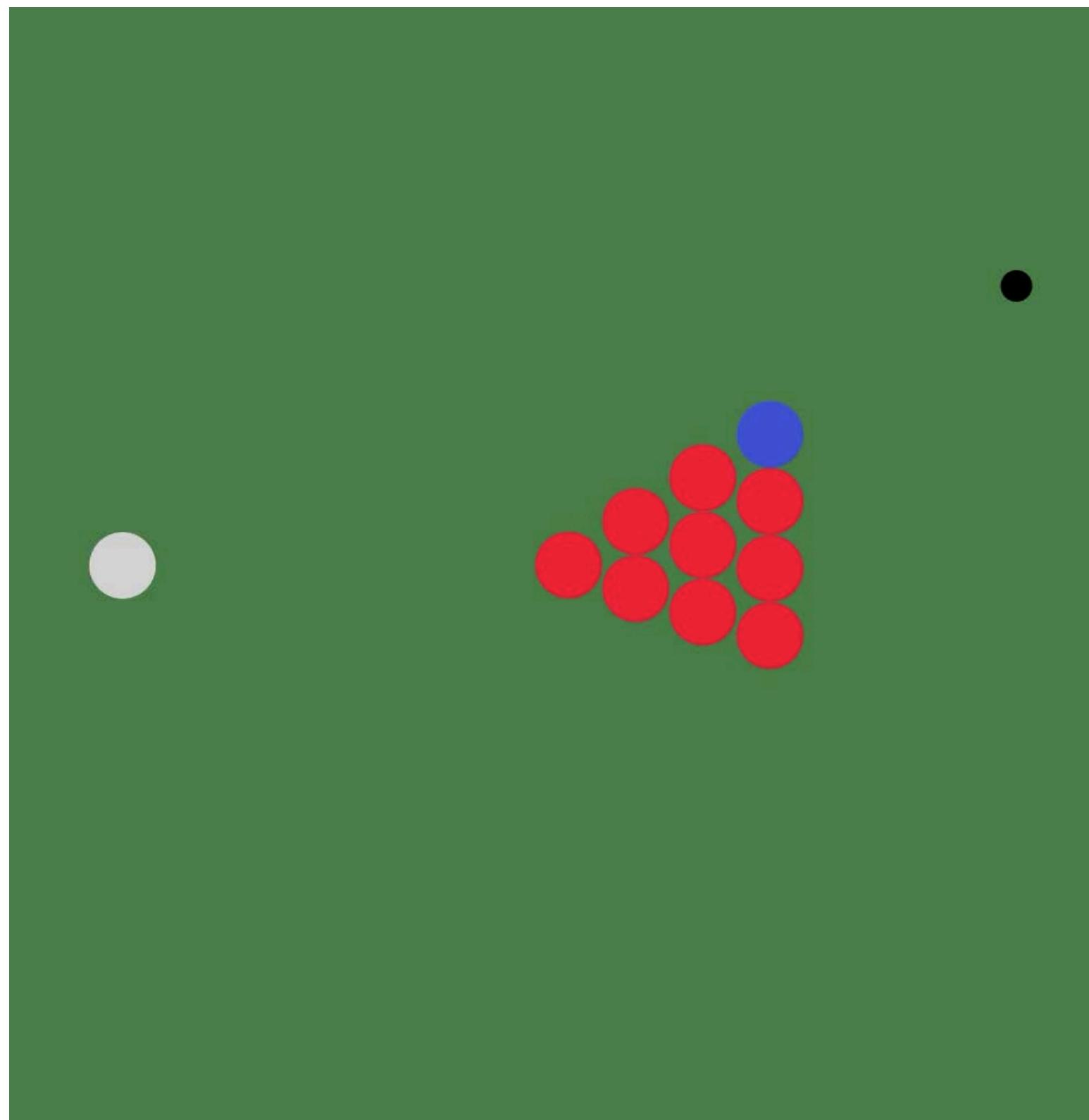


Three mass-spring robots that learn to move.
Closed-loop NN controller. Red=extension blue=contraction.

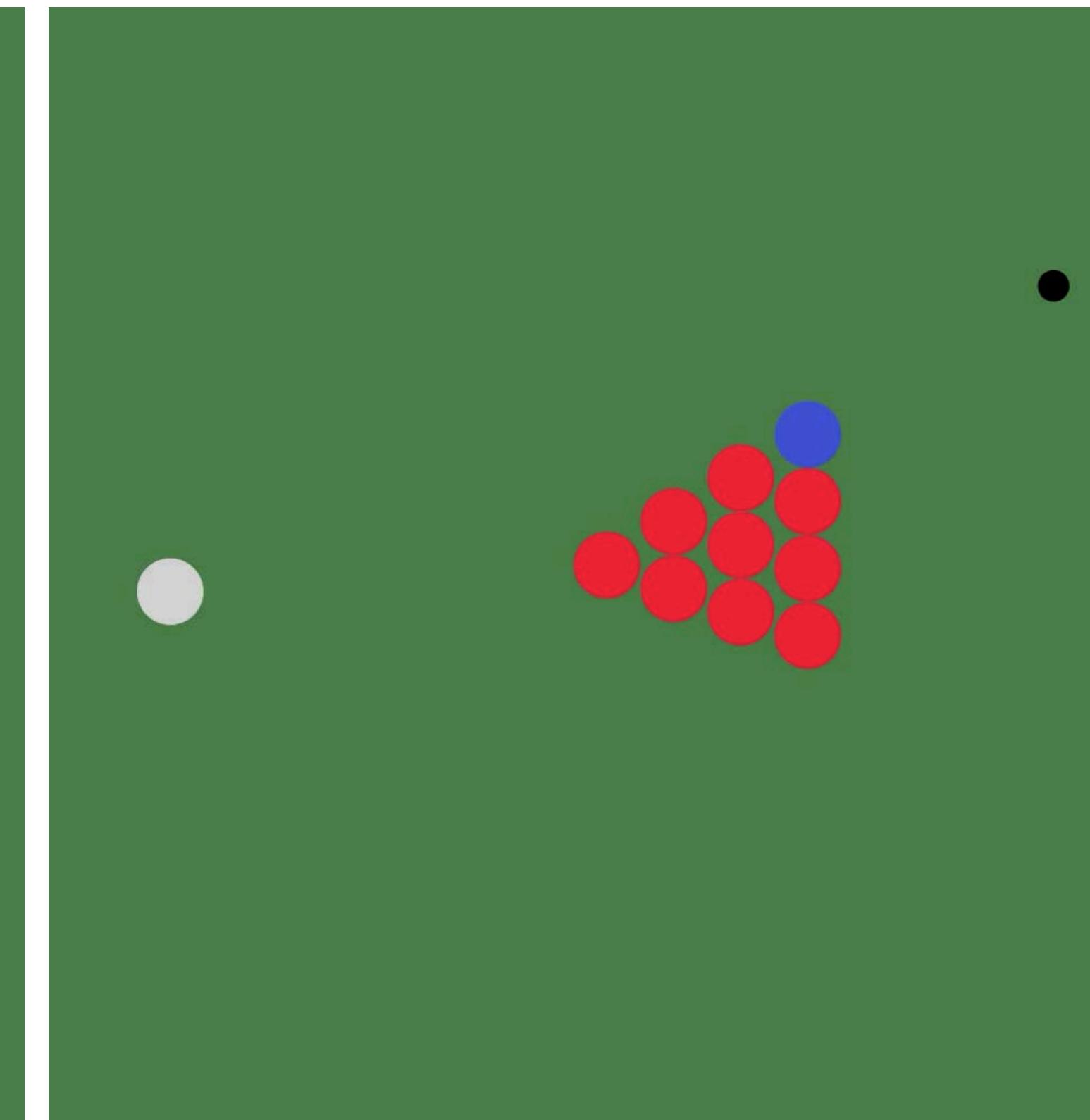
Reproduce: `python3 mass_spring.py 1/2/3 train`

Differentiable Billiard Simulation

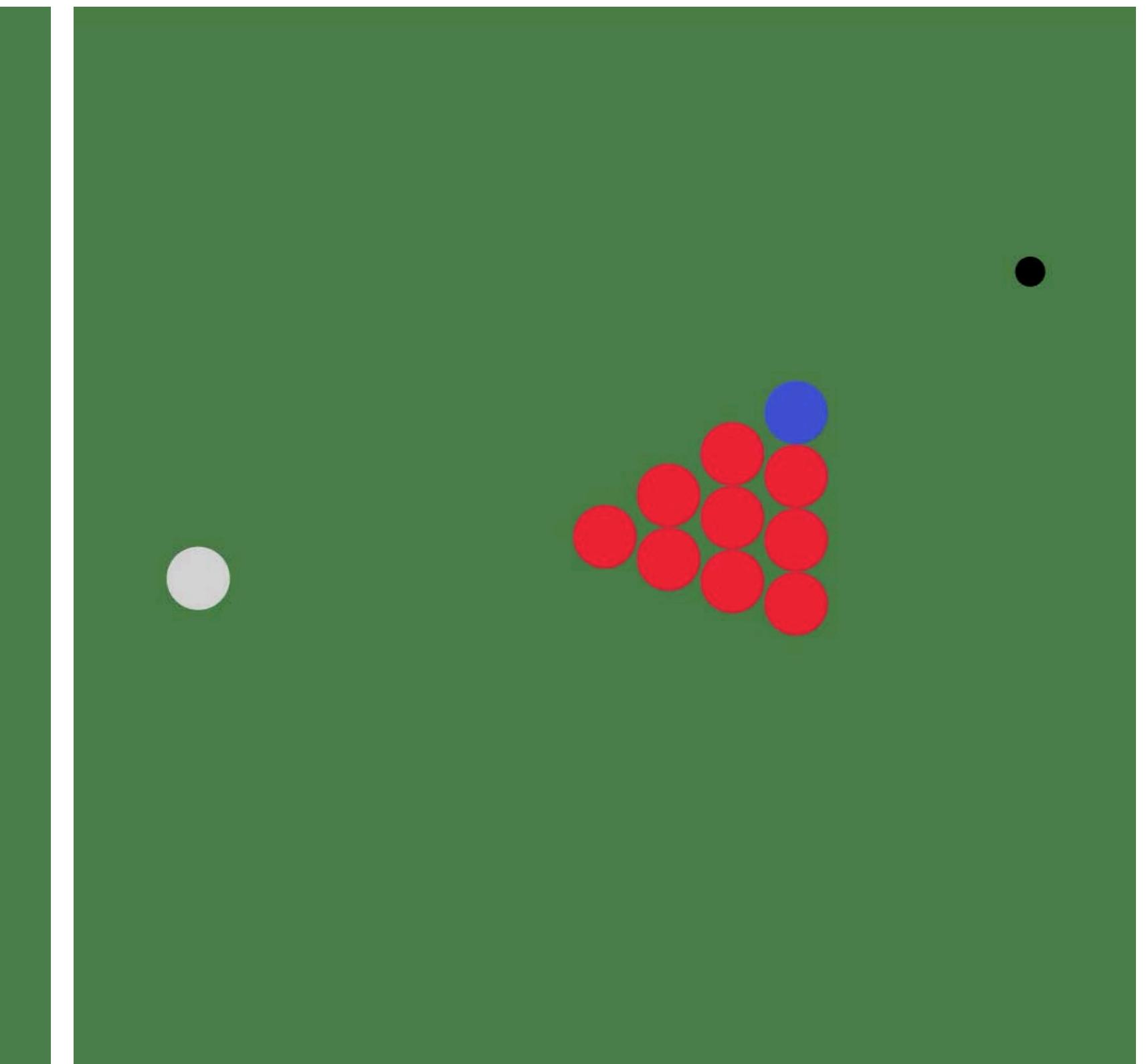
iter. 0



iter. 40



iter. 100

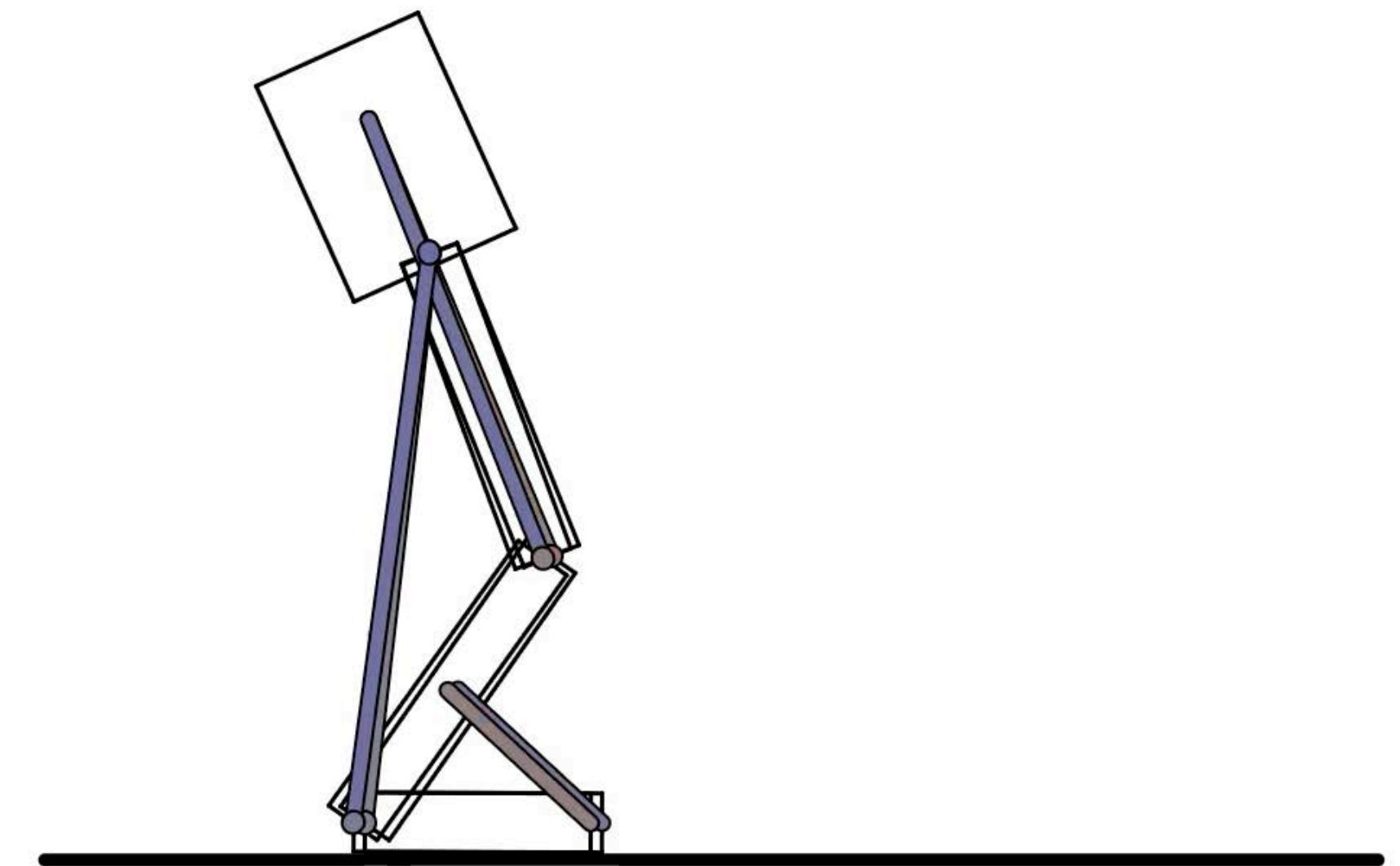
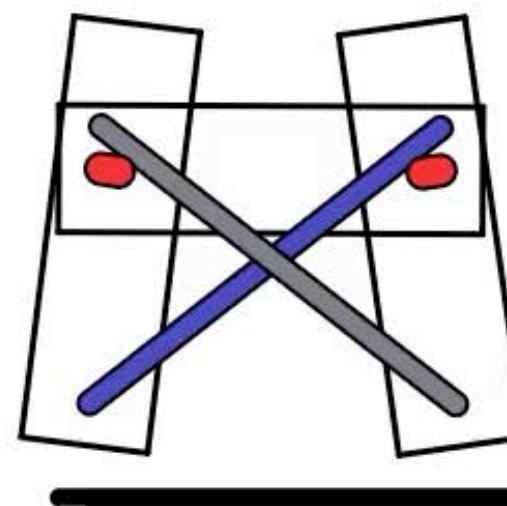


Optimize the **initial position** and **velocity** of the white ball so that the blue ball goes to the black destination

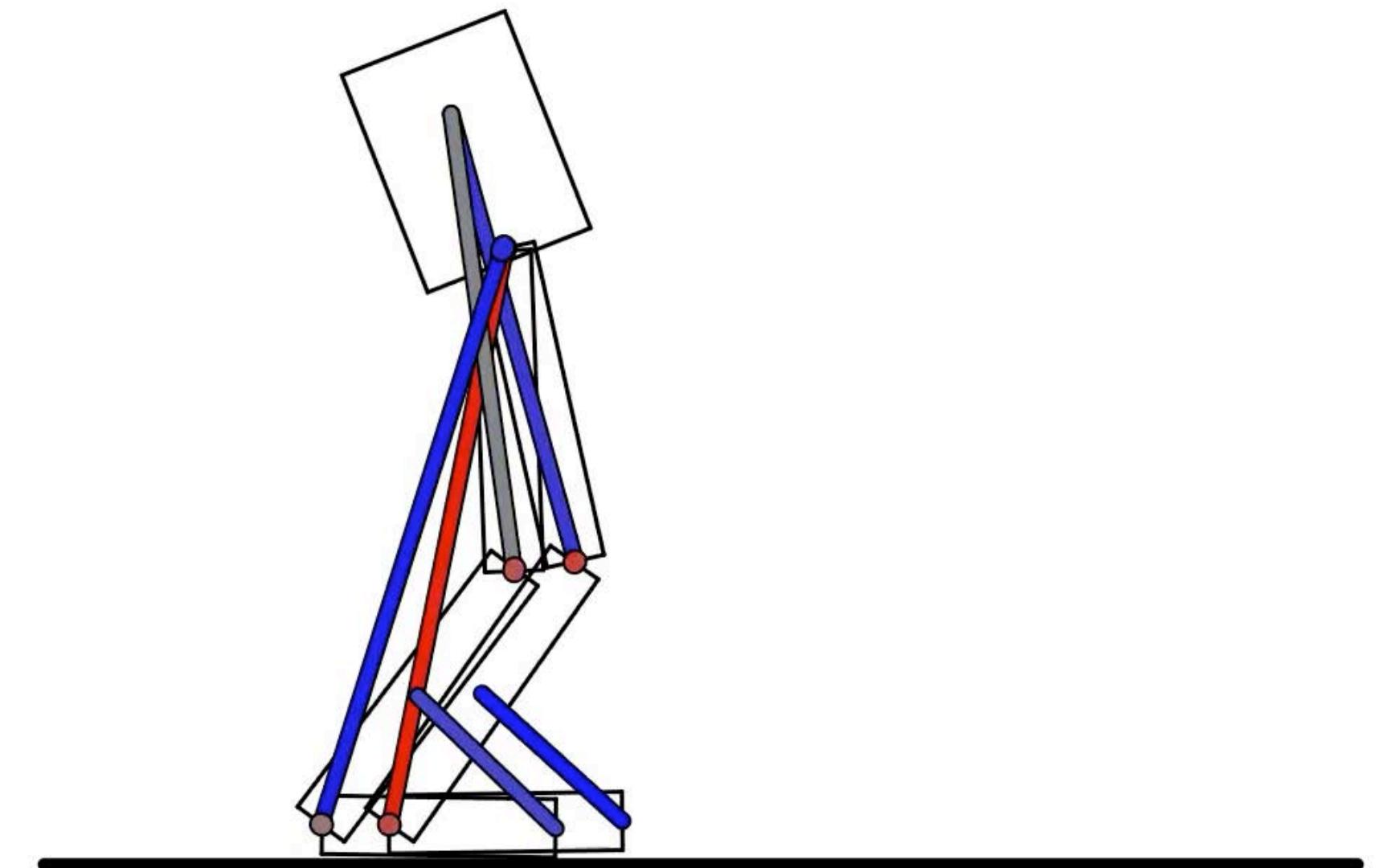
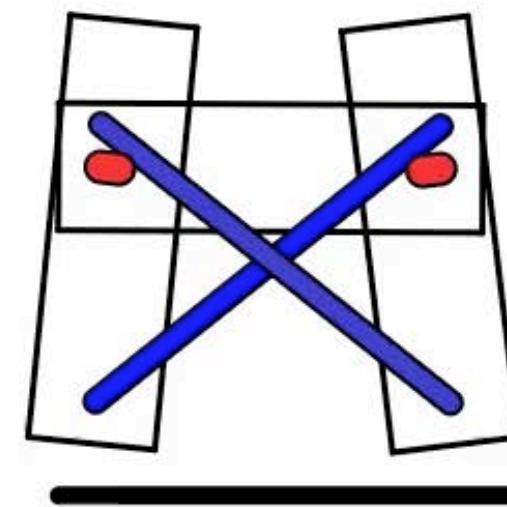
Reproduce: `python3 billiards.py`

Differentiable Rigid Body Simulation

Random Initialization



Iteration 20



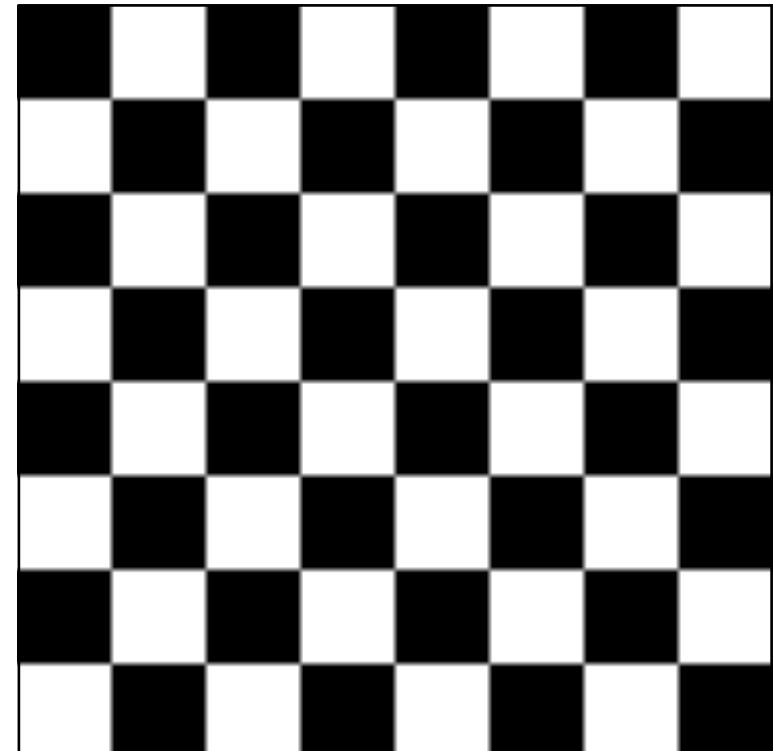
Two rigid body robots that learn to move.

Closed-loop controller. Red=extension blue=contraction.

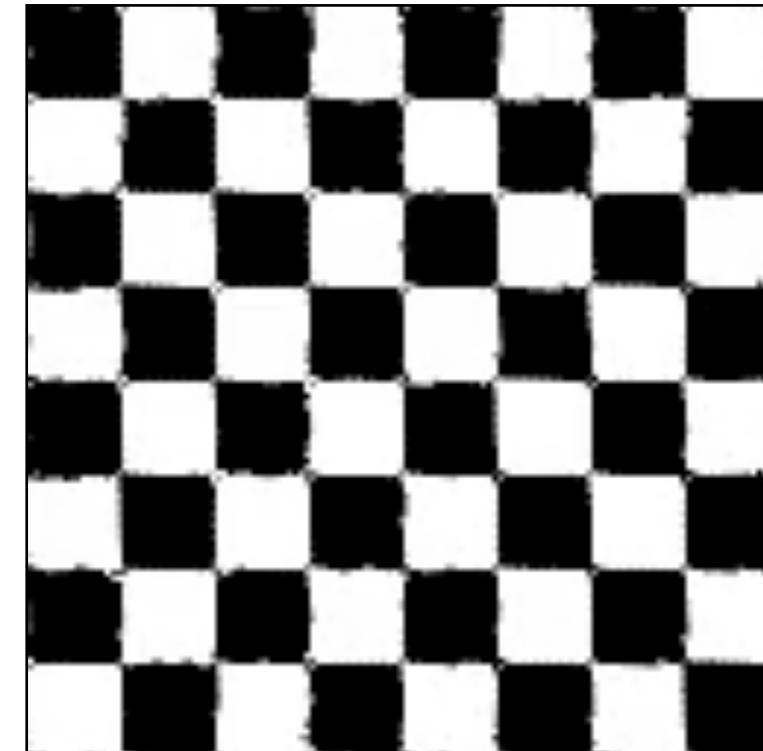
Reproduce:
python3 rigid_body.py 1/2 train

Differentiable Incompressible Fluid Simulation

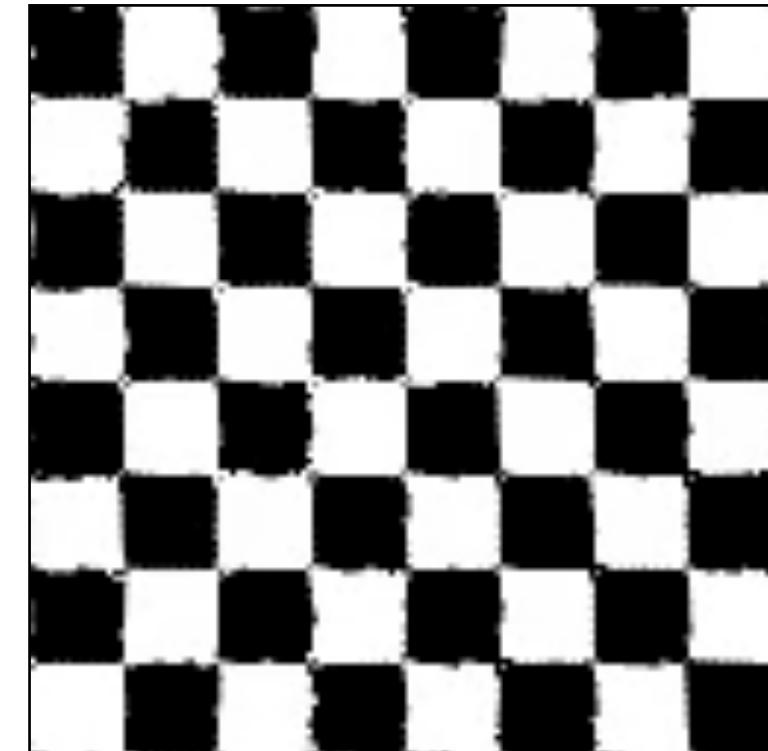
iter. 0



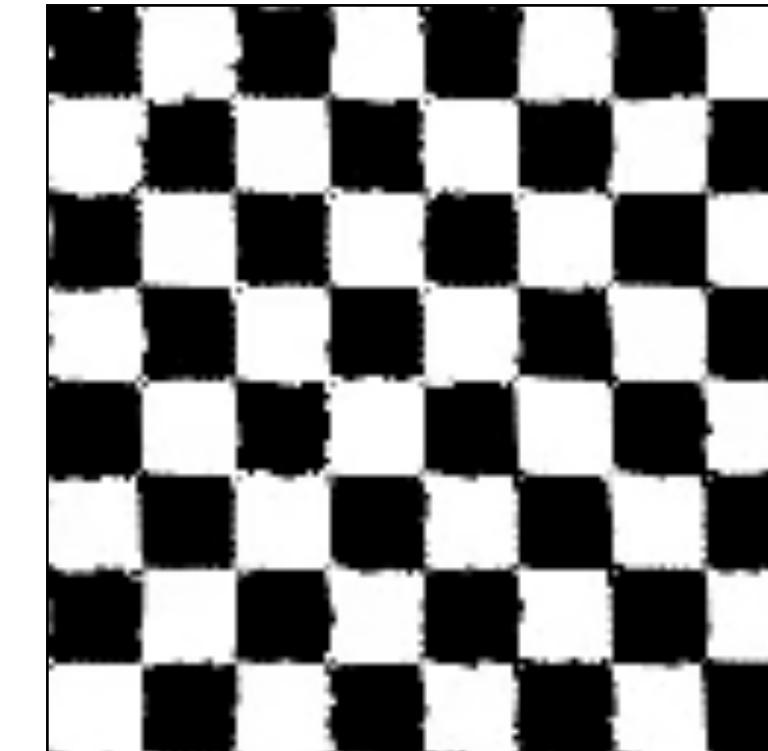
iter. 10



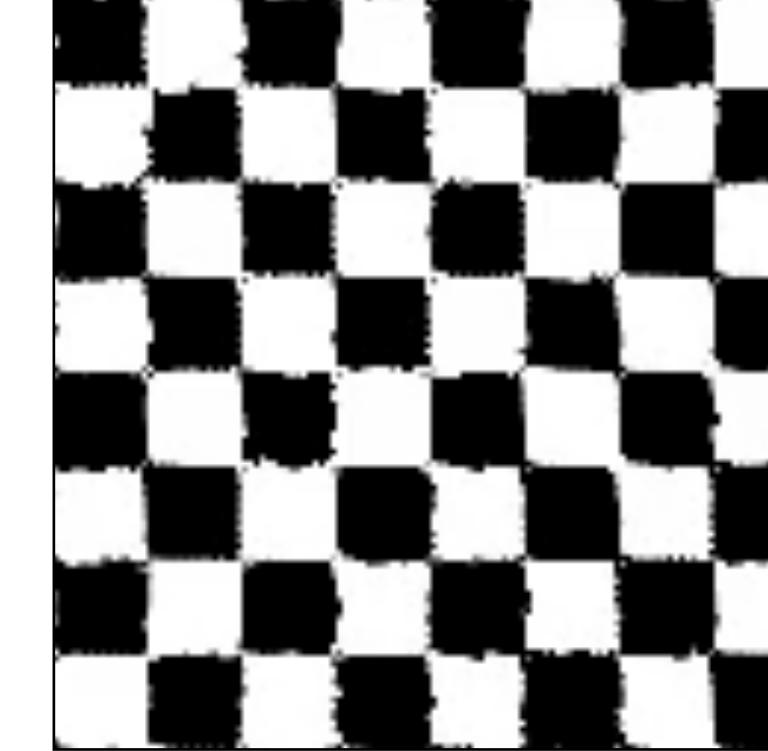
iter. 30



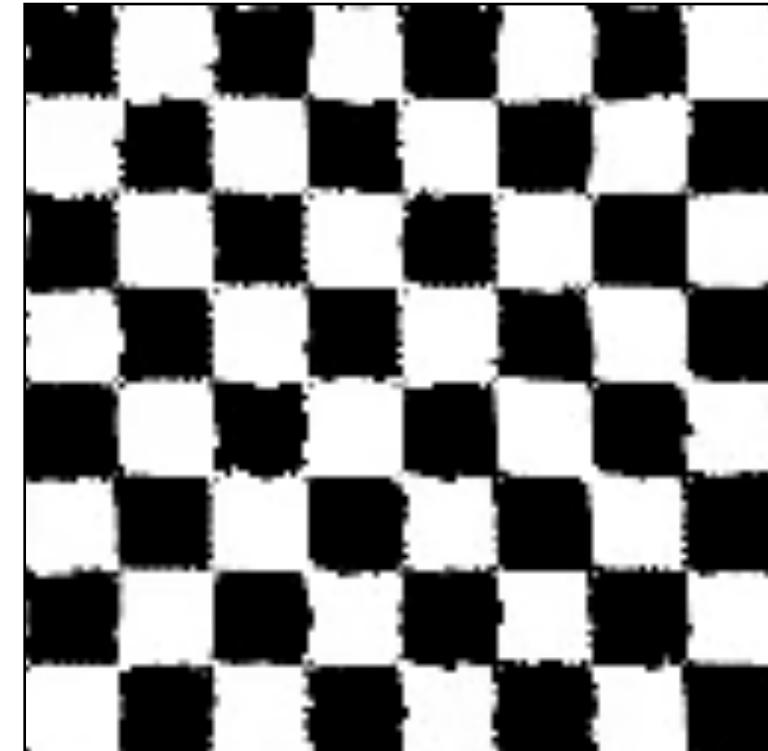
iter. 60



iter. 120



iter. 200



Optimize the **initial velocity field** so that the ink forms “Taichi” after 100 time steps.

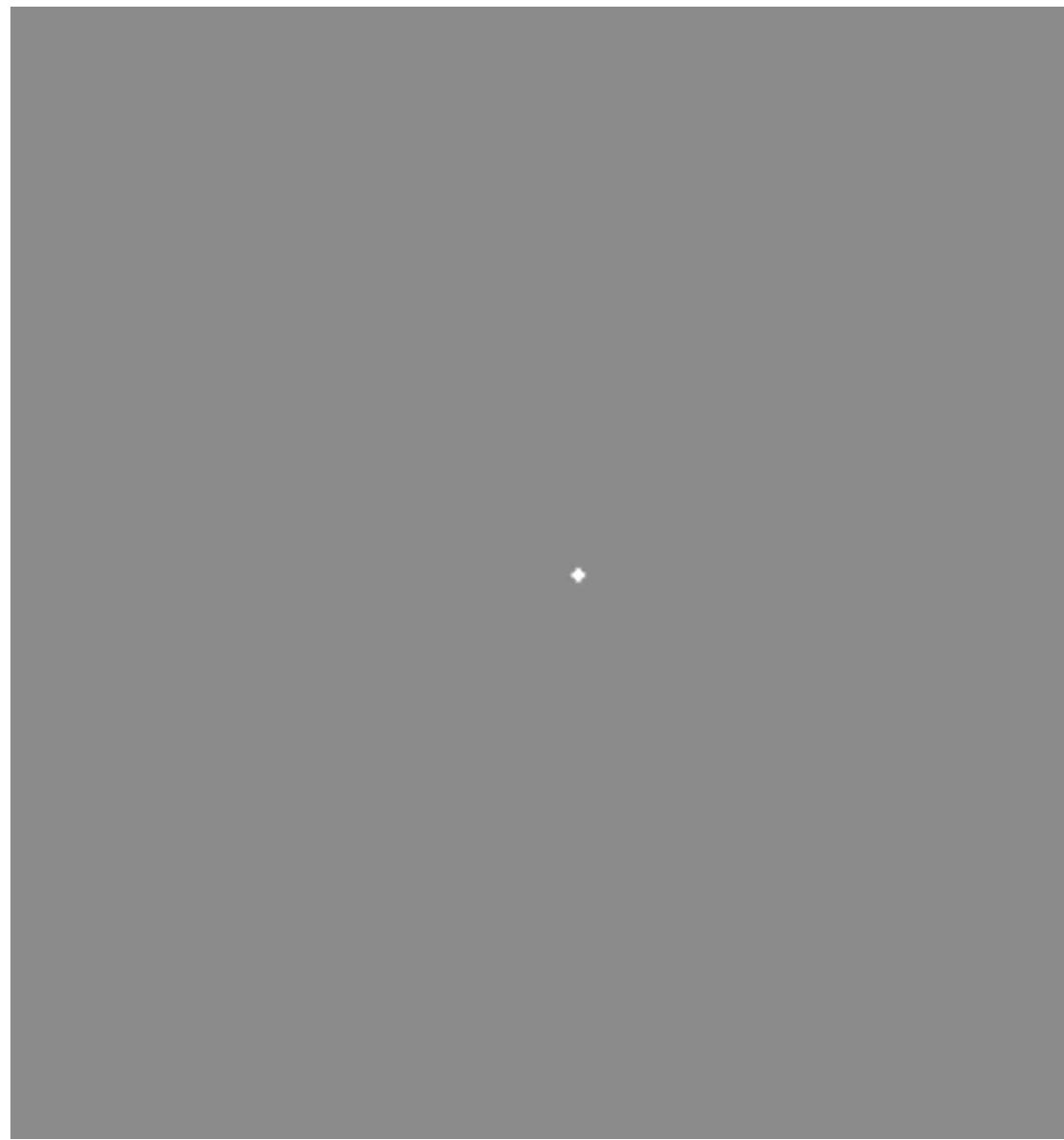
10 Jacobi iterations are applied per time step for incompressibility.

Optimized using 200 gradient descent iterations.

Reproduce: `python3 smoke.py`

Differentiable Water Wave Simulation

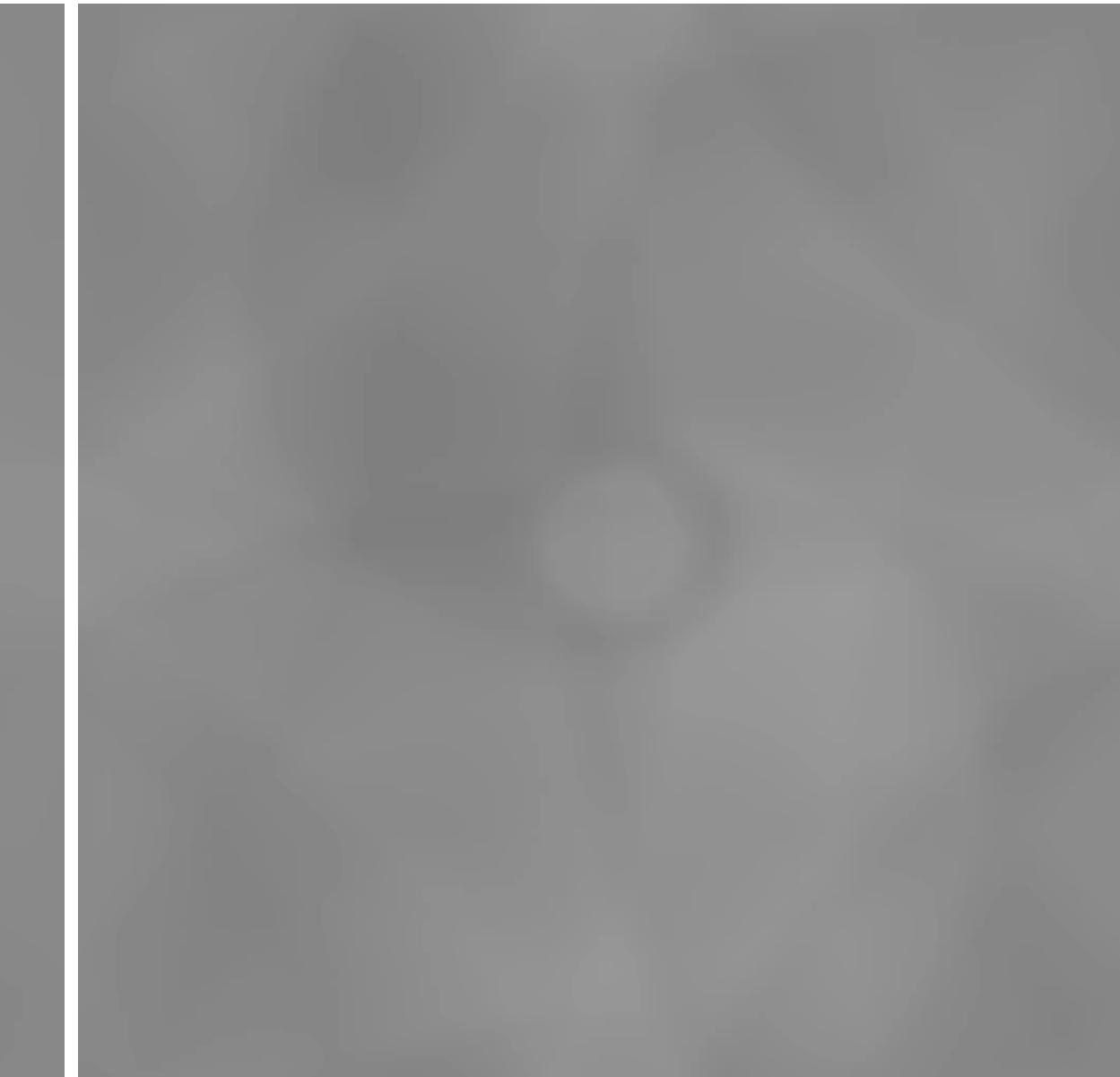
Center Activation



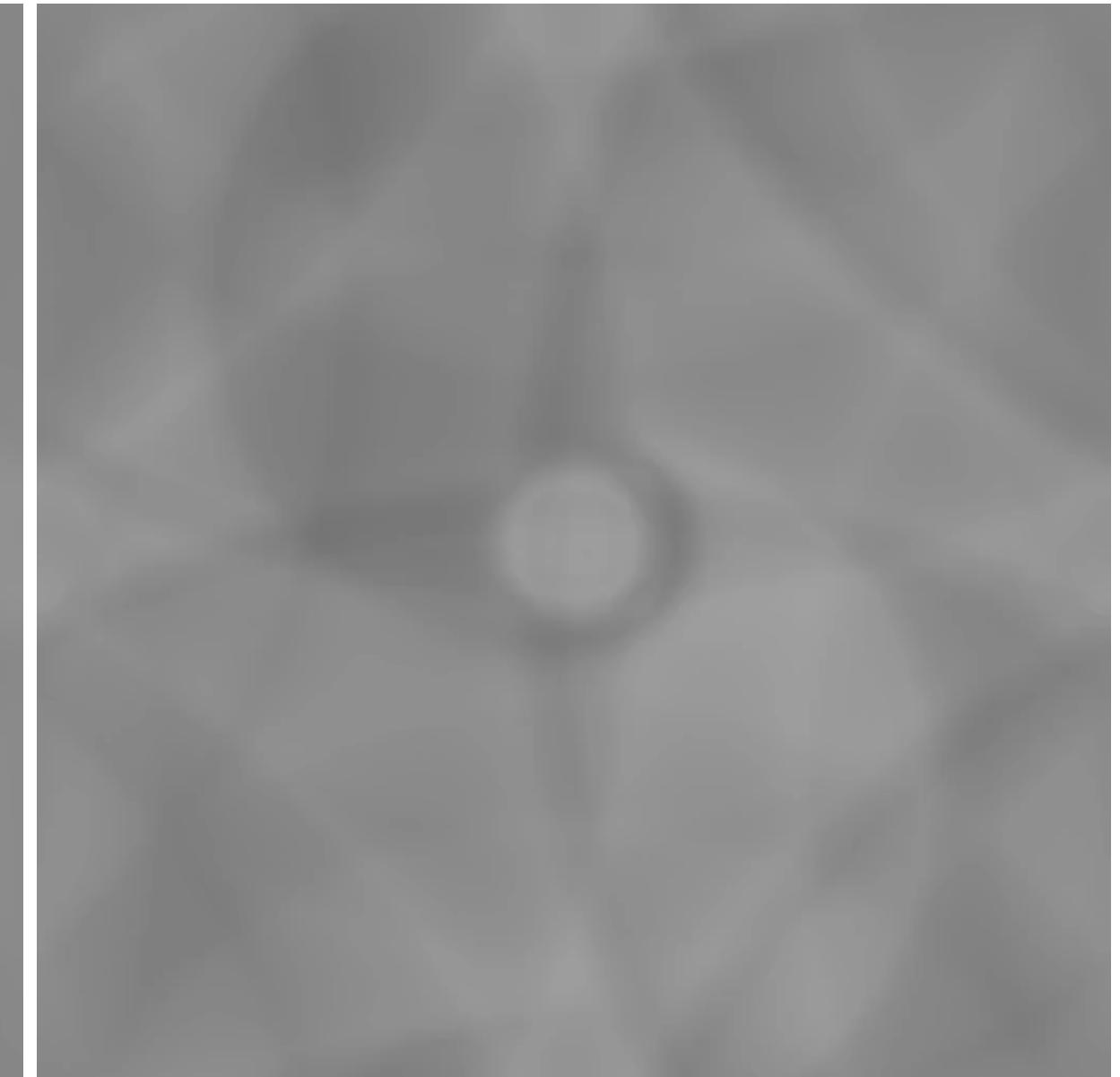
Iteration 20



Iteration 60



Iteration 180

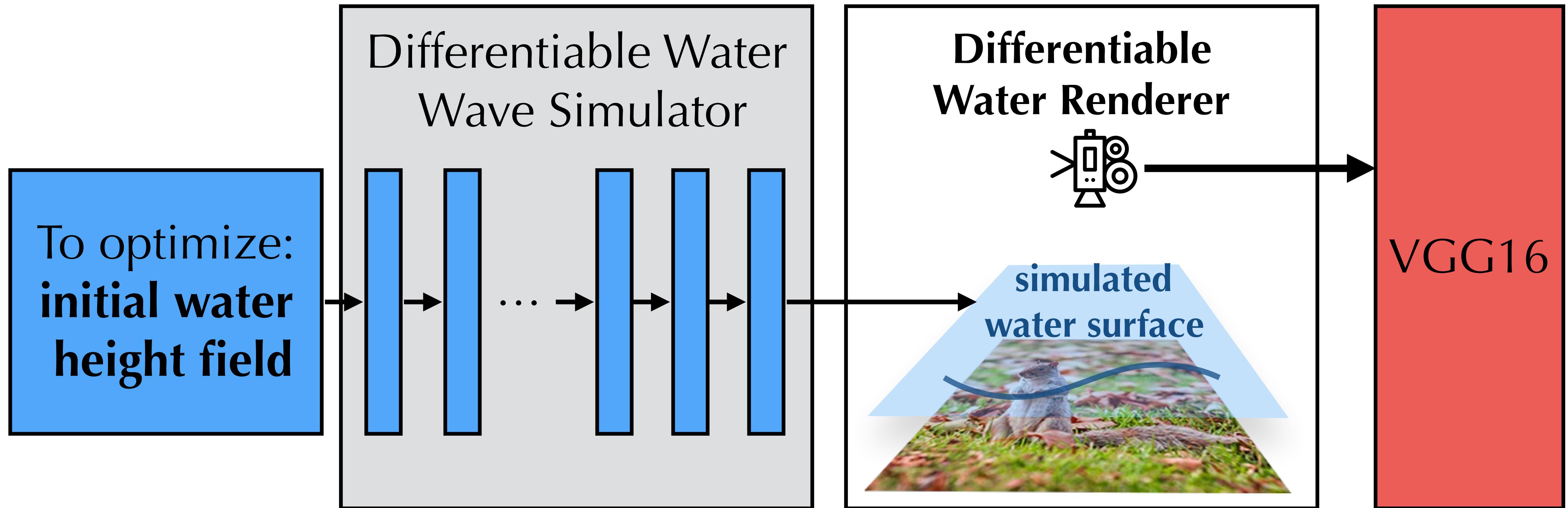


Height field fluid simulation.

Optimize the initial height field so that it forms “Taichi” after 256 time steps.

Reproduce: `python3 wave.py`

Differentiable Water Renderer



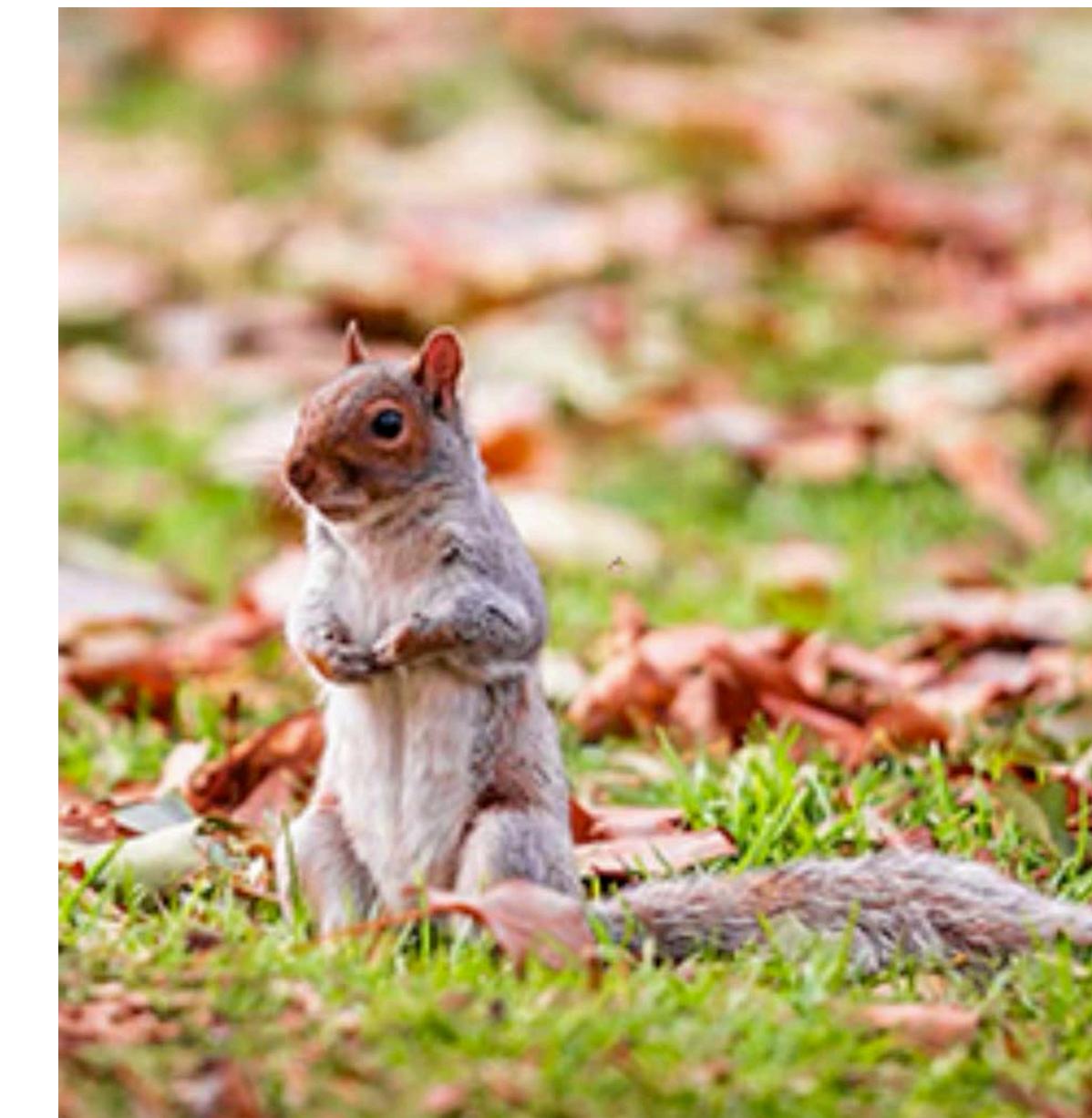
We wrote a differentiable water renderer to simulate refraction.
Then we connect the shader with the water wave simulator and VGG16.

Differentiable Water Renderer

Input image:



Center ripple



Iter. 10

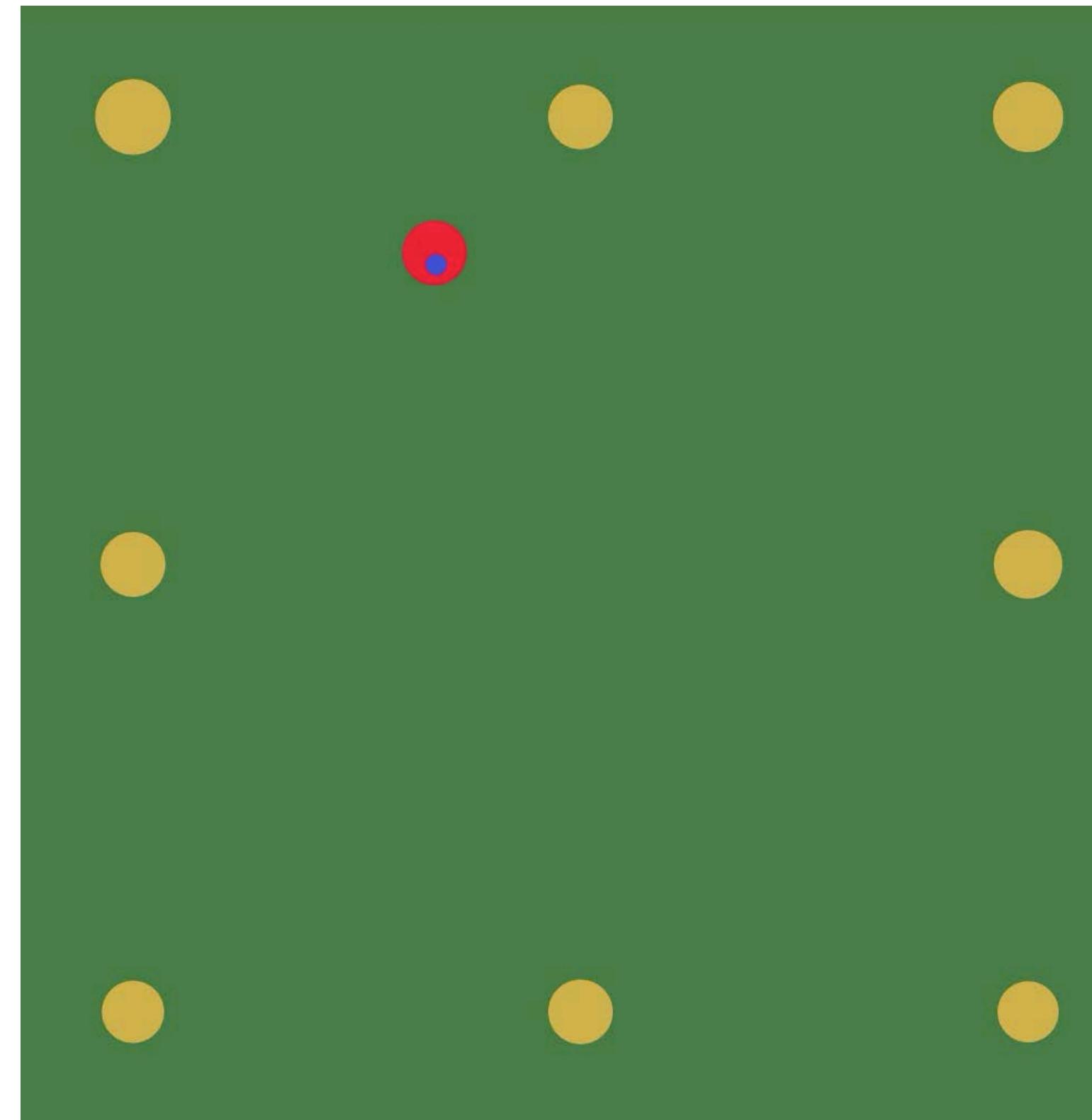


The optimization goal is to find an initial water height field,
so that after simulation and shading,
VGG16 thinks the squirrel image is a goldfish.

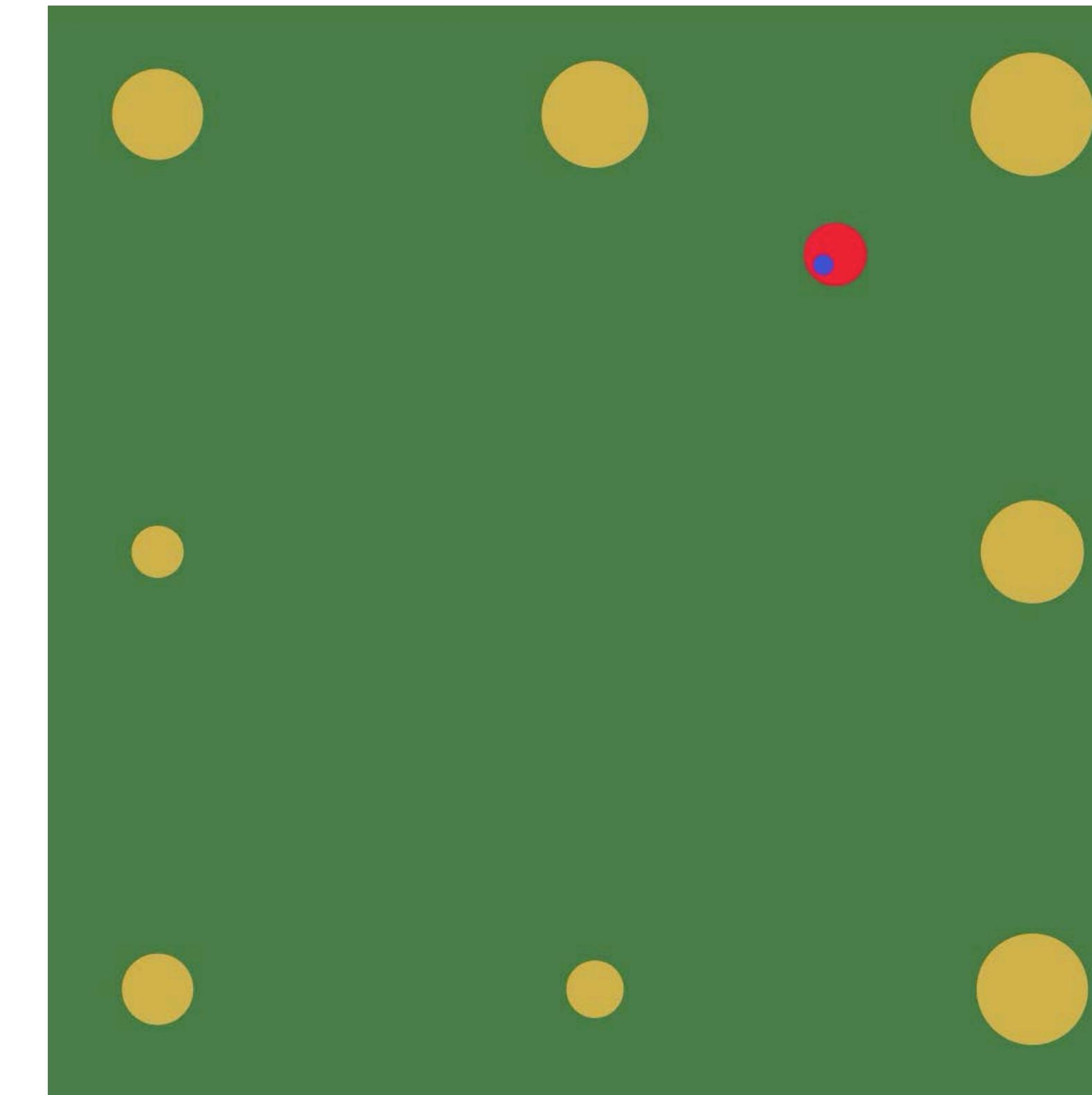
Reproduce: `python3 water_renderer.py`

Differentiable Electric Field Simulation

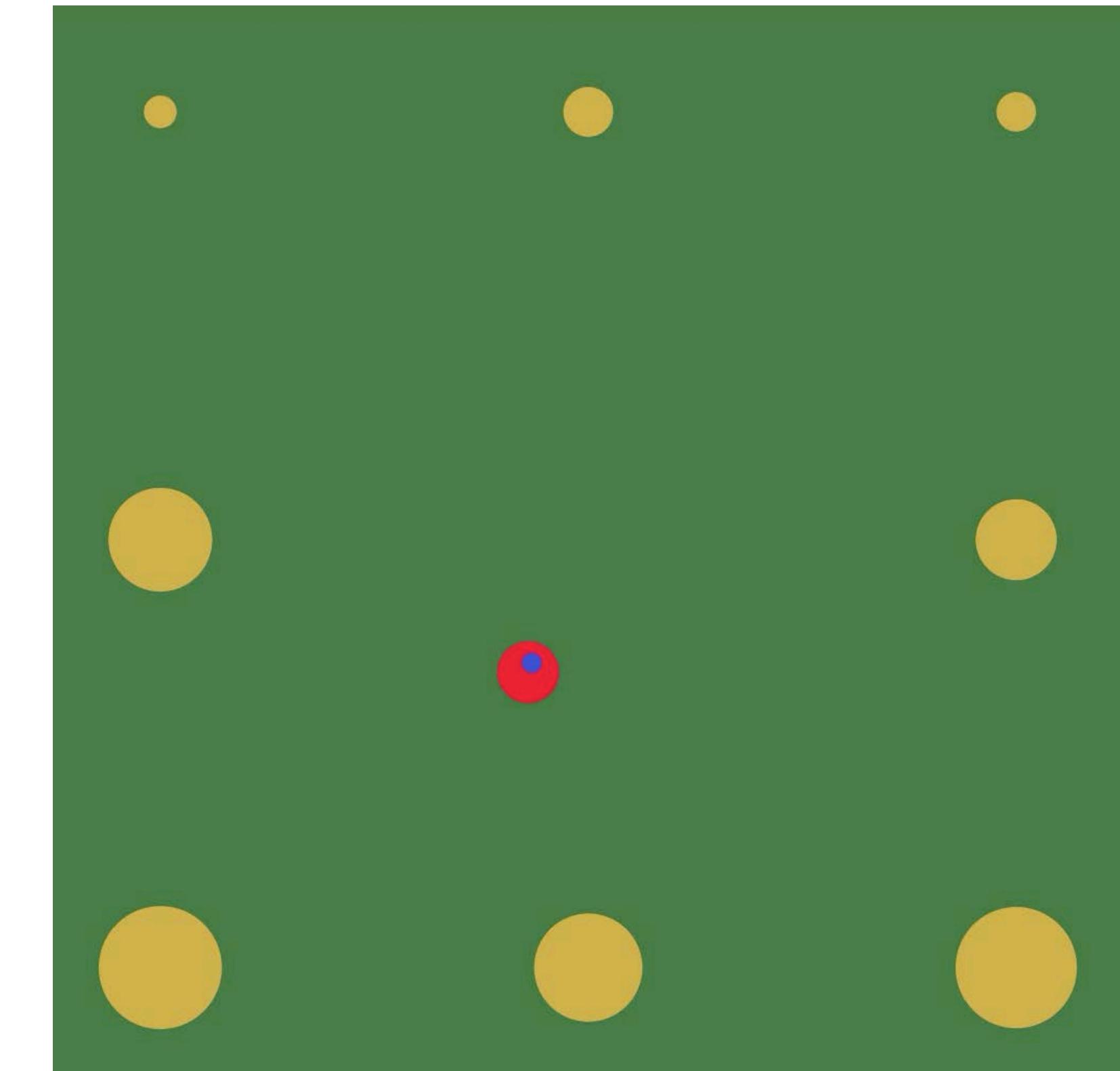
Iteration 0



Iteration 5000



Iteration 5200



The eight electrodes (yellow) changes its amount of charge to repulse the red ball, so that it follows the blue dot.

Reproduce: `python3 electric.py`

Building Robust Differentiable Physical Simulators

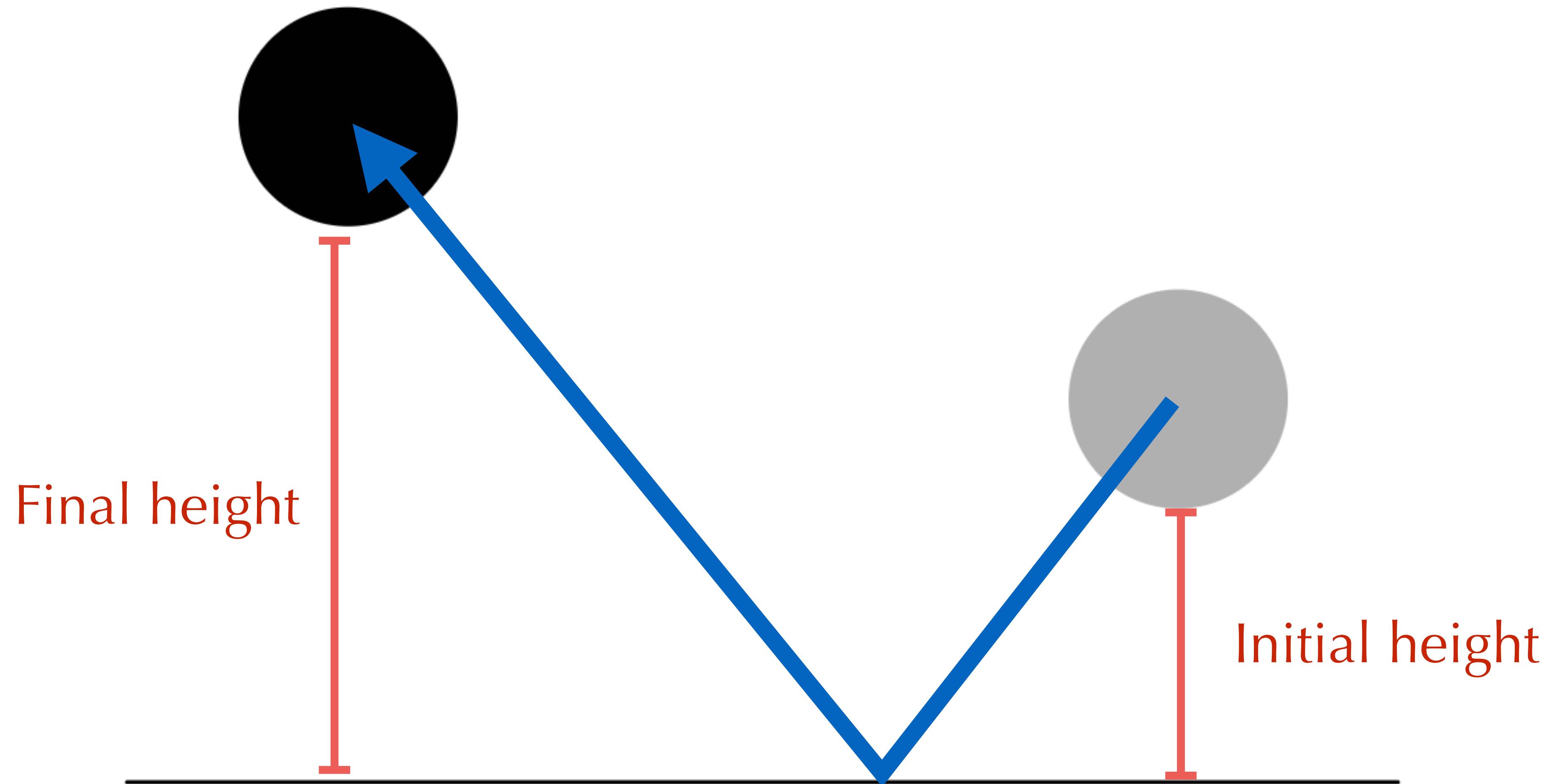
Differentiating physical simulators does not always yield useful gradients of the physical system being simulated.

How Gradients Go Wrong



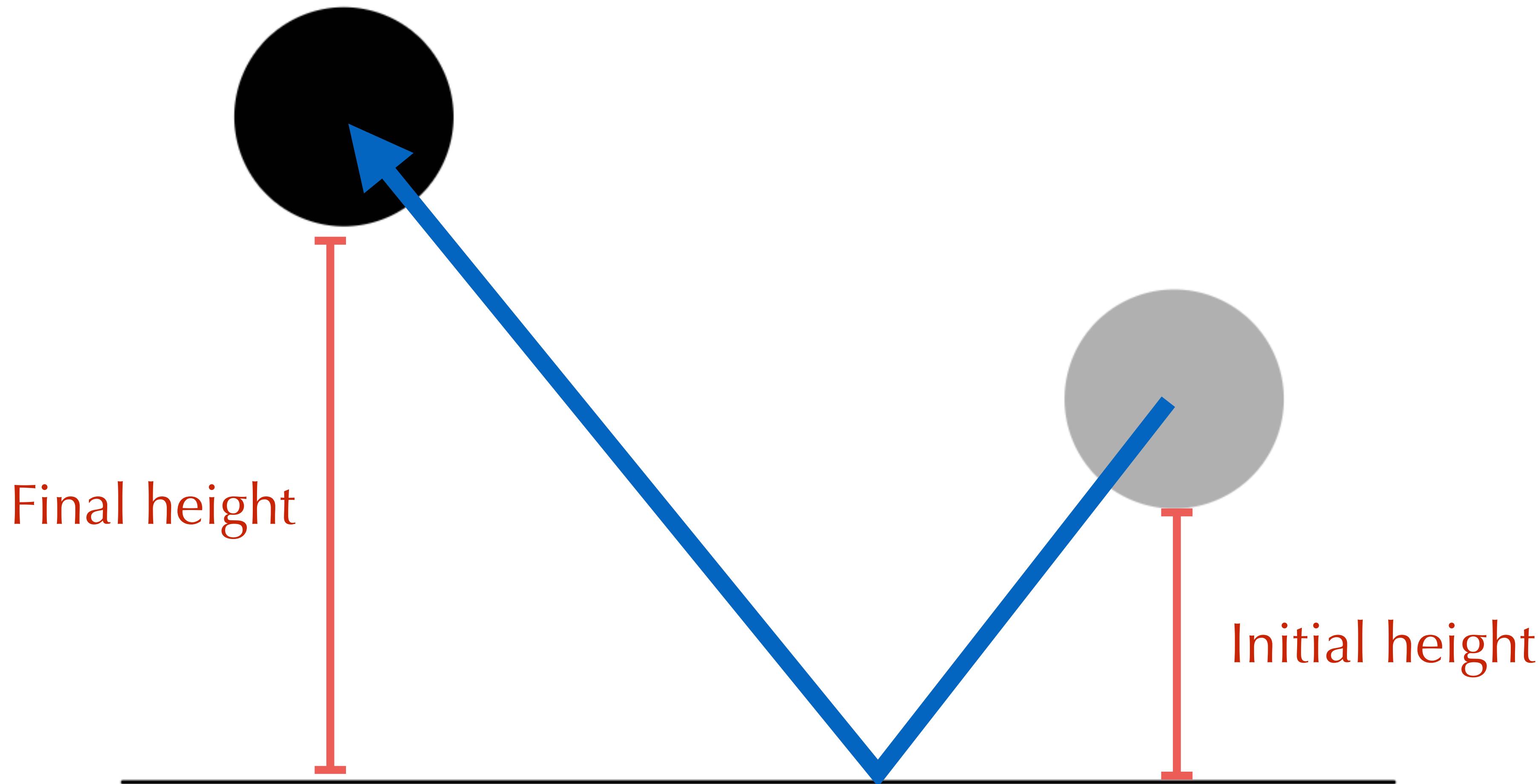
Consider this example where a rigid ball hits a friction-less ground.
No gravity, no friction, fully elastic collision.

How Gradients Go Wrong



Consider this example where a rigid ball hits a friction-less ground.
No gravity, no friction, fully elastic collision.

How Gradients Go Wrong



Initial height + final height = time \cdot v_y =constant

How Gradients Go Wrong



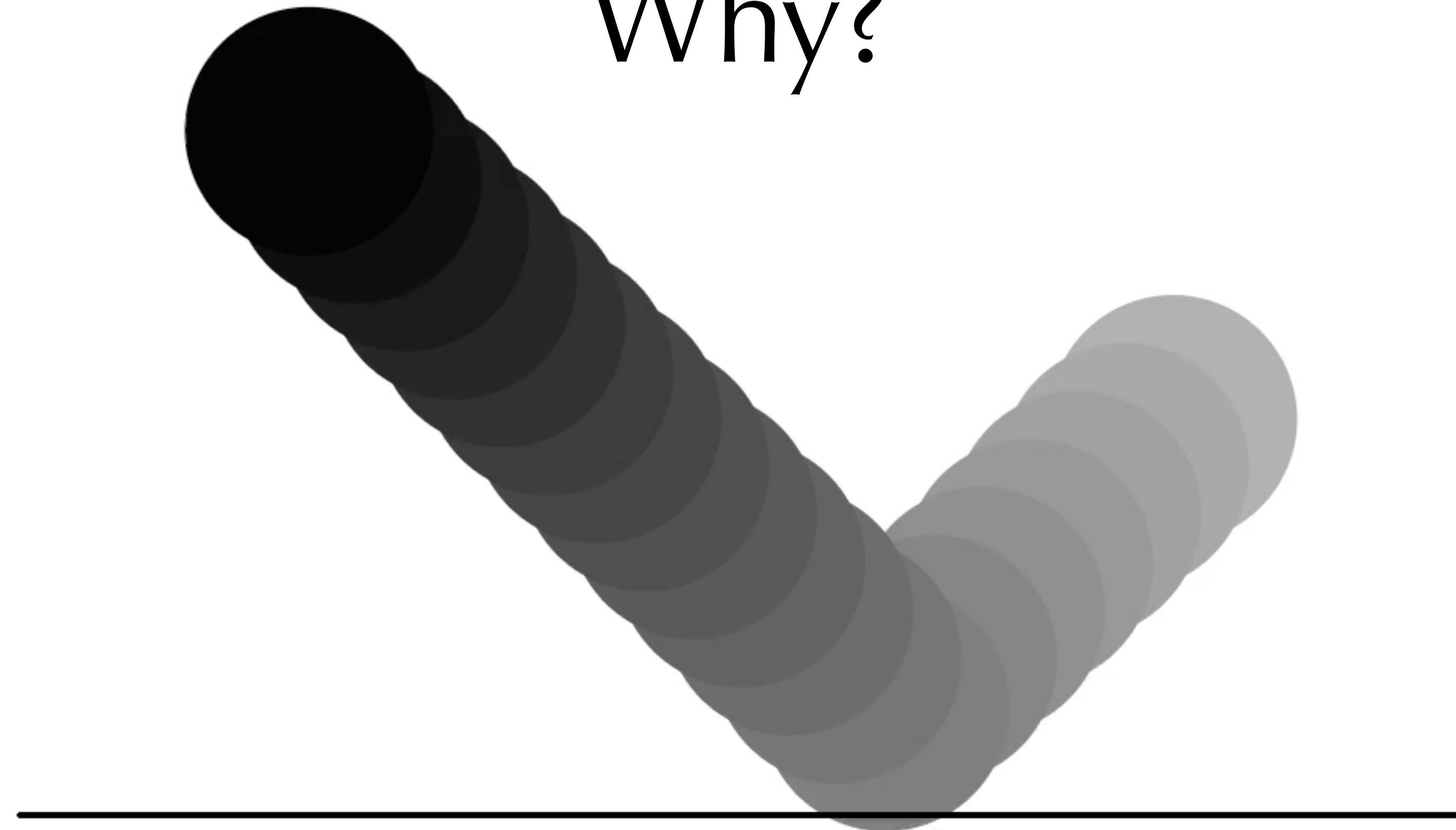
Initial height + final height = **constant** $\rightarrow \frac{\partial \text{final height}}{\partial \text{initial height}} = -1$

But the differentiable simulator may tell you

$$\frac{\partial \text{final height}}{\partial \text{initial height}} = 1$$

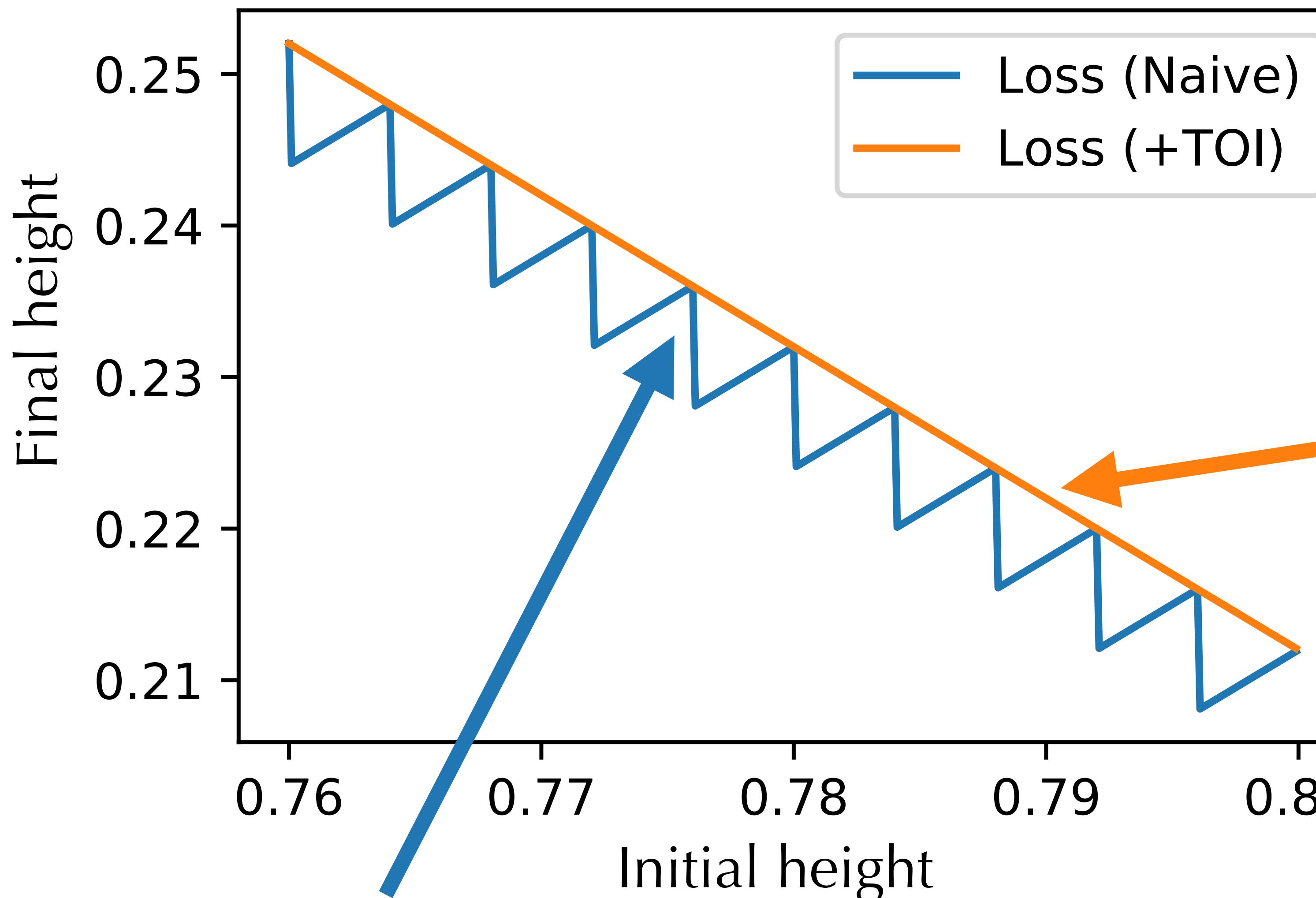
(instead of -1)

Why?



Using a large time step, it is easy to see that the final height actually **raises** together with the initial height, except for a few discontinuities.

The Effect of Time of Impact on Gradients

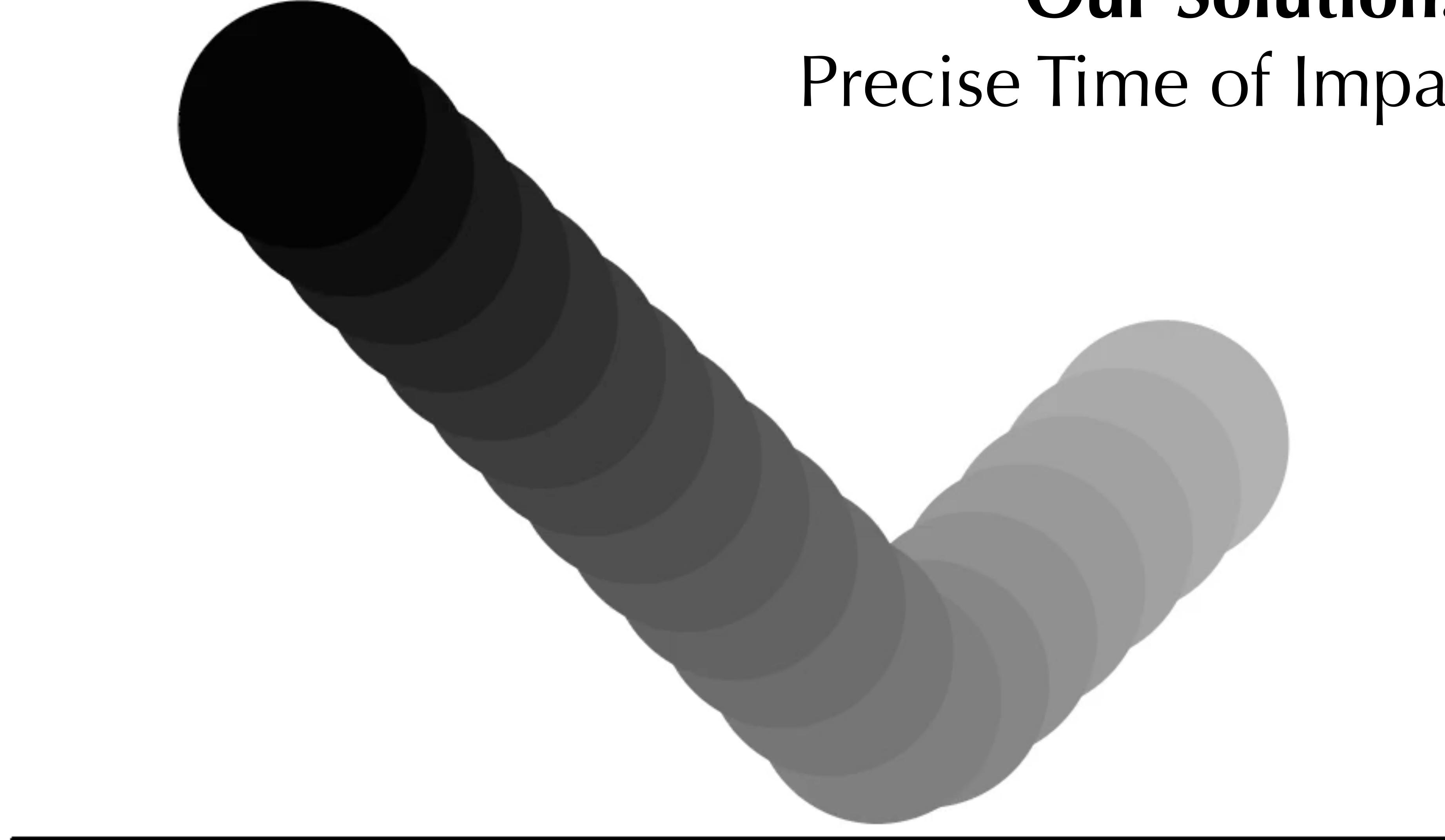


Question:
how can we get this?

A naive time integrator leads to saw-tooth like this: correct
tendency, but completely wrong gradients

Our Solution:

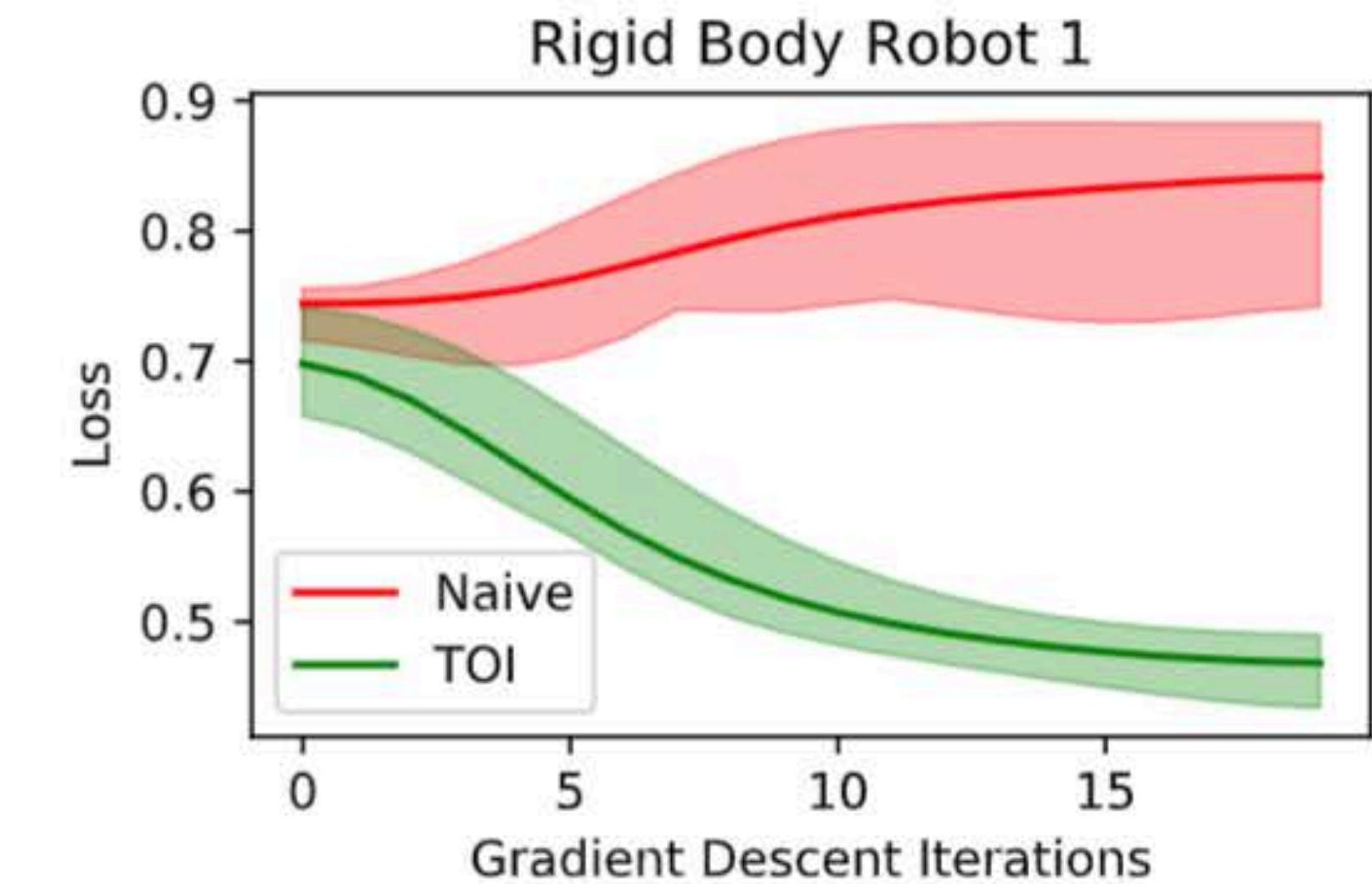
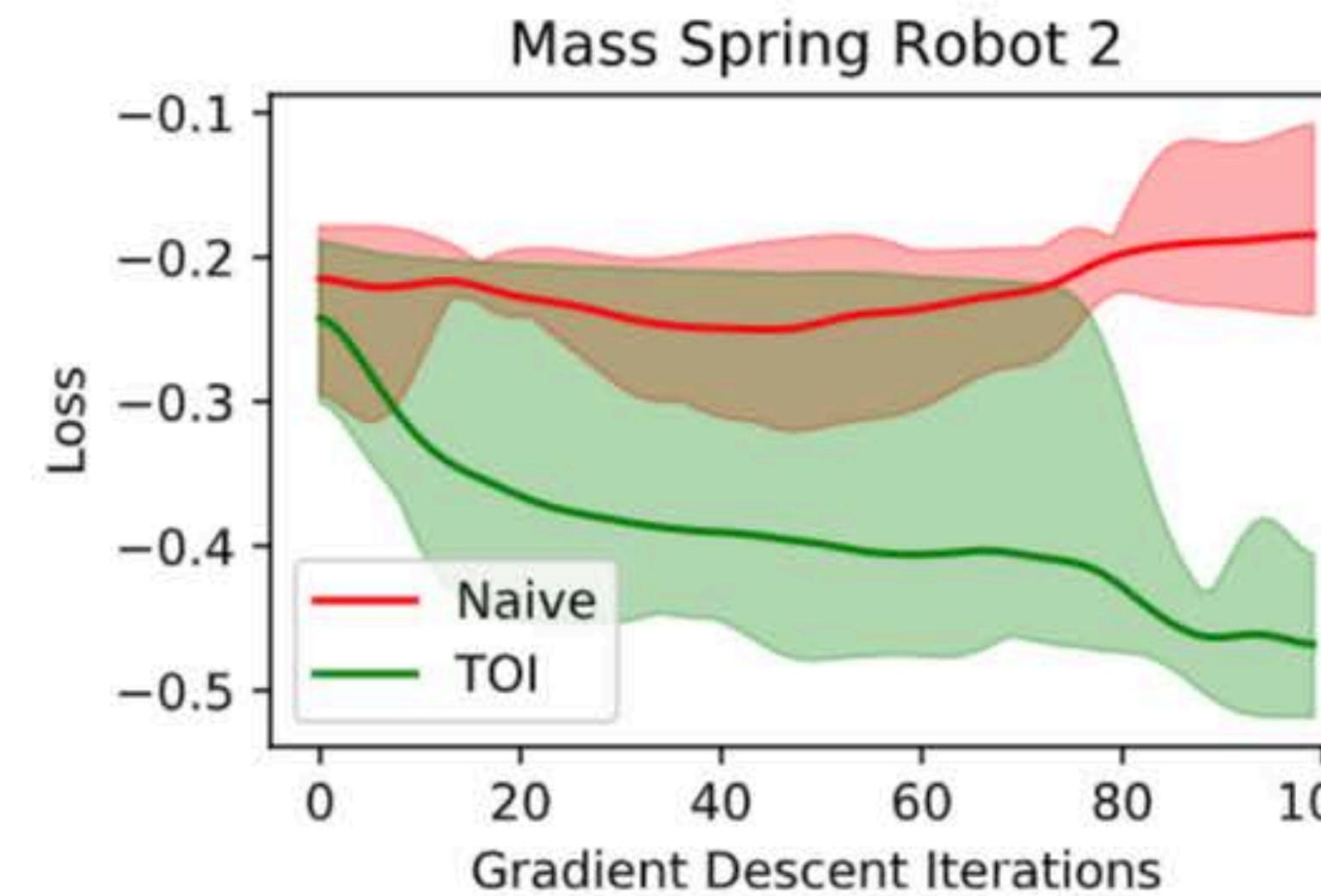
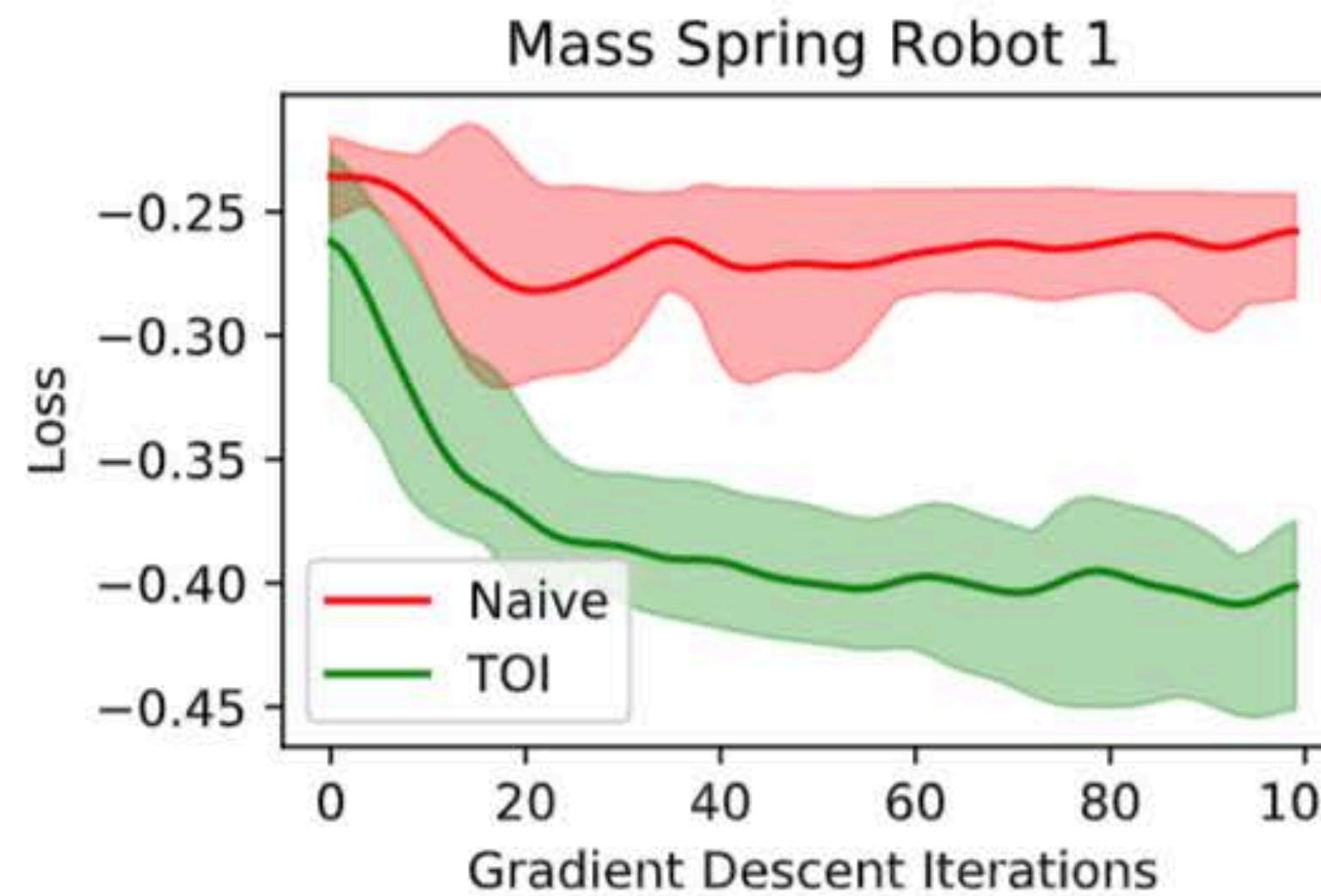
Precise Time of Impact (TOI)



Initial height + final height = **constant**

$$\rightarrow \frac{\partial \text{final height}}{\partial \text{initial height}} = -1$$

After fixing “wrong” gradients,
robots now learn much better.

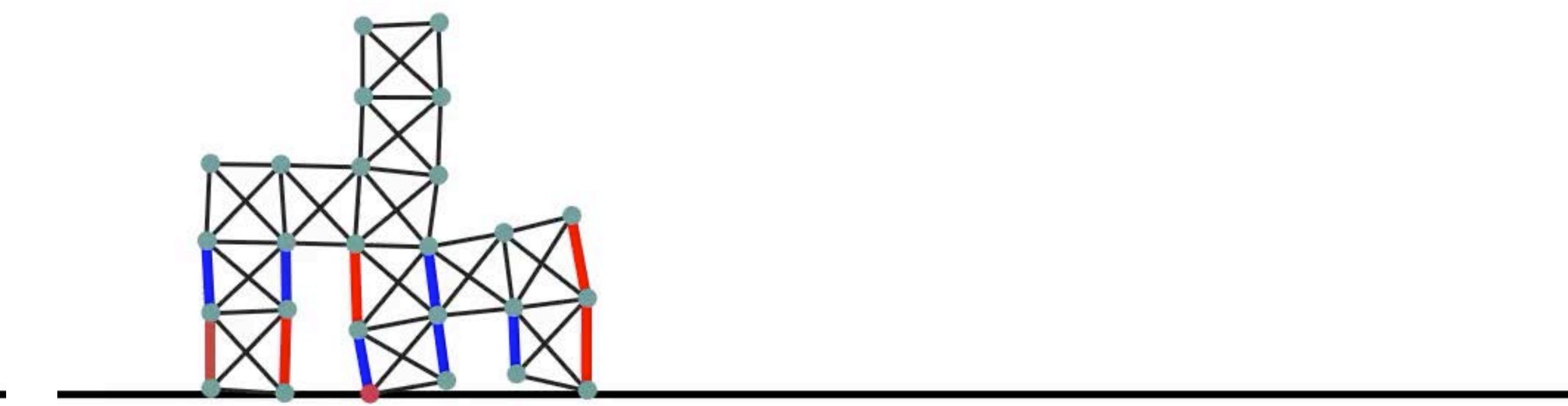


Optimize the Controller (needs gradients)

Optimized without TOI



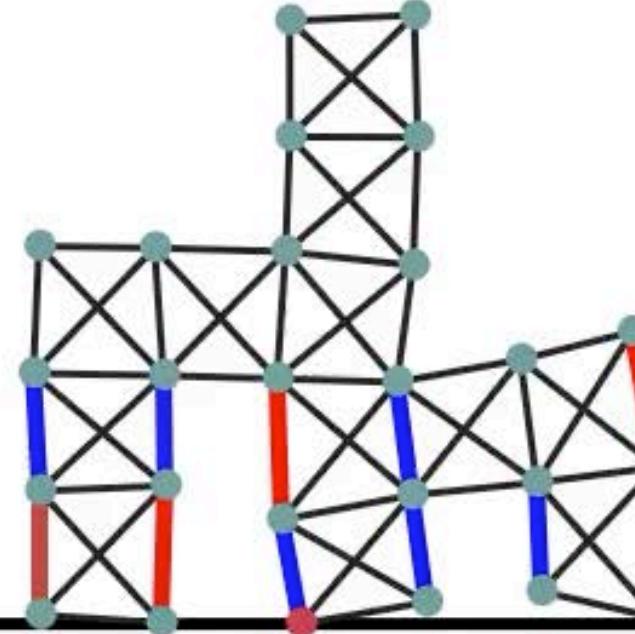
Optimized with TOI



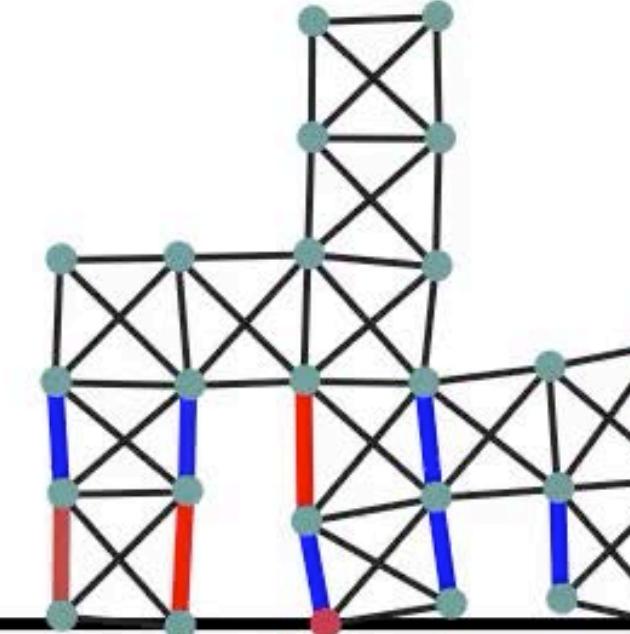
When gradient needed, without TOI the optimization fails.

Test the Optimized Controller (forward only)

Test environment with TOI



Test environment without TOI



When only forward needed, without TOI the simulator is good enough.

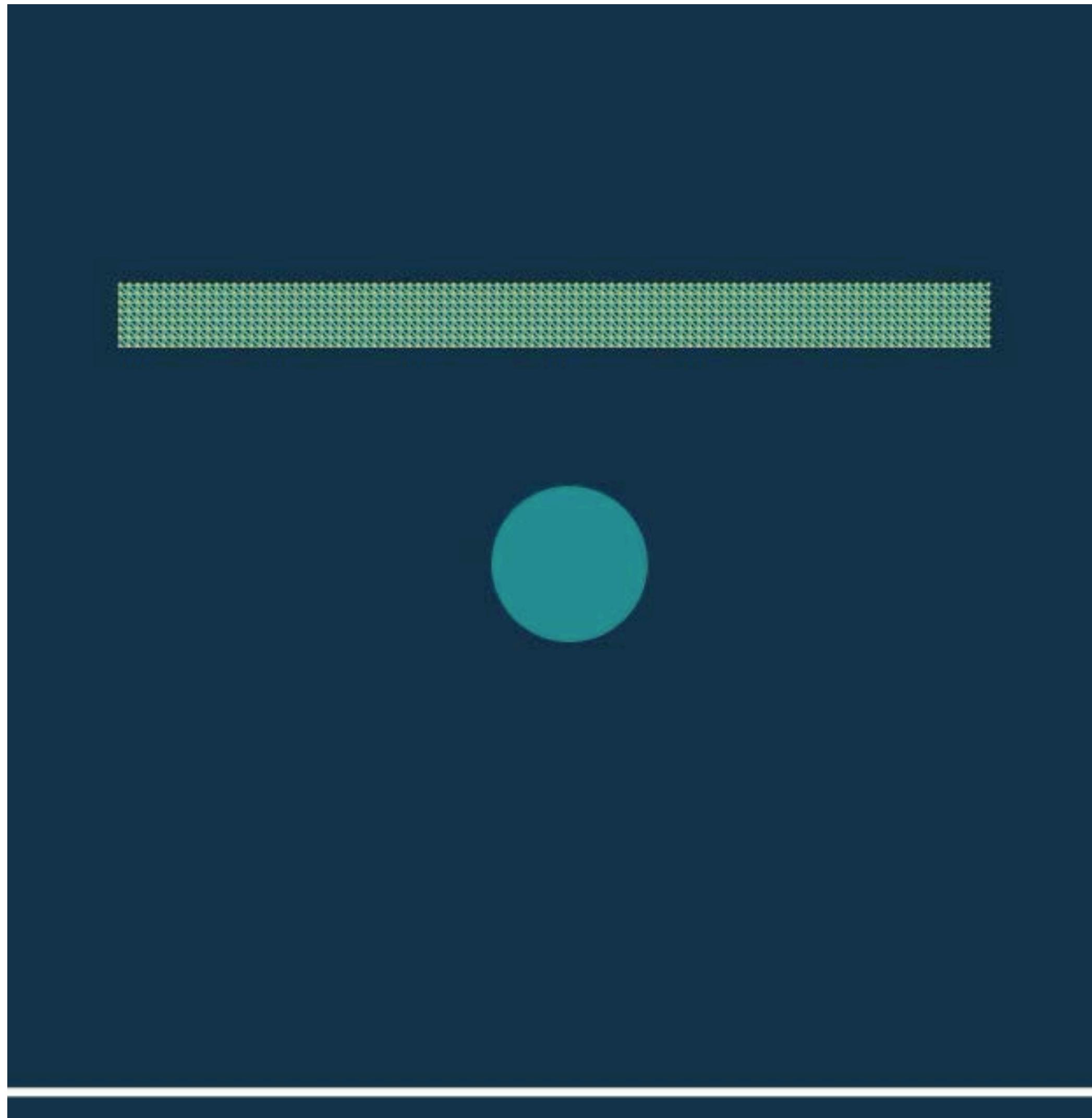
Takeaways:

Differentiating physical simulators does **not** always yield useful gradients of the physical system being simulated.

A simulation good enough for forward simulation may not be good enough for backpropagation.

Check out our paper for more details on building simulators with robust gradients, and how to use the gradients effectively.

Automatically Computing Forces by Differentiating Potential Energy

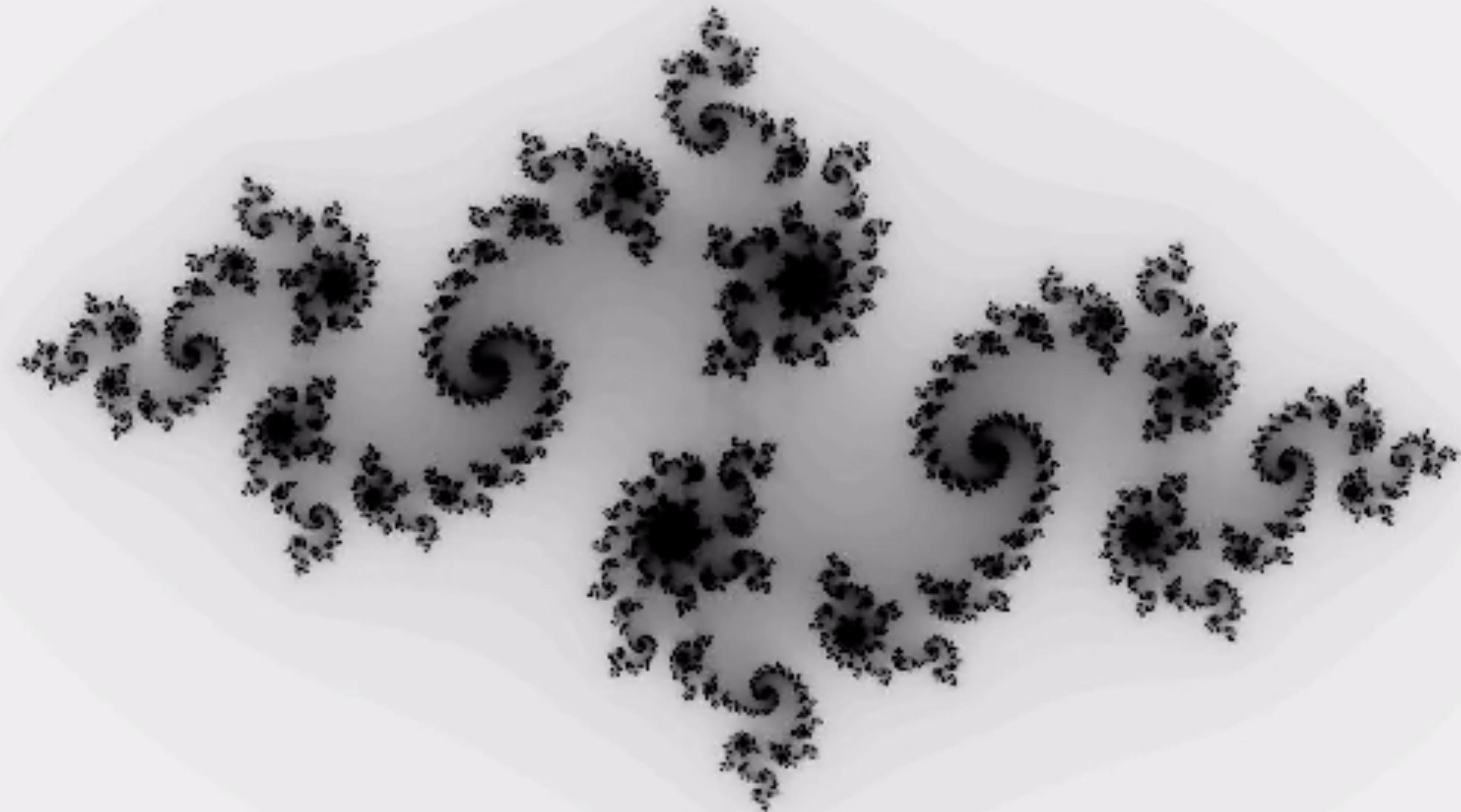


$$-f_i(\hat{x}) = \frac{\partial \Phi}{\partial \hat{x}_i}(\hat{x})$$

potential energy
↓
↑
particle force
↑
particle position

fractal.py: Your First Taichi Program

fractal.py: Your First Taichi Program



```

# fractal.py
import taichi as ti
ti.init(arch=ti.cuda) # Run on GPU by default

n = 320
pixels = ti.var(dt=ti.f32, shape=(n * 2, n))

@ti.func
def complex_sqr(z):
    return ti.Vector([z[0] * z[0] - z[1] * z[1], z[1] * z[0] * 2])

@ti.kernel
def paint(t: ti.f32):
    for i, j in pixels: # Parallelized over all pixels
        c = ti.Vector([-0.8, ti.sin(t) * 0.2])
        z = ti.Vector([float(i) / n - 1, float(j) / n - 0.5]) * 2
        iterations = 0
        while z.norm() < 20 and iterations < 50:
            z = complex_sqr(z) + c
            iterations += 1
        pixels[i, j] = 1 - iterations * 0.02

gui = ti.GUI("Fractal", (n * 2, n))
for i in range(1000000):
    paint(i * 0.03)
    gui.set_image(pixels)
    gui.show()

```

Initialization

Tensor Allocation

Computation Kernel

Main program & Visualization

Initialization⁷⁴

```
# fractal.py
import taichi as ti
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n = 320
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gui = ti.GUI("Fractal", (n * 2, n))
for i in range(1000000):
    paint(i * 0.03)
    gui.set_image(pixels)
    gui.show()
```

Tensor Allocation

Computation Kernel

Main program & Visualization

```
import taichi as ti
```

- ◆ Taichi is an embedded domain-specific language (DSL) in Python. It pretends to be a plain Python package.
- ◆ Virtually every Python programmer is capable of writing Taichi programs
 - ...after minimal learning efforts
 - also reuse the package management system, Python IDEs, and existing Python packages

ti.init

♦ Initialize a Taichi program (storage + computational kernels), with optional arguments

- arch (automatically fallback to host arch if target not found)
 - ▶ `ti.x64` (default)
 - ▶ `ti.arm`
 - ▶ `ti.cuda`
 - ▶ `ti.metal`
 - ▶ `ti.opengl`
- `debug=True/False`
- ...

```

# fractal.py
import taichi as ti
ti.init(arch=ti.cuda) # Run on GPU by default

n = 320
pixels = ti.var(dt=ti.f32, shape=(n * 2, n))

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        z = ti.Vector([float(i) / n - 1, float(j) / n - 0.5]) * 2
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```

Tensor Allocation

Computation Kernel

Main program & Visualization

(Sparse) Tensors

- ♦ Taichi is a data-oriented programming language, where dense or spatially-sparse tensors are first-class citizens
- ♦ `pixels = ti.var(dt=ti.f32, shape=(n * 2, n))` allocates a 2D dense tensor named `pixel` of size (640, 320) and type `ti.f32` (i.e. float in C).

Initialization⁷⁹

```
# fractal.py
import taichi as ti
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pixels = ti.var(dt=ti.f32, shape=(n * 2, n))

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@ti.kernel
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        z = ti.Vector([float(i) / n - 1, float(j) / n - 0.5]) * 2
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            iterations += 1
        pixels[i, j] = 1 - iterations * 0.02

gui = ti.GUI("Fractal", (n * 2, n))
for i in range(1000000):
    paint(i * 0.03)
    gui.set_image(pixels)
    gui.show()
```

Tensor Allocation

Computation Kernel

Main program
& Visualization

Kernel

```
@ti.kernel
def paint(t: ti.f32):
    for i, j in pixels: # Parallelized over all pixels
        c = ti.Vector([-0.8, ti.sin(t) * 0.2])
        z = ti.Vector([float(i) / n - 1, float(j) / n - 0.5]) * 2
        iterations = 0
        while z.norm() < 20 and iterations < 50:
            z = complex_sqrt(z) + c
            iterations += 1
        pixels[i, j] = 1 - iterations * 0.02
```

- ◆ Computation happens within Taichi kernels.
- ◆ Kernel arguments must be type-hinted
 - The language used in Taichi kernels and functions looks exactly like Python
 - The Taichi frontend compiler converts it into a language that is **compiled, statically-typed, lexically-scoped, parallel, and differentiable**.

Functions

```
@ti.func
def complex_sqr(z):
    return ti.Vector([z[0] * z[0] - z[1] * z[1], z[1] * z[0] * 2])

@ti.kernel
def paint(t: ti.f32):
    ...
    z = complex_sqr(z) + c
    ...
    ...
```

- ◆ You can also define Taichi functions with `@ti.func`, which can be called and reused by kernels and other functions.
- ◆ All function calls are force-inlined

Taichi-scope v.s. Python-scope

- ♦ Everything decorated with `ti.kernel` and `ti.func` is in Taichi-scope, which will be compiled by the Taichi compiler.
- ♦ Code outside the Taichi-scopes is simply native Python code.

```

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gui = ti.GUI("Fractal", (n * 2, n))
for i in range(1000000):
    paint(i * 0.03)
    gui.set_image(pixels)
    gui.show()

```

Initialization

Tensor Allocation

Computation Kernel

Main program
& Visualization

Interacting with Python

- Everything outside Taichi-scope (`ti.func` and `ti.kernel`) is simply Python.
- You can use your favorite Python packages (e.g. **numpy**, **pytorch**, **matplotlib**) with Taichi.
- In Python-scope, you can access Taichi tensors using plain indexing syntax, and helper functions such as **from_numpy** and **to_torch**:

```
image[42, 11] = 0.7
print(image[1, 63])
```

```
import numpy as np
pixels.from_numpy(np.random.rand(n * 2, n))
```

```
import matplotlib.pyplot as plt
plt.imshow(pixels.to_numpy())
plt.show()
```

Performance Tip:

Accessing single elements is slow.
Use `[from/to]_[numpy/torch]` as
much as possible!

Calling Taichi kernels...

```
@ti.kernel
def paint(t: ti.f32):
    ...

gui = ti.GUI("Fractal", (n * 2, n))
for i in range(1000000):
    paint(i * 0.03)           as if it is a Python function!
    gui.set_image(pixels)
    gui.show()
```

Linear Algebra

- ◆ **ti.Matrix** is for small matrices (e.g. 3x3) only. If you have 64x64 matrices, you should consider using a 2D tensor of scalars.
- ◆ **ti.Vector** is the same as **ti.Matrix**, except that it has only one column.
- ◆ Differentiate element-wise product “*****” and matrix product “**@**”
- ◆ Other useful functions:
 - **ti.transposed(A)**, **A.T()**
 - **ti.inverse(A)**
 - **ti.Matrix.abs(A)**
 - **ti.trace(A)**
 - **ti.determinant(A, type)**
 - **A.cast(type)**
 - **R, S = ti.polar_decompose(A, ti.f32)**
 - **U, sigma, V = ti.svd(A, ti.f32)**
(Note that sigma is a 3x3 diagonal matrix)

Differentiable programming

♦ 10 examples at <https://github.com/yuanming-hu/difftaichi>

pip3 install taichi



<https://github.com/taichi-dev/taichi>

「工欲善其事，必先利其器。」

——《论语·卫灵公》

Taichi is currently being developed by the Taichi community
前端语法 中间表示优化 编译器后端 文档翻译... 欢迎加入我们!

GAMES 201

Advanced Physics Engines 2020: A Hands-on Tutorial

高级物理引擎实战2020

(基于太极编程语言)

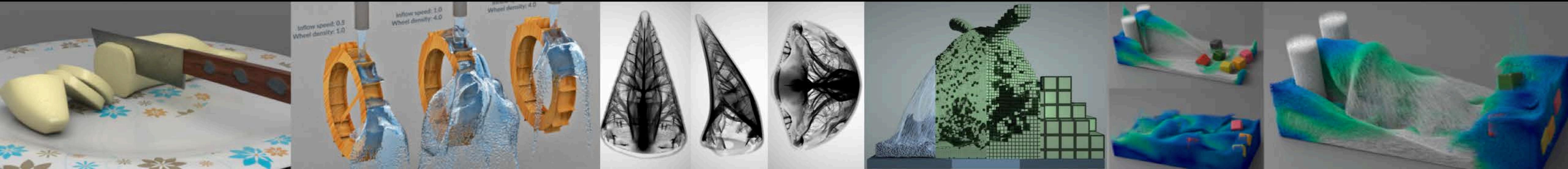
Yuanming Hu

胡渊鸣

麻省理工学院 计算机科学与人工智能实验室

MIT CSAIL

○ Taichi
Programming Language



高级物理引擎实战2020

- ◆ 课程目标：自己动手打造影视级物理引擎
- ◆ 适合人群：0-99岁的计算机图形学爱好者
- ◆ 预备知识：高等数学、Python或任何一门程序设计语言
- ◆ 课程安排：每周一北京时间晚上20:30-21:30 共10节课
- ◆ 课程内容：Taichi语言基础 刚体 液体 烟雾 弹塑性体 PIC/FLIP法 Krylov-子空间求解器 预条件 无矩阵法 多重网格 弱形式与有限元 隐式积分器 辛积分器 拓扑优化 带符号距离场 自由表面追踪 物质点法 大规模物理效果渲染 现代处理器微架构 内存层级 并行编程 GPU编程 稀疏数据结构 可微编程...

2020年六一儿童节开课 不见不散！

Questions are welcome!